

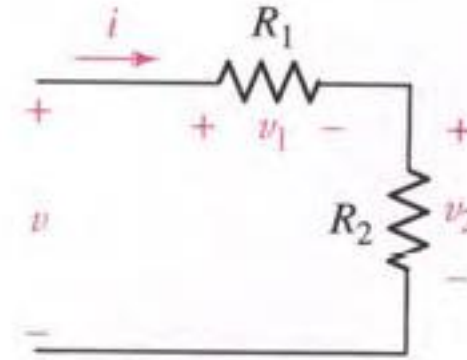
# Chapter 3

## Voltage and current laws

# VOLTAGE AND CURRENT DIVISION

Voltage divider rule (VDR) for resistors in series

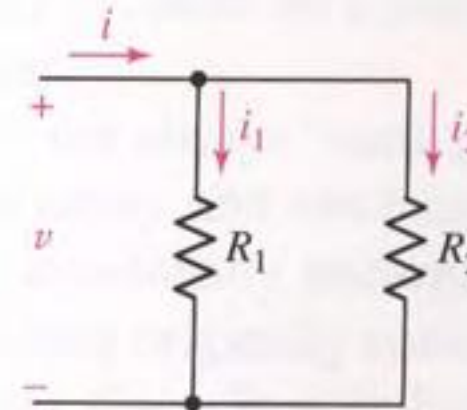
$$v_k = \frac{R_k}{R_1 + R_2 + \dots + R_N} v$$



Current divider rule (CDR) : only for two parallel resistors

$$i_2 = i \frac{R_1}{R_1 + R_2}$$

$$i_1 = i \frac{R_2}{R_1 + R_2}$$

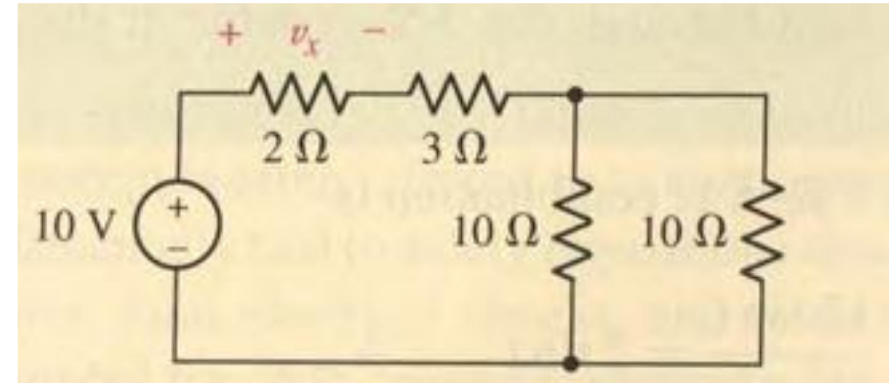


## Question

Using VDR find  $V_x$

$$R_{T1} = 5\Omega$$

$$V_x = \frac{10(2)}{2+3+5} = \frac{20}{10} = 2v$$



Question : find  $i_1, i_2, v_3$

$$R_{t1} = \frac{240(40+20)}{240+(40+20)} = \frac{240(60)}{240+60} = \frac{14400}{300} = 48\Omega$$

$$R_{t2} = 2 + R_{t1} = 2 + 48 = 50\Omega$$

$$R_{t3} = \frac{50(50)}{50+50} = 25\Omega$$

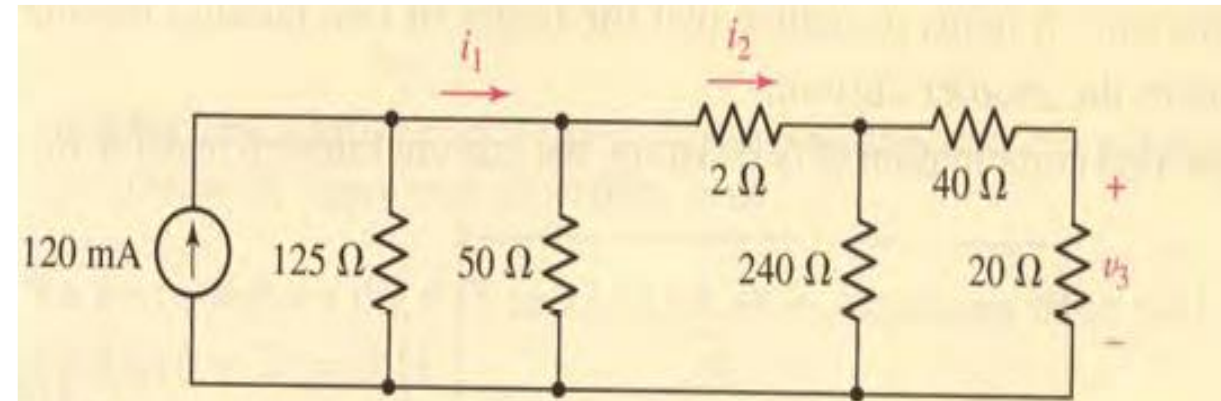
CDR

$$i_1 = \frac{120m(125)}{125+25} = \frac{15}{150} = 0.1A = 100mA$$

$$i_2 = \frac{i_1(50)}{50+50} = \frac{100mA(50)}{100} = 50mA$$

$$i_3 = \frac{i_2(240)}{240+60} = \frac{50mA(240)}{300} = 40mA$$

$$v_3 = 20(i_3) = 20(40mA) = 800mv = 0.8v$$

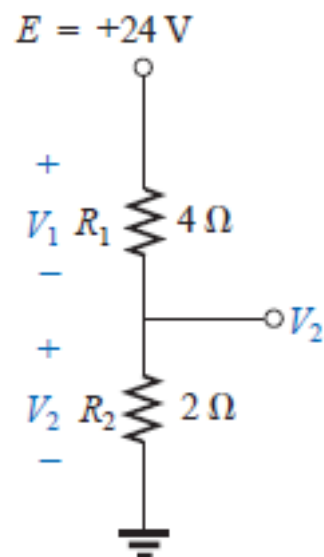


### EXAMPLE

Using the voltage divider rule, determine the voltages  $V_1$  and  $V_2$  of Fig.

$$V_1 = \frac{R_1 E}{R_1 + R_2} = \frac{(4 \Omega)(24 \text{ V})}{4 \Omega + 2 \Omega} = 16 \text{ V}$$

$$V_2 = \frac{R_2 E}{R_1 + R_2} = \frac{(2 \Omega)(24 \text{ V})}{4 \Omega + 2 \Omega} = 8 \text{ V}$$



### EXAMPLE

For the network of Fig.

- Calculate  $V_{ab}$ .
- Determine  $V_b$ .

#### Solutions:

- a. Voltage divider rule:

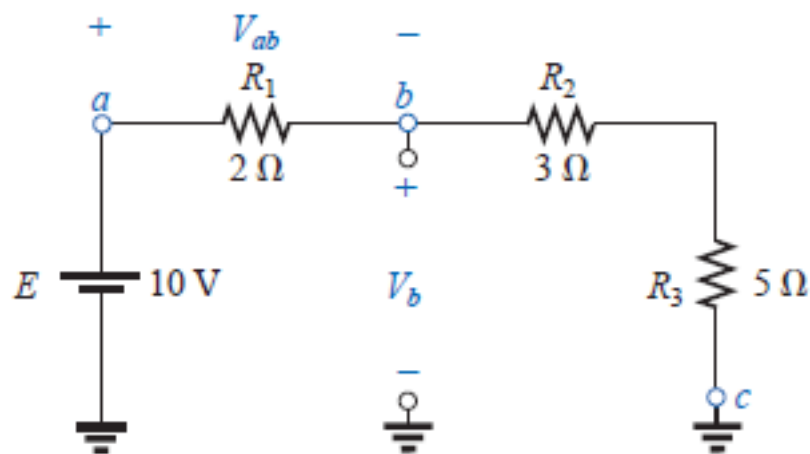
$$V_{ab} = \frac{R_1 E}{R_T} = \frac{(2 \Omega)(10 \text{ V})}{2 \Omega + 3 \Omega + 5 \Omega} = +2 \text{ V}$$

- b. Voltage divider rule:

$$V_b = V_{R_2} + V_{R_3} = \frac{(R_2 + R_3)E}{R_T} = \frac{(3 \Omega + 5 \Omega)(10 \text{ V})}{10 \Omega} = 8 \text{ V}$$

or  $V_b = V_a - V_{ab} = E - V_{ab} = 10 \text{ V} - 2 \text{ V} = 8 \text{ V}$

- c.  $V_c = \text{ground potential} = 0 \text{ V}$



**EXAMPLE**

Design the voltage divider of Fig. such that  $V_{R_1} = 4V_{R_2}$ .

**Solution:** The total resistance is defined by

$$R_T = \frac{E}{I} = \frac{20 \text{ V}}{4 \text{ mA}} = 5 \text{ k}\Omega$$

Since  $V_{R_1} = 4V_{R_2}$ ,

$$R_1 = 4R_2$$

Thus

$$R_T = R_1 + R_2 = 4R_2 + R_2 = 5R_2$$

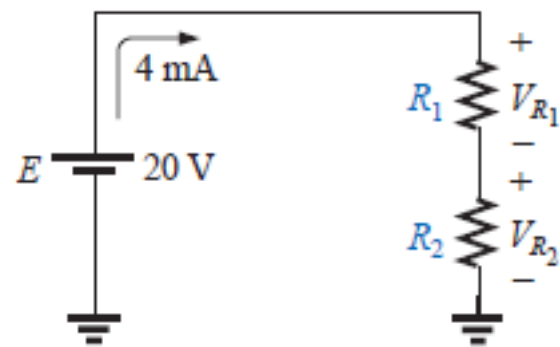
and

$$5R_2 = 5 \text{ k}\Omega$$

$$R_2 = 1 \text{ k}\Omega$$

and

$$R_1 = 4R_2 = 4 \text{ k}\Omega$$



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## EXAMPLE

- Determine  $V_2$  using Kirchhoff's voltage law.
- Determine  $I$ .
- Find  $R_1$  and  $R_3$ .

### Solutions:

- Kirchhoff's voltage law (clockwise direction):

$$-E + V_3 + V_2 + V_1 = 0$$

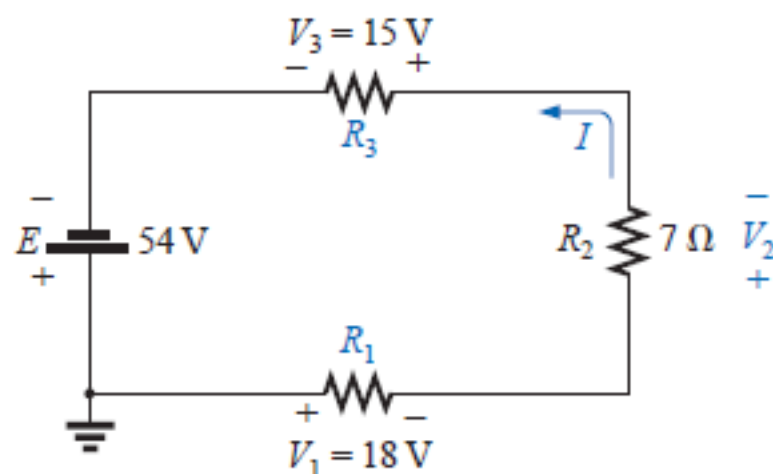
or 
$$E = V_1 + V_2 + V_3$$

and 
$$V_2 = E - V_1 - V_3 = 54 \text{ V} - 18 \text{ V} - 15 \text{ V} = \mathbf{21 \text{ V}}$$

- $$I = \frac{V_2}{R_2} = \frac{21 \text{ V}}{7 \Omega} = \mathbf{3 \text{ A}}$$

- $$R_1 = \frac{V_1}{I} = \frac{18 \text{ V}}{3 \text{ A}} = \mathbf{6 \Omega}$$

$$R_3 = \frac{V_3}{I} = \frac{15 \text{ V}}{3 \text{ A}} = \mathbf{5 \Omega}$$



## EXAMPLE

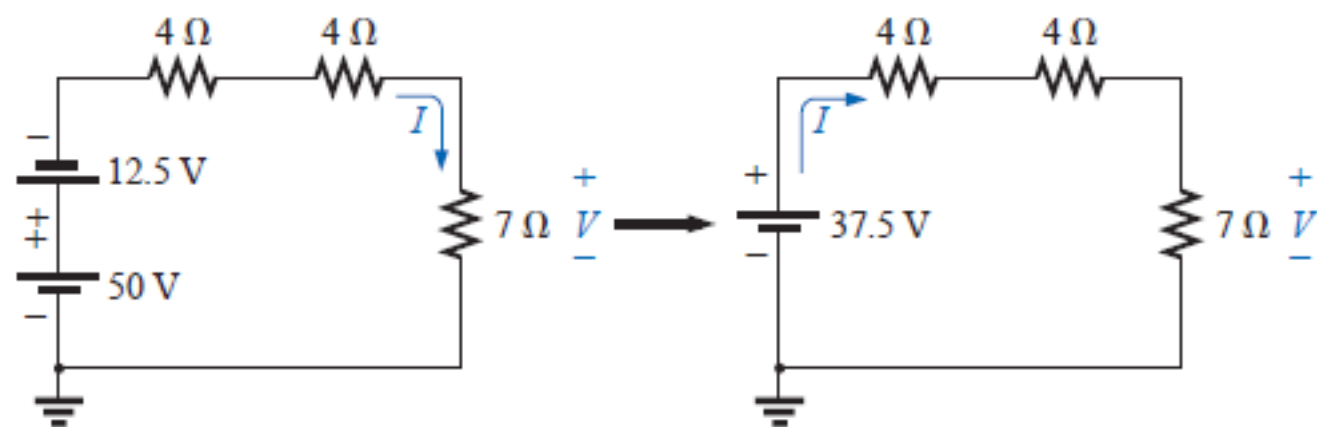
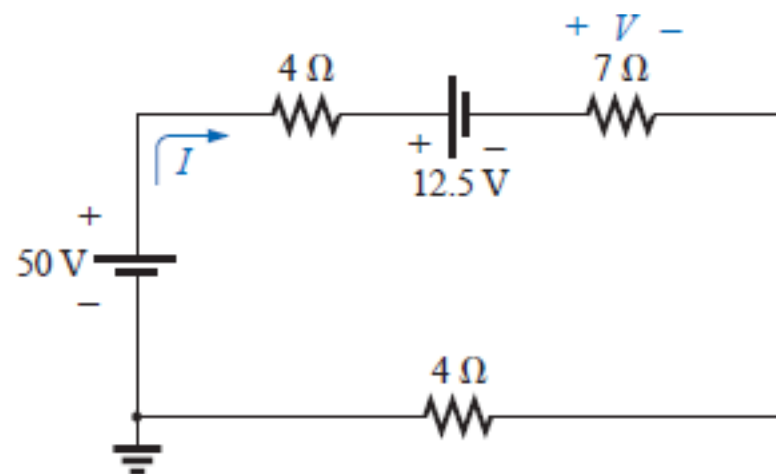
Determine  $I$  and the voltage across the  $7\text{-}\Omega$  resistor

**Solution:** The network is redrawn in Fig. 5.22.

$$R_T = (2)(4\ \Omega) + 7\ \Omega = 15\ \Omega$$

$$I = \frac{E}{R_T} = \frac{37.5\ \text{V}}{15\ \Omega} = 2.5\ \text{A}$$

$$V_{7\Omega} = IR = (2.5\ \text{A})(7\ \Omega) = 17.5\ \text{V}$$



**EXAMPLE** Find  $V_1$  and  $V_2$  for the network

**Solution:** For path 1, starting at point  $a$  in a clockwise direction:

$$+25 \text{ V} - V_1 + 15 \text{ V} = 0$$

and

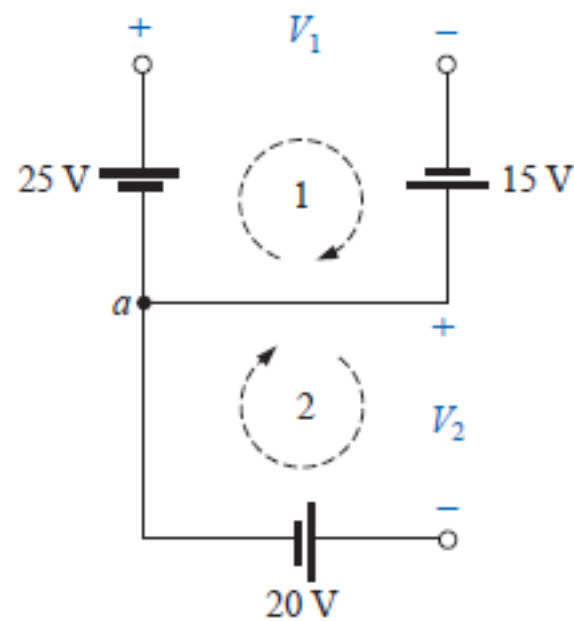
$$V_1 = \mathbf{40 \text{ V}}$$

For path 2, starting at point  $a$  in a clockwise direction:

$$-V_2 - 20 \text{ V} = 0$$

and

$$V_2 = \mathbf{-20 \text{ V}}$$





## EXAMPLE

- Find the total resistance
- Calculate the source current  $I_s$ .
- Determine the voltages  $V_1$ ,  $V_2$ , and  $V_3$ .
- Calculate the power dissipated by  $R_1$ ,  $R_2$ , and  $R_3$ .
- Determine the power delivered by the source, and compare it to the sum of the power levels of part (d).

### Solutions:

a.  $R_T = R_1 + R_2 + R_3 = 2 \Omega + 1 \Omega + 5 \Omega = 8 \Omega$

b.  $I_s = \frac{E}{R_T} = \frac{20 \text{ V}}{8 \Omega} = 2.5 \text{ A}$

c.  $V_1 = IR_1 = (2.5 \text{ A})(2 \Omega) = 5 \text{ V}$   
 $V_2 = IR_2 = (2.5 \text{ A})(1 \Omega) = 2.5 \text{ V}$   
 $V_3 = IR_3 = (2.5 \text{ A})(5 \Omega) = 12.5 \text{ V}$

d.  $P_1 = V_1 I_1 = (5 \text{ V})(2.5 \text{ A}) = 12.5 \text{ W}$   
 $P_2 = I_2^2 R_2 = (2.5 \text{ A})^2 (1 \Omega) = 6.25 \text{ W}$   
 $P_3 = V_3^2 / R_3 = (12.5 \text{ V})^2 / 5 \Omega = 31.25 \text{ W}$

e.  $P_{\text{del}} = EI = (20 \text{ V})(2.5 \text{ A}) = 50 \text{ W}$   
 $P_{\text{del}} = P_1 + P_2 + P_3$   
 $50 \text{ W} = 12.5 \text{ W} + 6.25 \text{ W} + 31.25 \text{ W}$   
 $50 \text{ W} = 50 \text{ W} \quad (\text{checks})$

