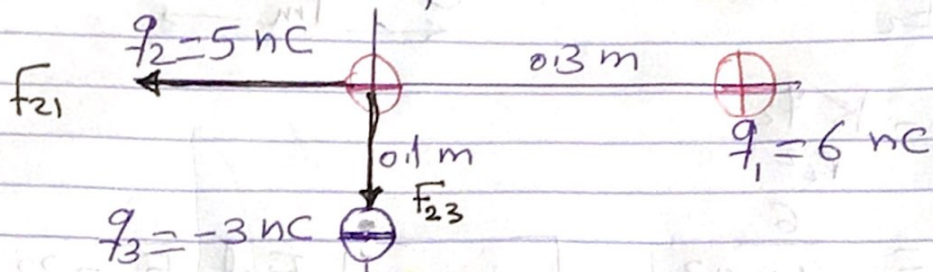


11/717 Three point charges are arranged as shown in Fig. Find the (a) the magnitude and (b) the direction of the electric force on the particle at the origin.



$$F_{21} = \frac{k q_2 q_1}{r_{21}^2} = \frac{9 \times 10^9 \times 6 \times 10^{-9} \times 5 \times 10^{-9}}{(0.3)^2}$$

$$\vec{F}_{21} = 3 \times 10^{-6} (-\hat{i})$$

$$F_{23} = \frac{9 \times 10^9 \times 5 \times 10^{-9} \times 3 \times 10^{-9}}{(0.1)^2}$$

$$= 13.5 \times 10^{-6} \text{ N } (-\hat{j})$$

$$\vec{F}_2 = \vec{F}_{21} + \vec{F}_{23}$$

$$= (-3\hat{i} - 13.5\hat{j}) \times 10^{-6} \text{ N}$$

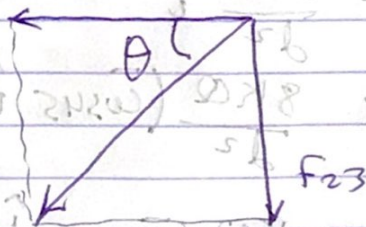
$$|F_2| = \sqrt{(3)^2 + (13.5)^2}$$

$$= 13.8 \times 10^{-6} \text{ N}$$

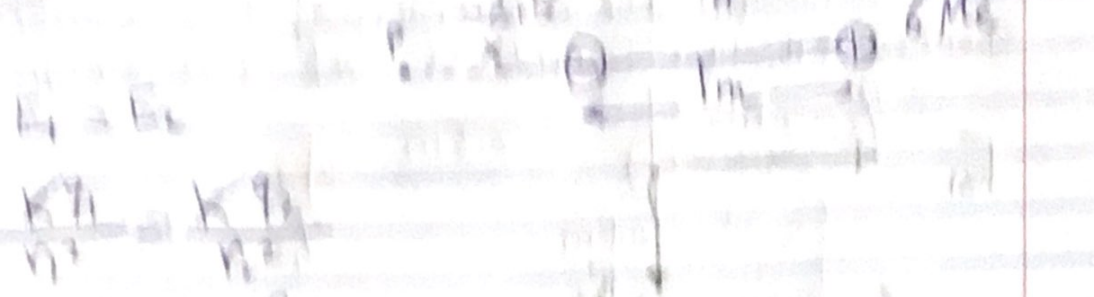
(b) direction  $\theta =$

$$\theta = \tan^{-1}\left(\frac{13.5}{3}\right)$$

$$= 77^\circ + 180 = 257.5^\circ$$



Q9 | Determine the point after than  
infinity at which the electric  
field is zero



$$\frac{kq}{r^2} = \frac{kq}{(1-x)^2}$$

$$\frac{4q}{x^2} = \frac{6q}{(1-x)^2}$$

$$\frac{2}{x^2} = \frac{3}{(1-x)^2}$$

$$\sqrt{\frac{2}{x^2}} = \sqrt{\frac{3}{(1-x)^2}}$$

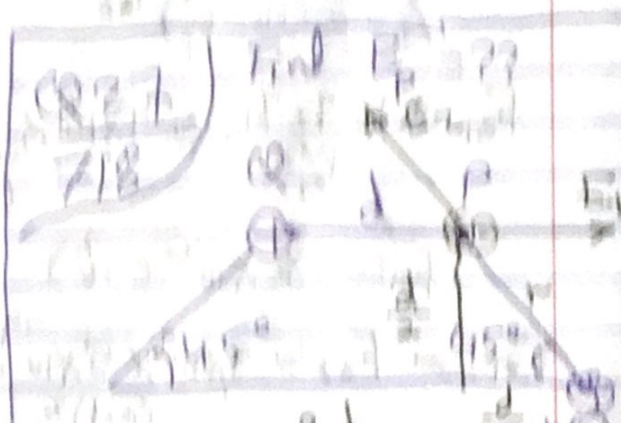
$$\frac{\sqrt{2}}{x} = \frac{\sqrt{3}}{1-x}$$

$$\sqrt{2}(1-x) = \sqrt{3}x$$

$$\sqrt{2} - \sqrt{2}x = \sqrt{3}x$$

$$\sqrt{2} = x(\sqrt{2} + \sqrt{3})$$

$$x = \frac{\sqrt{2}}{\sqrt{2} + \sqrt{3}}$$



$$E_1 = \frac{kq}{d^2}$$

$$E_2 = \frac{kq}{d^2}$$

$$= \frac{8kq}{d^2}$$

$$k = \sqrt{\left(\frac{d}{2}\right)^2 + \left(\frac{d}{2}\right)^2}$$

$$= \sqrt{\frac{d^2}{4} + \frac{d^2}{4}} = \frac{d}{2\sqrt{2}}$$

$$k^2 = \frac{d^2}{8}$$

$$\vec{E}_1 = \frac{kq}{d^2} \hat{i}$$

$$\vec{E}_2 = \frac{8kq}{d^2} (\cos 45^\circ \hat{i} + \sin 45^\circ \hat{j})$$

$$\vec{E}_3 = \frac{kq}{d^2} (\cos 45^\circ \hat{i} + \sin 45^\circ \hat{j})$$

$$\vec{E}_p = \vec{E}_1 + \vec{E}_2 + \vec{E}_3$$

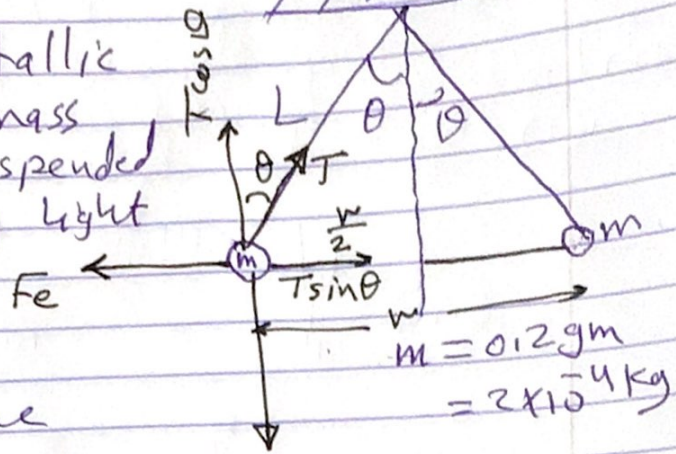
$$= \frac{kq}{d^2} (1 + 8 \cdot \frac{1}{\sqrt{2}} + \frac{1}{\sqrt{2}}) \hat{i} + \frac{kq}{d^2} (0 + 8 \cdot \frac{1}{\sqrt{2}} + \frac{1}{\sqrt{2}}) \hat{j}$$

$$= \frac{kq}{d^2} (4.66 \hat{i} + 5.66 \hat{j})$$

16/7171

Two small metallic spheres each of mass 0.2 gm are suspended as pendulums by light strings of length  $L$  as shown in Fig.

The spheres are given the same electric charge of 7.2 nC and come to equilibrium when  $\theta = 5^\circ$ .  
How long is the string,  $L = ?$



$$F_g = mg$$

$$q = 7.2 \text{ nC}$$

$$= 7.2 \times 10^{-9} \text{ C}$$

$$\theta = 5^\circ$$

$$\sum F_x = 0$$

$$F_e = T \sin \theta \quad \text{--- (1)}$$

$$\sum F_y = 0$$

$$F_g = T \cos \theta \quad \text{--- (2)}$$

$$\frac{\text{(1)}}{\text{(2)}} \rightarrow \frac{F_e}{F_g} = \frac{T \sin \theta}{T \cos \theta}$$

$$\frac{F_e}{F_g} = \tan \theta$$

$$F_e = mg \tan \theta$$

$$\frac{k q^2}{r^2} = mg \tan \theta$$

$$k q^2 = r^2 mg \tan \theta$$

$$9 \times 10^9 \times (7.2 \times 10^{-9})^2 = r^2 \times 2 \times 10^{-4} \times 10 \times \tan 5^\circ$$

$$r^2 = 2.666 \times 10^{-3}$$

$$r = 0.0516 \text{ m}$$

$$\text{but } \sin \theta = \frac{0.5 r}{L}$$

$$L = \frac{0.5 r}{\sin \theta} = \frac{0.5 (0.0516)}{\sin 5^\circ}$$

$$L = 0.3 \text{ m}$$