

Calculating Sun Angles

Today you will calculate the angle of the sun at NOON (12:00) for different locations on Earth.

Calculating Sun Angles

You will be working with complementary angles.

Remember, complementary angles always add up to 90° .

Calculating Sun Angles

High sun angles (45° to 90°) mean more intense sunlight. ●

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Calculating Sun Angles

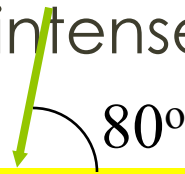
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Low sun angles (0° to 45°) mean less intense sunlight. ●

Calculating Sun Angles

High sun angles (45° to 90°) mean more intense sunlight. ●



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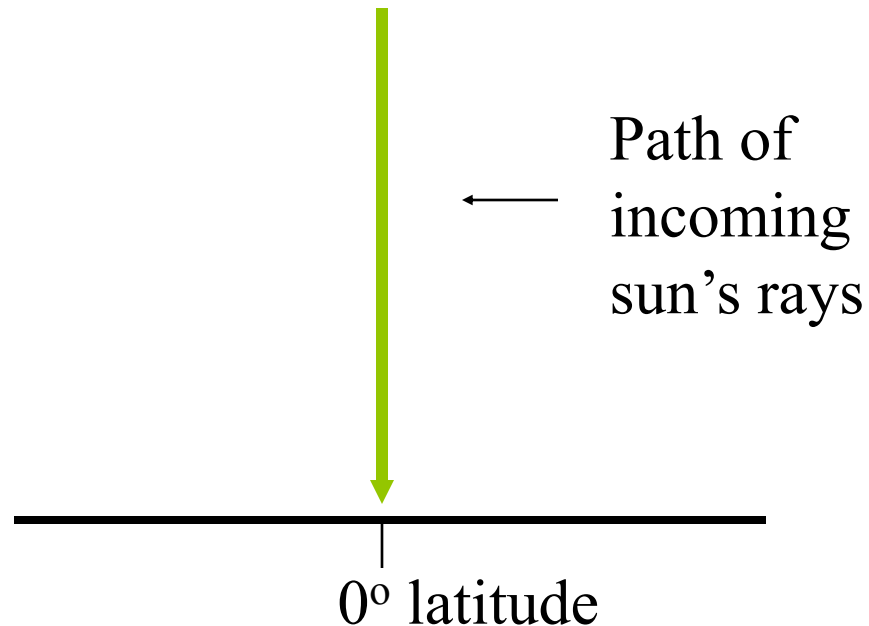


Latitude of 90° Sun Angle Changes

Over the year, the latitude where the sun's rays form a 90° angle, at noon, with the surface, moves slowly between the Tropic of Cancer and the Tropic of Capricorn.

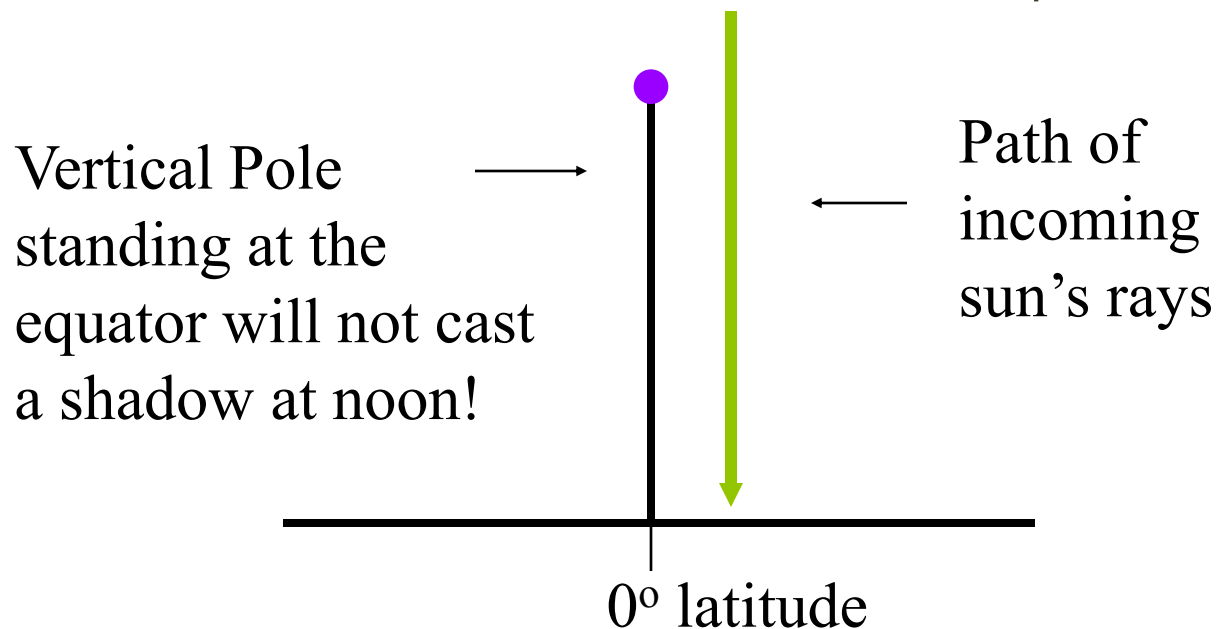
Equinox

On March 22 and on September 22, the sun's rays form a 90° angle at noon at the equator.



Equinox

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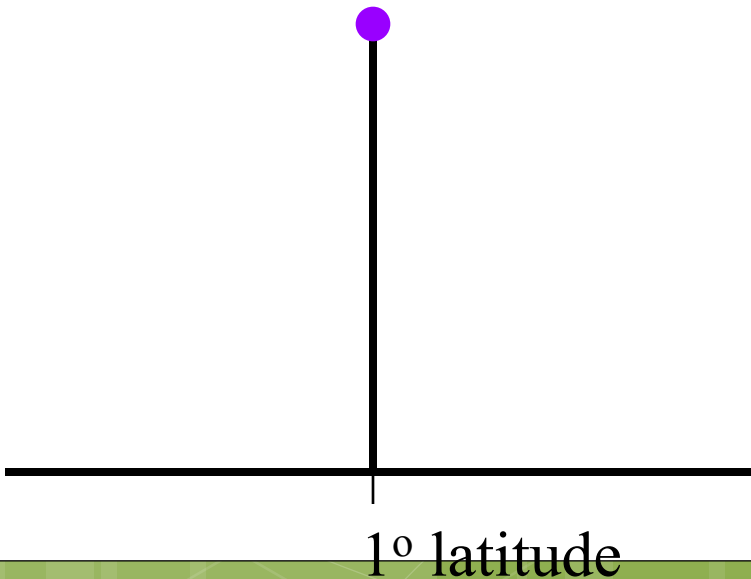


Equinox

At an Equinox, for every degree of latitude you move away from the equator, the sun angle at noon decreases by 1 degree.

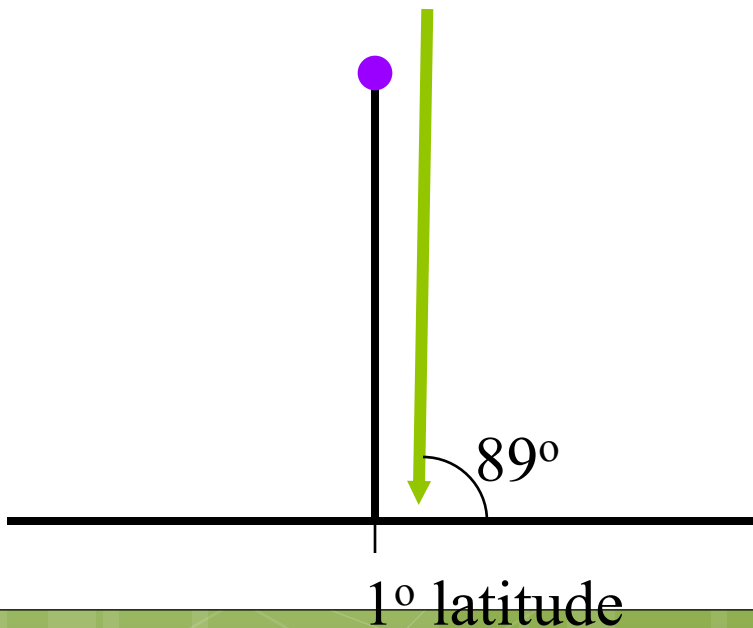
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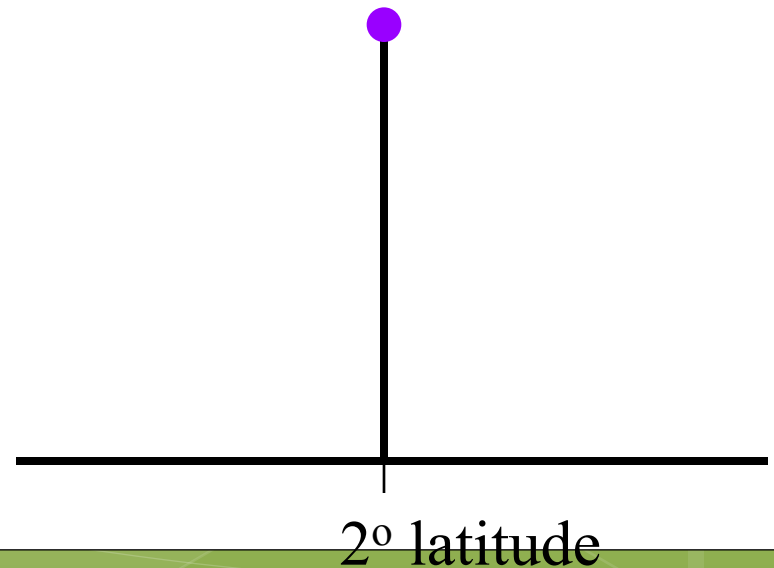
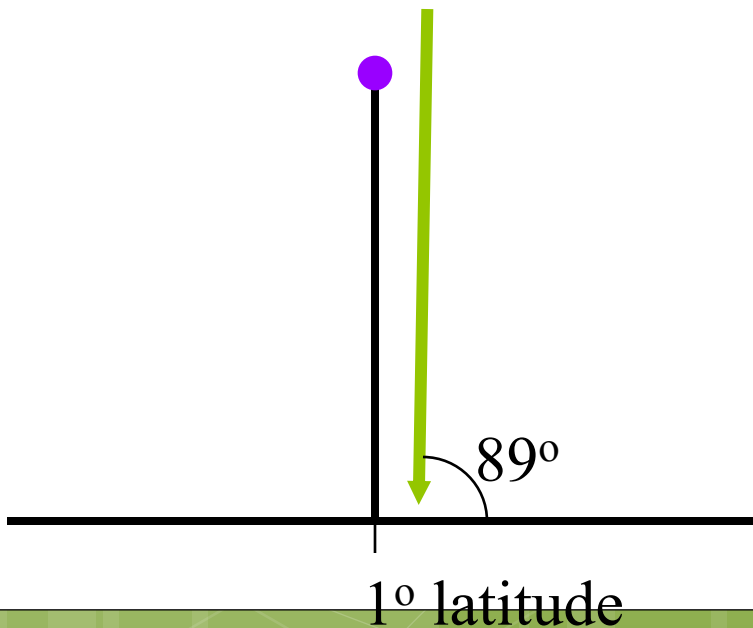
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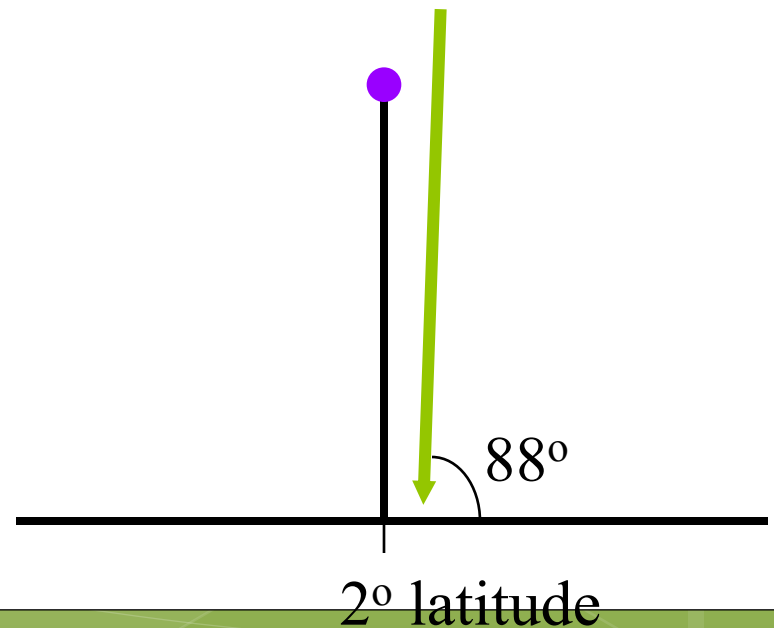
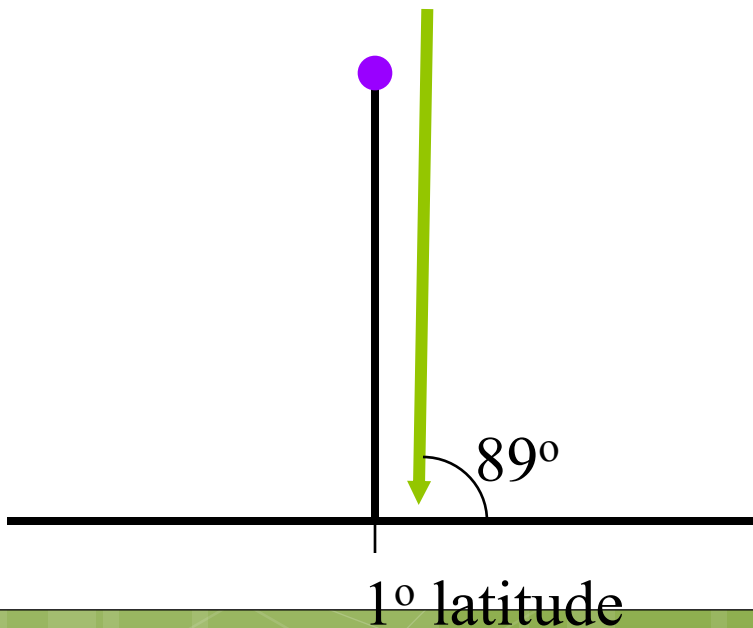
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Solstices

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June 22

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June 22

The sun forms a 90° angle at noon at 23.5° N ●

Solstices

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The sun forms a 90° angle at noon at 23.5° N ●

This latitude is called the Tropic of Cancer. ●

Solstices

June 22

- The sun forms a 90° angle at noon at 23.5° N ●
- This latitude is called the Tropic of Cancer. ●
- This is the summer solstice for the Northern Hemisphere. ●

Solstices

June 22

The sun forms a 90° angle at noon at 23.5° N ●

This latitude is called the Tropic of Cancer. ●

This is the summer solstice for the Northern Hemisphere. ●

This is the winter solstice for the Southern Hemisphere. ●



Solstices

December 22

Solstices

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The sun forms a 90° angle at noon at 23.5° S ●

Solstices

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The sun forms a 90° angle at noon at 23.5° S ●

This latitude is called the Tropic of Capricorn ●

Solstices

December 22

The sun forms a 90° angle at noon at 23.5° S ●

This latitude is called the Tropic of Capricorn ●

This is winter solstice for the Northern ●
Hemisphere.

Solstices

December 22

The sun forms a 90° angle at noon at 23.5° S ●

This latitude is called the Tropic of Capricorn ●

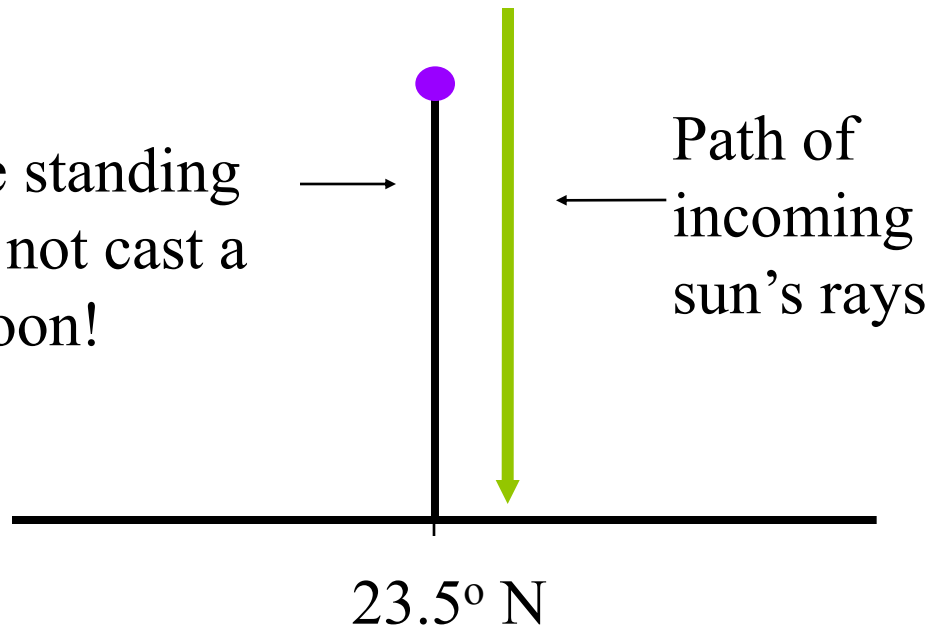
This is winter solstice for the Northern ●
Hemisphere.

This is the summer solstice for the Southern ●
Hemisphere.

Solstices

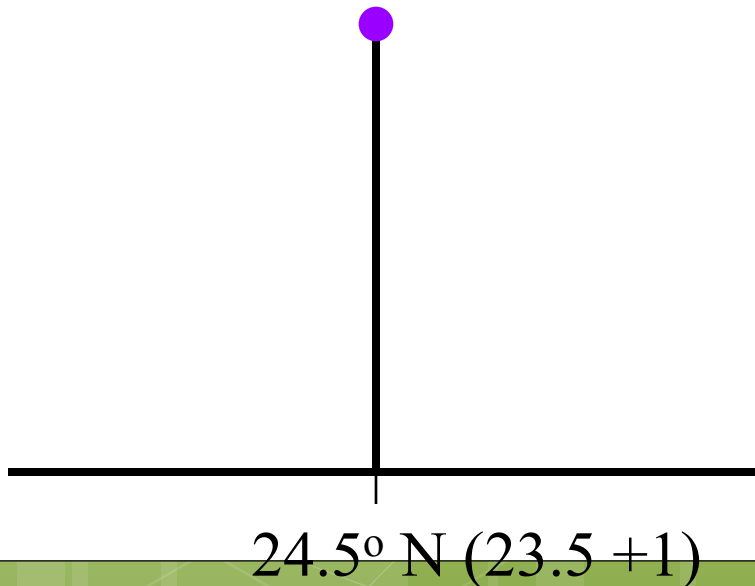
On the summer solstice the sun's rays form a 90° angle at noon at 23.5° N

Vertical Pole standing
at 23.5° will not cast a
shadow at noon!



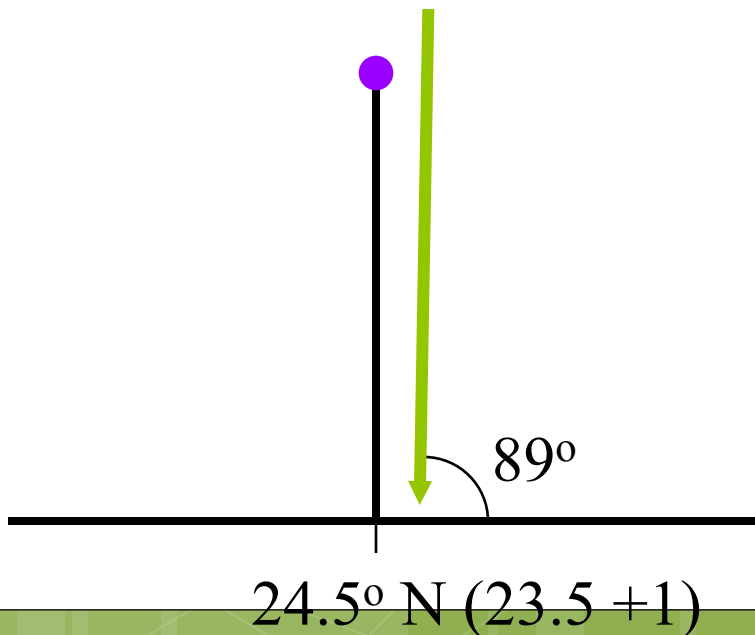
Solstices

On the summer solstice, for every degree of latitude you move away from 23.5° , the sun angle at noon decreases by 1 degree.



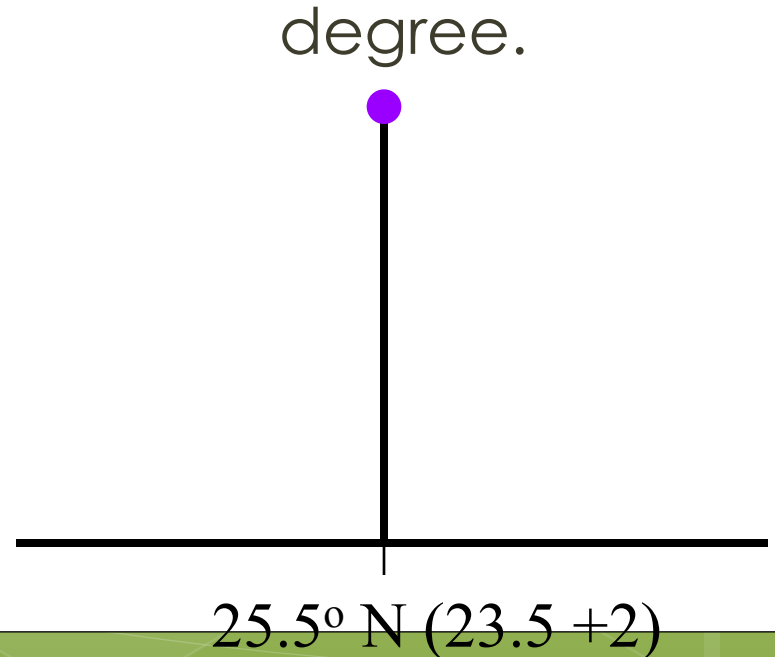
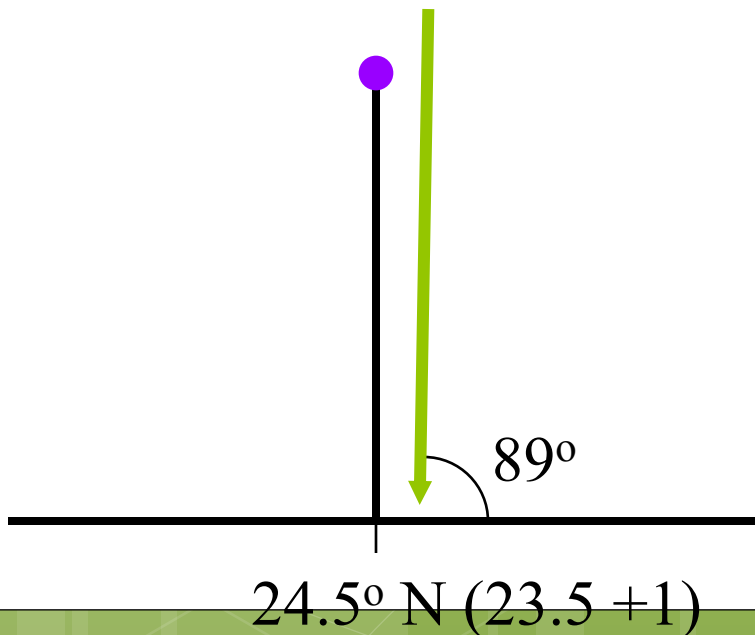
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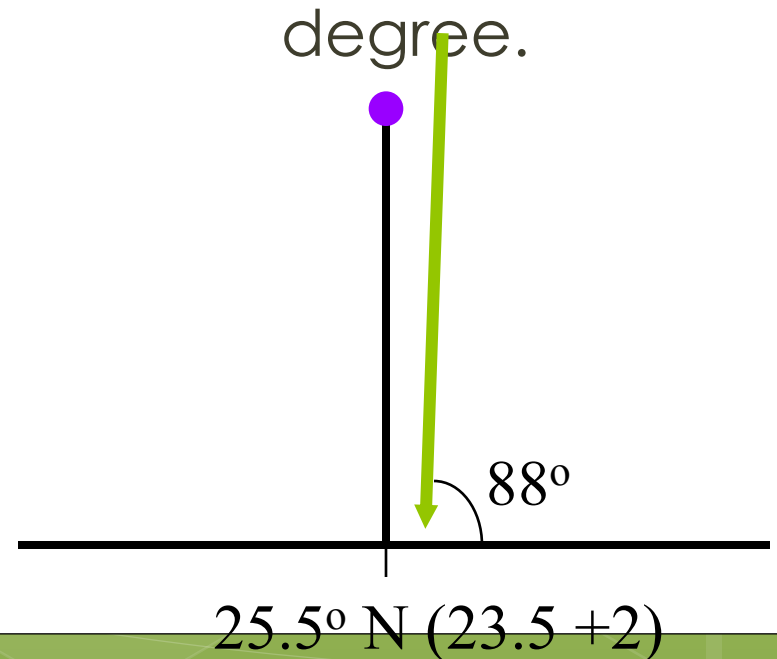
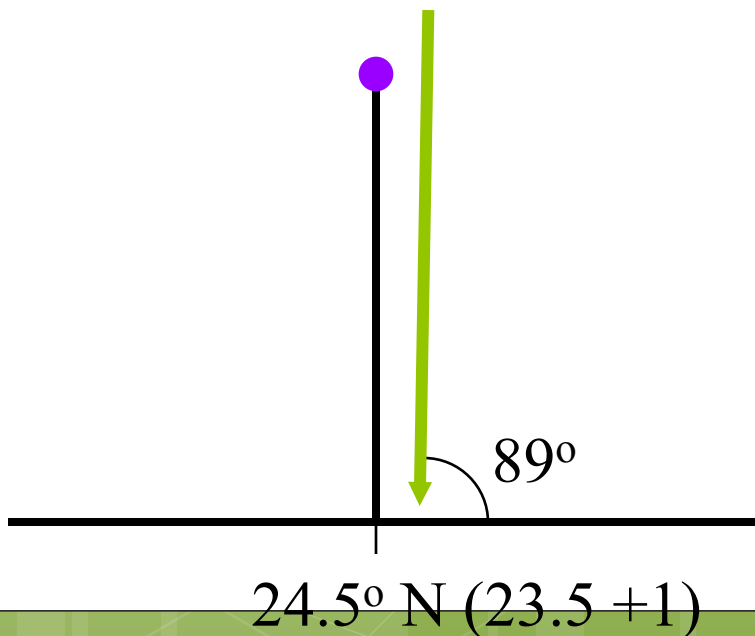
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Noon Sun Angle Equation

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You are about to find the angle of the sun 
at noon at different latitudes.

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To do this, you will use the following formula: 

Noon Sun Angle Equation

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$$\text{Noon Sun Angle} = 90 - \text{Zenith Angle}$$

Noon Sun Angle Equation

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Noon Sun Angle Equation

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You need to subtract from 90 because the angles you are working with are complementary.

Noon Sun Angle Equation

$$\text{Sun Angle} = 90 - \text{Zenith Angle}$$

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The zenith angle is the distance between the subsolar point and the latitude you are “at”.

Noon Sun Angle Equation

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The zenith angle is the distance between the subsolar point and the latitude you are “at”.

The subsolar point is the latitude where the sun’s rays form a 90° angle at noon.

Noon Sun Angle Equation


$$\text{Sun Angle} = 90 - \text{Zenith Angle}$$

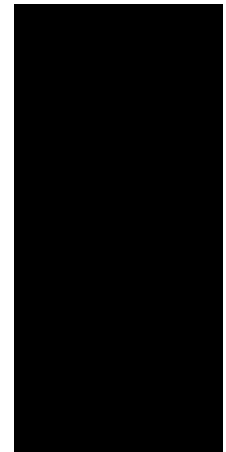
The zenith angle is the distance between the subsolar point and the latitude you are “at”.

The subsolar point is the latitude where the sun’s rays form a 90° angle at noon.

In other words: Noon Sun Angle = $90 - (\text{latitude you are at} \pm \text{latitude where sun is } 90^\circ \text{ at noon})$

Noon Sun Angle Equation

To calculate the zenith angle between  the subsolar point and the latitude you are “at” requires a bit of thought....



Noon Sun Angle Equation

If the subsolar point and your latitude are \bullet
in the same hemisphere, subtract.

Noon Sun Angle Equation

If the **subsolar point** and your latitude are **◉**
in the **same** hemisphere, **subtract**.

Example: **Subsolar Point** = 0° **◉**

Noon Sun Angle Equation

If the **subsolar point** and your latitude are **◉**
in the **same** hemisphere, **subtract**.

Example: **Subsolar Point** = 0° ◉

You are at 45°N . ◉

Noon Sun Angle Equation

If the **subsolar point** and your latitude are **in the same hemisphere, subtract.**

Example: **Subsolar Point** = 0°

You are at 45°N .

Zenith Angle = $(45 - 0) =$

Noon Sun Angle Equation

If the **subsolar point** and your latitude are **in the same hemisphere, subtract.**

Example: **Subsolar Point** = 0°

You are at 45°N .

Zenith Angle = $(45 - 0) = 45$

Noon Sun Angle Equation

If the subsolar point and your latitude are ◉ in different hemispheres, add.

Noon Sun Angle Equation

If the subsolar point and your latitude are in different hemispheres, add.

Example: Subsolar Point = 23.5° S

Noon Sun Angle Equation

If the subsolar point and your latitude are in different hemispheres, add.

Example: Subsolar Point = 23.5° S

You are at 45° N.

Noon Sun Angle Equation

If the subsolar point and your latitude are in different hemispheres, add.

Example: Subsolar Point = 23.5° S

You are at 45°N.

$$\text{Zenith Angle} = (45 + 23.5) =$$

Noon Sun Angle Equation

If the subsolar point and your latitude are in different hemispheres, add.

Example: Subsolar Point = 23.5° S

You are at 45°N.

$$\text{Zenith Angle} = (45 + 23.5) = 68.5$$

Noon Sun Angle Equation

If the **subsolar point** and your latitude are **in the same hemisphere**, **subtract**.

If the **subsolar point** and your latitude are **in different hemispheres**, **add**.

Noon Sun Angle Equation

Let's do some problems together! ●



Noon Sun Angle Equation

It is the June 22nd solstice (summer). ➤

Noon Sun Angle Equation

It is the June 22nd solstice (summer). ➤

The subsolar point is 23.5° N ➤

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You are visiting a friend in Brussels, Belgium ➤

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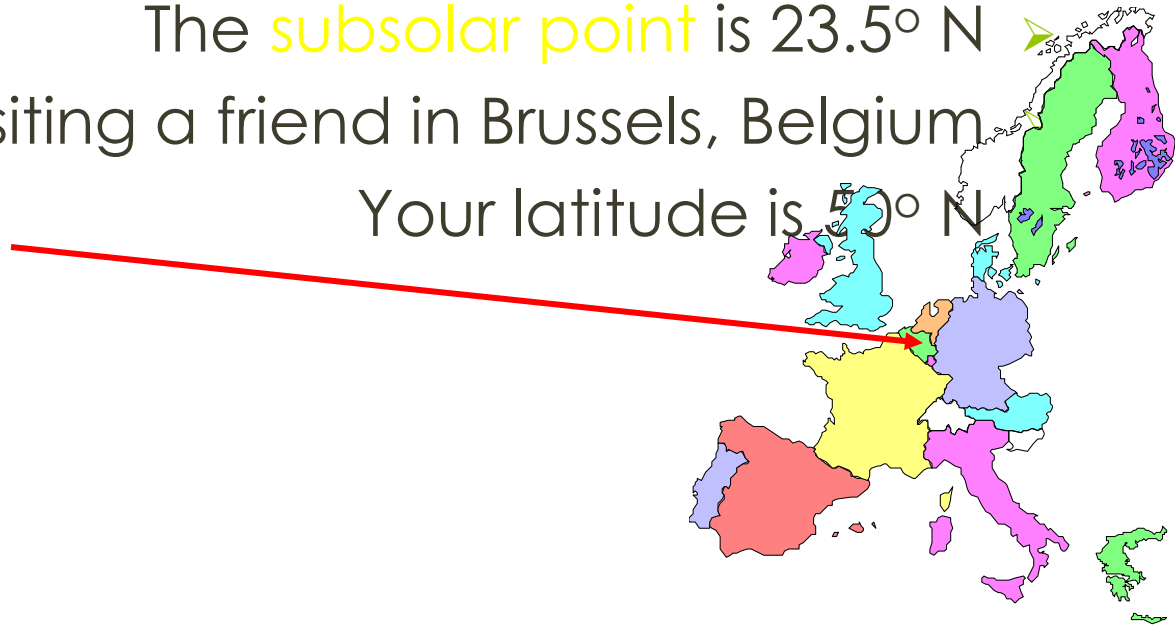
Noon Sun Angle Equation

It is the June 22nd solstice (summer). ➤

The subsolar point is 23.5° N ➤

You are visiting a friend in Brussels, Belgium

Your latitude is 50° N



Noon Sun Angle Equation

It is the June 22nd solstice (summer). ➤

The subsolar point is 23.5° N ➤

You are visiting a friend in Brussels, Belgium

Your latitude is 50° N

What is the angle of the sun at noon?



Noon Sun Angle Equation

Noon Sun Angle = $90 - \text{Zenith Angle}$

Noon Sun Angle Equation

$$\text{Noon Sun Angle} = 90 - \text{Zenith Angle}$$

Zenith Angle: **Subsolar point** & your location are in the **same** hemisphere, **subtract!**

Noon Sun Angle Equation

Noon Sun Angle = $90 - \text{Zenith Angle}$

Zenith Angle: **Subsolar point** & your location are in the **same** hemisphere, **subtract!**

$$50 - 23.5 =$$

Noon Sun Angle Equation

$$\text{Noon Sun Angle} = 90 - \text{Zenith Angle}$$

Zenith Angle: **Subsolar point** & your location
are in the **same** hemisphere, **subtract!**

$$50 - 23.5 = 26.5$$

Noon Sun Angle Equation

$$\text{Noon Sun Angle} = 90 - \text{Zenith Angle}$$

Zenith Angle: **Subsolar point** & your location are in the **same** hemisphere, **subtract!**

$$50 - 23.5 = 26.5$$

$$\text{Noon Sun Angle} = 90 - 26.5 =$$

Noon Sun Angle Equation

$$\text{Noon Sun Angle} = 90 - \text{Zenith Angle}$$

Zenith Angle: **Subsolar point** & your location are in the **same** hemisphere, **subtract!**

$$50 - 23.5 = 26.5$$

$$\text{Noon Sun Angle} = 90 - 26.5 = 63.5^\circ$$

Noon Sun Angle Equation

A noon sun angle of 63.5° is considered a high angle. ➤

This answer makes sense because it is summer time where you are. ➤

Noon Sun Angle Equation

Good Job!!!



Let's try another one!

Noon Sun Angle Equation

It is the March 22nd. ➤

Noon Sun Angle Equation

It is the March 22nd. ➤

It is the Spring Equinox. ➤

Noon Sun Angle Equation

- It is the March 22nd. ➤
- It is the Spring Equinox. ➤
- The **subsolar point** is 0° ➤

Noon Sun Angle Equation

- It is the March 22nd. ➤
- It is the Spring Equinox. ➤
- The **subsolar point** is 0° ➤
- You are going to go skiing in New Zealand. ➤

Noon Sun Angle Equation

It is the

It is the Spr

The **subsola**

You are going to go skiing in New Zealand. ➤



Noon Sun Angle Equation

It is the

It is the Spr

The **subsola**

You are going to go skiing in New Zealand. ➤

Your latitude is 43° S ➤



Noon Sun Angle Equation

It is the

It is the Spr

The **subsola**



You are going to go skiing in New Zealand. ➤

Your latitude is 43° S ➤

What is the angle of the sun at noon? ➤

Noon Sun Angle Equation

$$\text{Noon Sun Angle} = 90 - \text{Zenith Angle}$$

Noon Sun Angle Equation

$$\text{Noon Sun Angle} = 90 - \text{Zenith Angle}$$

Zenith Angle: **Subsolar point** & your location are in the **same** hemisphere, **subtract!**

Noon Sun Angle Equation

$$\text{Noon Sun Angle} = 90 - \text{Zenith Angle}$$

Zenith Angle: **Subsolar point** & your location
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$$43 - 0 =$$

Noon Sun Angle Equation

$$\text{Noon Sun Angle} = 90 - \text{Zenith Angle}$$

Zenith Angle: **Subsolar point** & your location
are in the **same** hemisphere, **subtract!**

$$43 - 0 = 43$$

Noon Sun Angle Equation

$$\text{Noon Sun Angle} = 90 - \text{Zenith Angle}$$

Zenith Angle: **Subsolar point** & your location
are in the **same** hemisphere, **subtract!**

$$43 - 0 = 43$$

$$\text{Noon Sun Angle} = 90 - 43 =$$

Noon Sun Angle Equation

Noon Sun Angle = $90 - \text{Arc Distance}$

Arc Distance: **Subsolar point** & your location are in the **same** hemisphere, **subtract!**

$$43 - 0 = 43$$

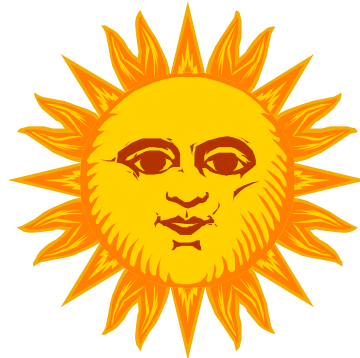
$$\text{Noon Sun Angle} = 90 - 43 = 47^\circ$$

Noon Sun Angle Equation

- A noon sun angle of 47° is a moderate angle.
- This answer makes sense because it is spring time where you are.
- The snow may be melting, but you can probably still get in a few runs!

Noon Sun Angle Equation

Excellent work!



Let's try one last problem together.

Noon Sun Angle Equation

It is the December 22nd. ➤

Noon Sun Angle Equation

It is the December 22nd. ➤

It is the Winter Solstice. ➤

Noon Sun Angle Equation

It is the December 22nd. ➤

It is the Winter Solstice. ➤

The **subsolar point** is 23.5° S ➤

Noon Sun Angle Equation

It is the December 22nd. ➤

It is the Winter Solstice. ➤

The **subsolar point** is 23.5° S ➤

You just won a trip to Oulu, Finland ➤

Noon Sun Angle Equation

It is the December 22nd. ➤

It is the Winter Solstice. ➤

The subsolar point is 23.5°

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Noon Sun Angle Equation

It is the December 22nd. ➤

It is the Winter Solstice. ➤

The subsolar point is 23.5°

You just won a trip to Oulu, Finland.



Noon Sun Angle Equation

It is the December 22nd. ➤

It is the Winter Solstice. ➤

The subsolar point is 23.5° . ➤

You just won a trip to Oulu, Finland. ➤

Your latitude is 64° N ➤



Noon Sun Angle Equation

It is the December 22nd. ➤

It is the Winter Solstice. ➤

The subsolar point is 23.5° . ➤

You just won a trip to Oulu, Finland. ➤

Your latitude is 64° N. ➤

What is the angle of the sun at noon? ➤



Noon Sun Angle Equation

$$\text{Noon Sun Angle} = 90 - \text{Arc Distance}$$

Noon Sun Angle Equation

Noon Sun Angle = $90 - \text{Arc Distance}$

Arc Distance: **Subsolar point** & your location are in **different** hemispheres,
add!

Noon Sun Angle Equation

Noon Sun Angle = $90 - \text{Arc Distance}$

Arc Distance: **Subsolar point** & your location are in **different** hemispheres,
add!

$$64 + 23.5 =$$

Noon Sun Angle Equation

Noon Sun Angle = $90 - \text{Arc Distance}$

Arc Distance: **Subsolar point** & your location are in **different** hemispheres,
add!

$$64 + 23.5 = 87.5$$

Noon Sun Angle Equation

Noon Sun Angle = $90 - \text{Arc Distance}$

Arc Distance: **Subsolar point** & your location are in **different** hemispheres, **add!**

$$64 + 23.5 = 87.5$$

$$\text{Noon Sun Angle} = 90 - 87.5 =$$

Noon Sun Angle Equation

Noon Sun Angle = $90 - \text{Arc Distance}$

Arc Distance: **Subsolar point** & your location are in **different** hemispheres,
add!

$$64 + 23.5 = 87.5$$

$$\text{Noon Sun Angle} = 90 - 87.5 = 2.5^\circ$$

Noon Sun Angle Equation

A noon sun angle of is 2.5° a VERY low angle. ➤

This answer makes sense because it is wintertime where you are. ➤

You will need to take a lot of warm clothes for this trip! ➤

Noon Sun Angle Equation

Congratulations!

You get to try some of these problems on your own. All the hints you've been shown are on your worksheet!

Good Luck

