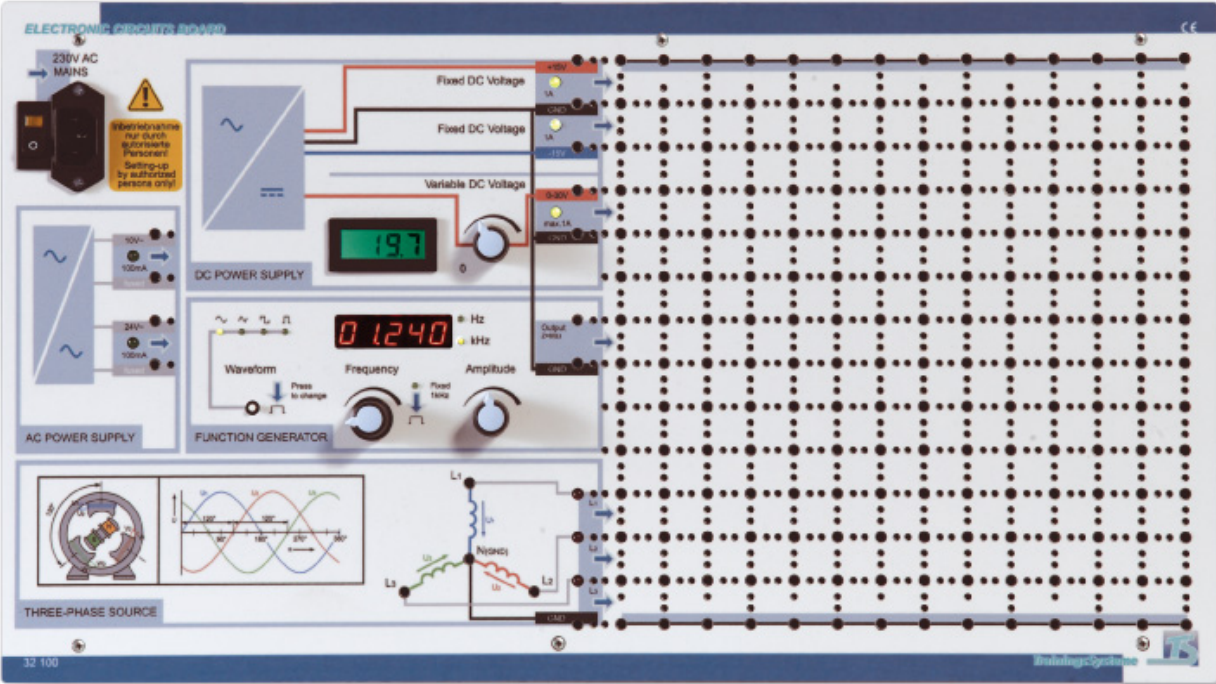


# DC and AC Technology



## Practical Experiments

Version 4.2 – Order No. E32 104

# Safety Notice



## Caution!

When assembling and testing the equipment, remember to observe all the necessary safety requirements, the laboratory regulations and all protective measures!

Do not apply any voltage until all connections have been completed and checked

Use only safety-protected test leads when assembling the exercise!

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## Practical Experiments

### 1. The Electric Circuit

#### 1.1 Components and Function of an Electric Circuit

When both poles of a voltage source are connected to the two terminals of a consumer, a current flows through the consumer. Thus, an electric circuit always contains at least three components:

- Voltage source: This contains the energy or charge, that drives the current through the circuit.
- Consumer: Depending on the type of consumer, the flow of current causes the desired effect, i.e. light, heat, sound, electromechanical movement, etc.

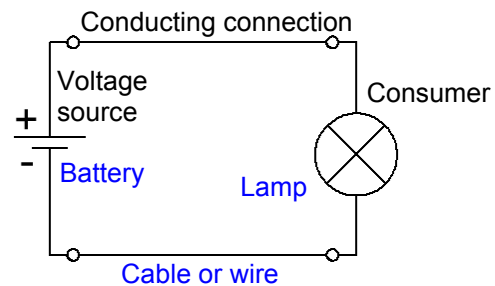


Fig. 1.1.1: The electric circuit

- Conducting connections: They have the task of allowing a flow of current between source and consumer. The connections can be in the form of wires, copper tracks on a printed circuit board or other conducting material.

A **current** is described as the movement or flow, of an electric charge through a conducting material to effect an exchange of charge. The flow of current between the poles of a voltage source, is caused by the opposing charges present at the terminals of the source. Current can only flow in a closed electric circuit.

- The **negative pole** of a voltage source has a **surplus of electrons**, this produces a **negative charge**.
- At the **plus pole** of a voltage source there is a **deficiency of electrons**. This produces a **positive charge**.

The direction of current flow is specified when describing the function of a circuit. There are two different definitions that are used:

- For **technical purposes**, the **direction of current flow** is assumed to be from the plus pole of the voltage source through the circuit connected, to the negative pole; i.e. external to the voltage source.
- The **physical direction of current flow** is from the negative pole to the plus pole of the voltage source.

**Note: If not otherwise mentioned, the technical direction of current flow will be used in this handbook.**

The reason for the flow of current, is that the charges are attempting to equalise each other. This is known as electric voltage. It can be measured, using suitable instruments connected across the poles of a voltage source. The magnitude of the voltage is a measure of the charge quantity. An electric voltage can also be measured when there is no flow of current.

## Practical Experiments

The magnitude of the current flowing in a closed circuit, depends in part, on the magnitude of the voltage applied. The current flow is also determined by the consumer, since the consumer presents an electrical **resistance** that opposes the flow of current.

### 1.2 Description of Basic Electrical Quantities

The previously defined basic electrical quantities, Current / Voltage / Resistance, have a direct relationship and can be described, mathematically:

**Current:** The magnitude of current flowing (**I**) in a circuit corresponds to the quantity of charge (**Q**), that flows per unit of time (**t**) through a conducting medium.

$$I = \frac{Q}{t}$$

Formula:

**Voltage:** The quantity of charge present in a voltage source determines its energy content (**E**) and the voltage present at the poles (**U**).

$$U = \frac{E}{Q}$$

Formula:

**Resistance:** The current is driven by the voltage and restricted or limited by the sum of all resistances (**R**) in the circuit. The formulae shown here apply:

$$I = \frac{U}{R} \Rightarrow R = \frac{U}{I}$$

Table 1.2.1 summarises the basic electrical quantities, gives the units and standard abbreviations.

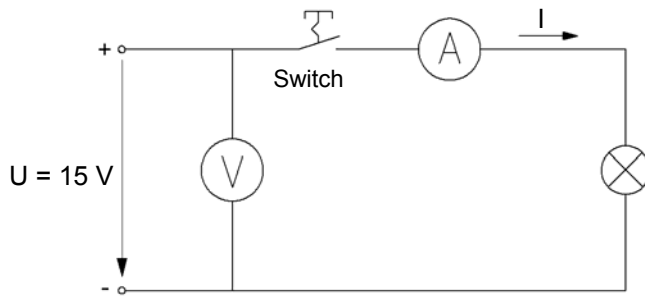
	Formula character	Basic unit	Unit character	Units commonly used
<b>Voltage</b>	U	Volt	V	mV, V, kV
<b>Current</b>	I	Ampere	A	μA, mA, A
<b>Resistance</b>	R	Ohm	Ω	Ω, kΩ, MΩ
<b>Charge</b>	Q	Coulomb	C	mC, C

Table 1.2.1: Basic electrical quantities

### 1.3 The Electric Circuit in a Practical Exercise

To examine the basic electrical quantities in a circuit, test instruments are required that indicate the magnitudes of current and voltage. A so-called 'Multimeter' can measure both electrical quantities and can be used equally, as a 'Voltmeter' or 'Amperemeter' (commonly called an ammeter). The basic circuit in 1.1.1 is extended by the test instruments. Also, for an easy and safe closing and breaking the circuit, a switch is included (Fig. 1.3.1).

## Practical Experiments



In Fig. 1.1.1 the voltage source was shown by the standard symbol for a battery. In the exercise, the DC voltage source from the Board is used. This provides a fixed voltage of 15 V or an adjustable voltage of 0 to approximately 30 V at the outputs (Fig. 1.5.2). This voltage is applied to the contacts of the circuit.

Fig. 1.3.1: Circuit with test instruments and switch

### Exercise Sequence:

**- Set the main switch on the Electronic Circuits Board to OFF!**

- Assemble the exercise on the Board. Connect the outputs of the Fixed DC Voltage source (red socket '+15V' is the plus pole, black socket 'GND', is the negative pole) to the inputs of your circuit (Fig. 1.3.1).
- Now, switch the voltage supply to the Board ON.
- Check the basic functions of the circuit, by way of the lamp.

Switch to OFF:      The lamp .....

Switch to ON:      The lamp .....

- Measure the voltage between the inputs of the circuit with the multimeter and enter the values in table 1.3.2.

Switch	Voltage, U	Current, I	Lamp
Open			
Closed			

Table 1.3.2: Measured values

- Read the value of current at each switch setting and enter the values in table 1.3.2.



## Practical Experiments

### 1.4 Tasks / Questions

- Which direction of current flow is shown in the circuit diagram in Fig. 1.3.1 and which direction in Fig. 1.4.1?

Circuit 1.3.1:

Circuit 1.4.1:

- What value is the current flow to the lamp, ' $I_{to}$ ' assumed to be in relation to the return current from the lamp ' $I_{from}$ '?

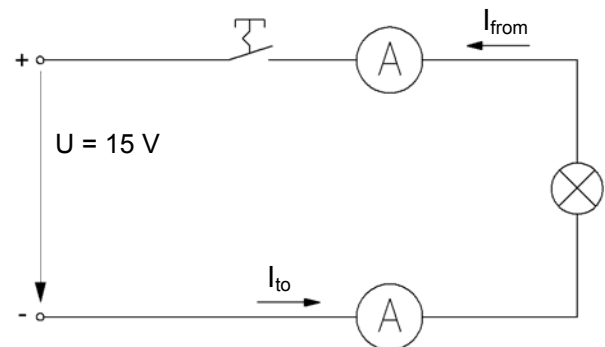


Fig. 1.4.1: Circuit for the first question

- Check your statement by measurement.

$I_{to} =$

$I_{from} =$

### 1.5 Test assembly on the Electronic Circuits Board

Construction of the circuit:

- **During construction (or any changes) of the circuit always ensure that the main switch 'MAINS' on the Electronic Circuits Board (left hand top corner on the Board) is set to OFF!**
- Note: The 2mm and 4mm sockets that are directly adjacent to each other, are connected together. Between any other neighbouring 2mm sockets there is no connection (see Fig. 1.5.1).
- First, the bridges should be inserted in the patchboard as 'conducting paths'. The positions marked 'Switch' and 'Lamp' remain free (see Fig. 1.5.2).

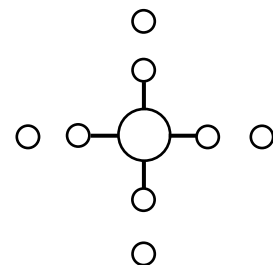


Fig. 1.5.1: Connections layout on the patchboard

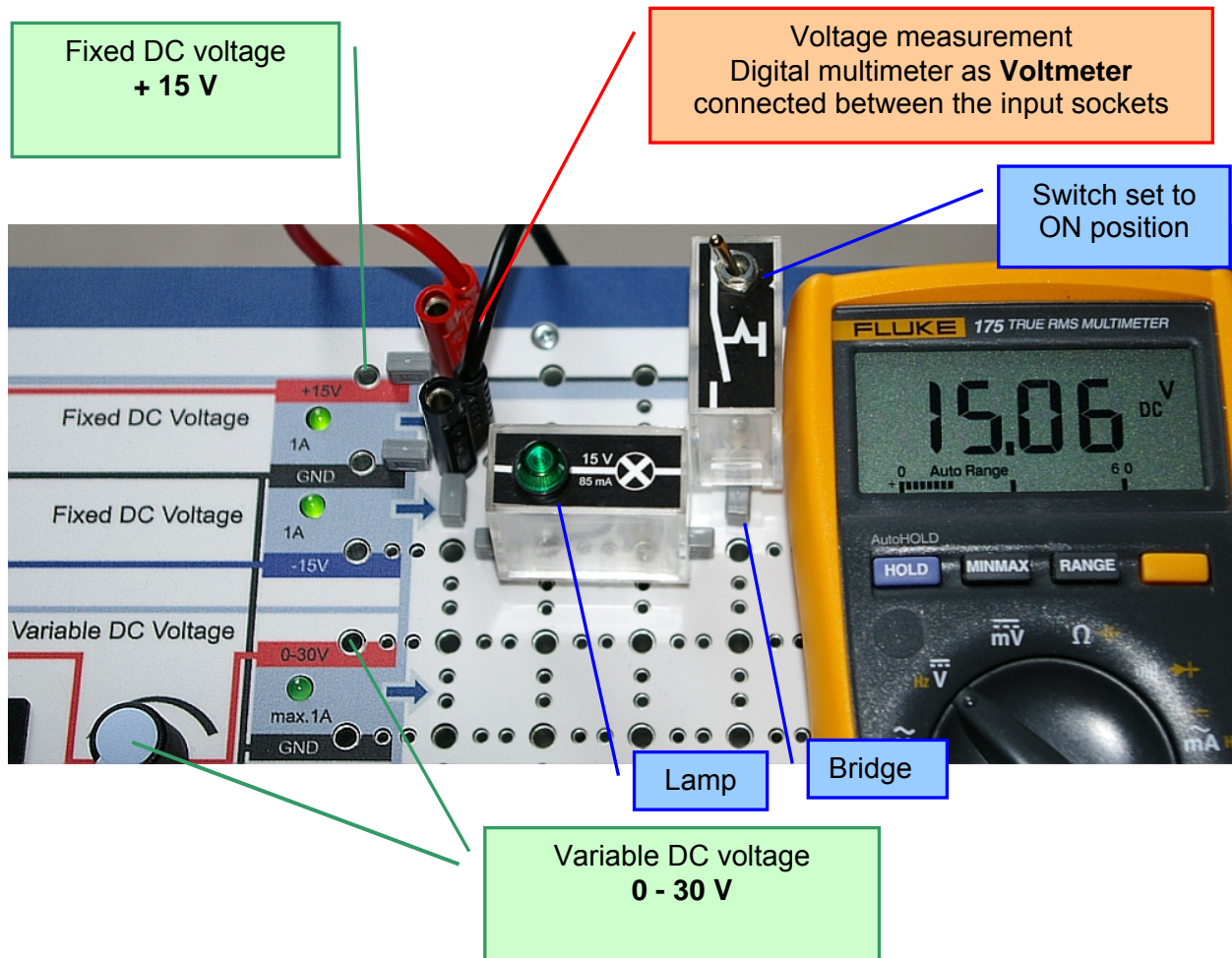


Fig. 1.5.2: Circuit construction and measurements on the Electronic Circuits Board

- Ensure that the circuit is connected to the outputs of the voltage source (plus pole: +15V / negative pole: GND) via bridging plugs (Fig. 1.5.2).
- Bridging plugs complete the circuit between the components lamp and switch (Fig. 1.5.2).

### Measurement sequence:

- A **voltmeter** is always connected **in parallel** with the test points; **ammeters** must always be connected in the circuit, **in series** with the components (Figs. 1.3.1 and 1.5.2).
- The procedure for measurements with the multimeter depends largely on the type of instrument. Fig. 1.5.2 shows a voltage measurement with a digital multimeter. The voltmeter is connected to the input sockets of the circuit, using 4mm test leads.
- To measure the current flow, a bridging plug must be removed. An ammeter is inserted in its place.

## 2. Ohm's Law

### 2.1 Importance of Ohm's Law

As in discussed in chapter 1, the current flowing in a closed circuit, is dependent only on the applied voltage and the limiting effect of the resistance of the consumer. **Ohm's law** describes in mathematical form, this statement of the relationship between the basic electrical quantities voltage (U), current (I) and resistance (R) in a circuit.

Thus,

$$I = \frac{U}{R} \Rightarrow U = R \cdot I \Rightarrow R = \frac{U}{I}$$

A missing quantity can be calculated from the formulae above, when two other values are known.

- With a constant resistance R, the current flow increases as the applied voltage is increased. In other words, the current flow is **directly proportional** to the applied voltage.
- If on the other hand, the applied voltage U remains constant and the resistance R is varied, the current flow is **indirectly proportional** to the variation in resistance.

The German physicist Georg Simon Ohm noticed these effects and made public in 1826 his now famous, law. In his honour, the unit of electrical resistance was defined as 'ohm'.

### 2.2 Ohm's Law in a Practical Exercise

The exercises are completed with a circuit where various values of resistance R, are used. The standard circuit symbol for a resistor is a rectangle (Fig. 2.2.1). For measurements, the ammeter is connected in the circuit. The voltage driving the flow of current, is measured directly across the current-limiting resistor.

**Note: The term 'resistor' is usually used to denote a component that introduces resistance into a circuit.**

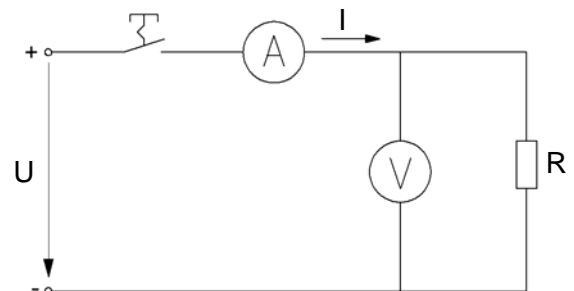


Fig. 2.2.1: Practical exercise for Ohm's law

**- Set the main switch on the Electronic Circuits Board to OFF!**

- Assemble the exercise on the Board (Fig. 2.2.1). Connect the outputs of the Variable DC Voltage source ('0 – 30 V' is the plus pole, 'GND' the negative pole) to the inputs of the circuit. As a resistance, first use the plug-in component R = 100 Ω.

## Practical Experiments

### 2.2.1 Examining the Relationship between Current and Voltage

The first measurement examines the reaction of the current to changes in the voltage. Also expressed a “current as a function of voltage”. Mathematics expression:  $I = f(U)$ .

- Set the voltage values as given in table 2.2.1.1 one after the other (check each value on the voltmeter across the resistor). At each voltage, measure the value of current flow in the circuit and enter the values in the table.

U [Volt]	0	1	2	4,5	6,5	8,5	10
I [mA], R = 100 Ω							
I [mA], R = 220 Ω							

Table 2.2.1.1:  $I = f(U)$

- Replace the resistor with one of  $R = 220 \Omega$ . Repeat the series of measurements and complete table 2.2.1.1, accordingly. After completion, set the switches on the Board and circuit to OFF!
- Plot both series of measured values in the chart below (Fig. 2.2.1.2) and join the points plotted to produce a characteristic for each resistor.

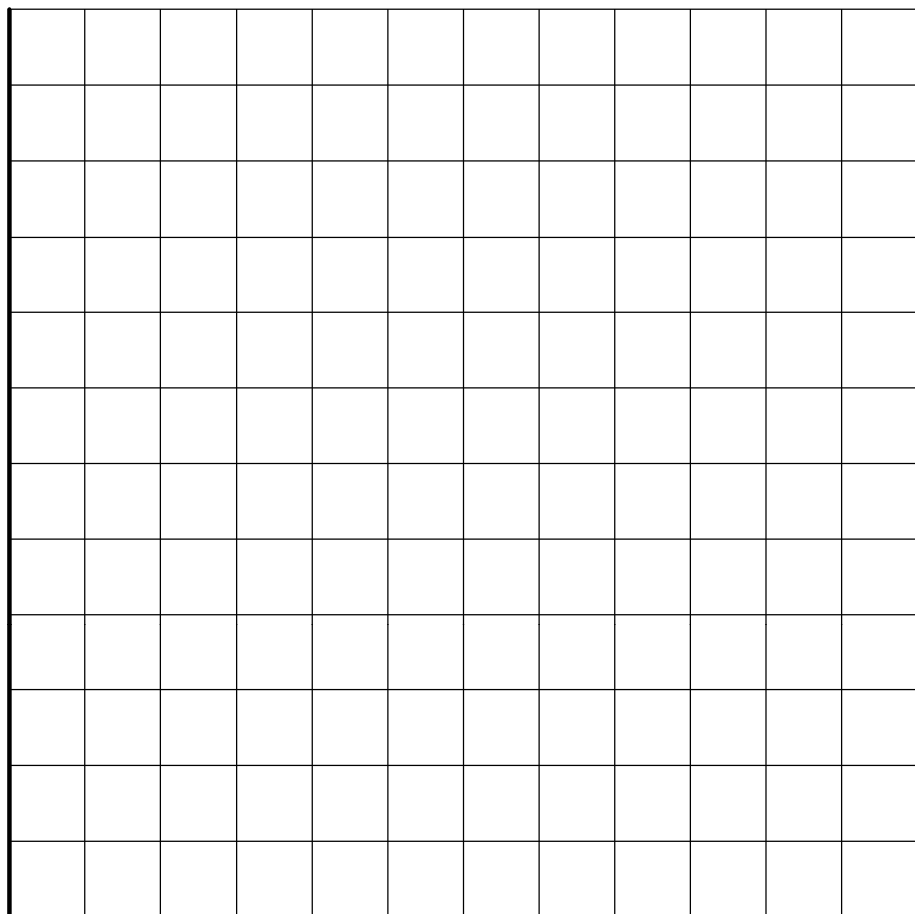


Fig. 2.2.1.2: Graph  $I = f(U)$

## Practical Experiments

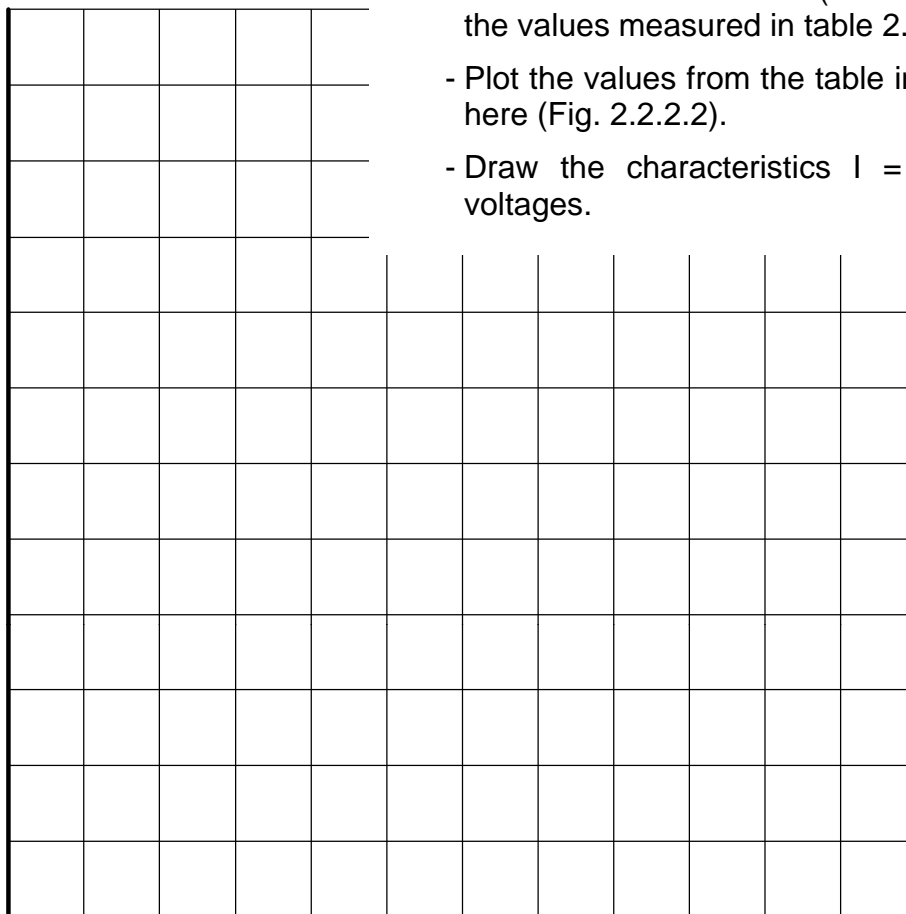
### 2.2.2 Examining the Relationship between Current and Resistance

In this exercise, the current flow is measured for different values of resistance. The voltage remains constant and is thus, “current as a function of resistance”. Mathematics expression:  $I = f(R)$ .

- Have the resistors given in table 2.2.2 ready to hand and first insert a resistor with a value of  $R = 33 \Omega$  in the measurement circuit (Fig. 2.2.1).
- Set the voltage across the resistor to 4 V. Measure the current in the circuit and enter the value in table 2.2.2.1.
- Complete the series of measurements and note the current each time, in the table.

R [ $\Omega$ ]	33	100	330	470	680	1000
I [mA], U = 4 V						
I [mA], U = 7 V	XXXX					

Table 2.2.2.1:  $I = f(R)$



- Increase the voltage to 7 V and repeat the series of measurements (**Not  $R = 33 \Omega$ !**). Enter the values measured in table 2.2.2.1.
- Plot the values from the table in the chart given here (Fig. 2.2.2.2).
- Draw the characteristics  $I = f(R)$  for both voltages.

Fig. 2.2.2.2: Diagram  $I = f(R)$

### 2.3 Tasks / Questions

- Calculate the current  $I$ , flowing through the resistor  $R$ , shown in Fig. 2.3.1, when the switch is closed.

- Check your calculation by measurement.

Measured value:

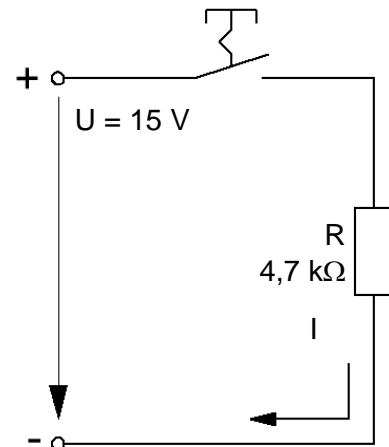


Fig. 2.3.1: Task for Ohm's law

- How does the current change when the voltage is decreased?

- The resistor is replaced by a component with a smaller resistance. The voltage remains unchanged. How does the current in the circuit react?

- The voltage across the resistor is doubled,  $R$  remains constant. What is the value of current flow now?

- The voltage  $U$  in Fig. 2.3.1 assumes the value 2,18 V. What value of resistor  $R$  must be used for the current to remain unchanged at 3,2 mA? Calculate the value of resistance and check your calculation by measurement.

Calculated:

Measurement check:

### 2.4 Exercise Assembly on the Electronic Circuits Board

Fig. 2.4.1 shows a possible test assembly for all exercises in chapter 2 “Ohm's Law”.

#### Warning:

Current flowing through a resistor produces heat. Thus for example, the components inserted in Fig. 2.4.1 have a rating limit of 2 Watt.

**Never connect a higher value of voltage to the exercise circuit than those specified!**

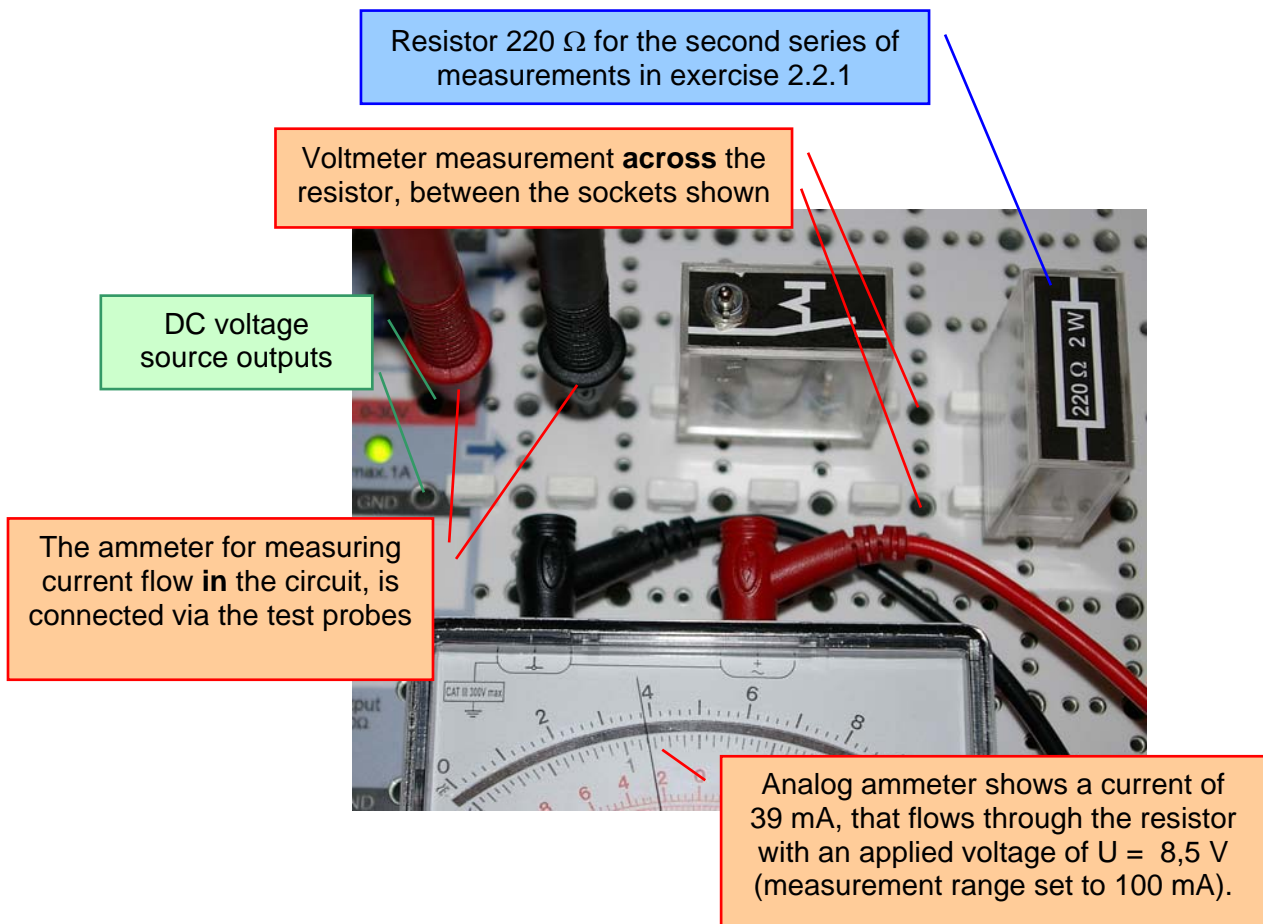


Fig. 2.4.1: Test assembly for the exercises on “Ohm's law”



## 3. Electrical Resistance

### 3.1 Types and Properties of Electrical Resistance

Electrical resistance has the property of limiting the magnitude of current flowing in a circuit. In principle, any form of resistance is a consumer that absorbs energy from the circuit and radiate this energy in the form of heat into the environment. Resistances with special functions (lamps, signal sensing elements, motors, etc.), convert the electrical energy into other physical forms of energy.

In this conversion process, a certain amount of work or power (P), is effective at the resistance that is proportional to the current flowing through the resistance and the applied voltage.

The electrical power transformed at the resistance is given by:  $P = U \cdot I$

Quite often, either the current I, or voltage U, at the resistance is unknown. By substituting the unknown quantity by the application of Ohm's law, various forms of the expression for power, P, are obtained:

Substituting current:  $P = U \cdot I$  and  $I = \frac{U}{R} \Rightarrow P = \frac{U}{R} \cdot U \Rightarrow P = \frac{U^2}{R}$

Substituting voltage:  $P = U \cdot I$  and  $U = R \cdot I \Rightarrow P = R \cdot I \cdot I \Rightarrow P = I^2 \cdot R$

Electrical power is given with the unit Watt, W.

The **rating** must be known for any resistors used in electrical circuits. The rating indicates the maximum converted **power** that can be **dissipated** at the resistor without causing any damage to the component.



The rating of the resistors used with the Electronic Circuits Board can be read on the upper face of the plastic housing. Fig. 3.1.1 shows an example.

Fig. 3.1.1: Rating of the resistors in the accessory set for the Electronic Circuits Board

Resistors are temperature-dependent components. Their **temperature response** depends on the material used in manufacturing the resistor. The resistance of the component can increase or decrease as the temperature increases. This property is applied in the selection of resistors for specific purposes, where the change in resistance caused by variations in temperature is either positive or negative.

Calculation of the change of resistance,  $\Delta R$ :  $\Delta R = R_{20} \cdot \alpha \cdot \Delta \vartheta$

- where,  $\Delta R$  : Change in resistance
- $R_{20}$  : Resistance value at 20°C
- $\alpha$  : Temperature coefficient of the material
- $\Delta \vartheta$  : Change in temperature



## Practical Experiments

Resistors are the most frequently used components in electrical circuits. Product developer use resistors for setting voltage or current conditions in various sections of a circuit. Resistance also occurs where it is not wanted. An example, is the very small resistance of wires or conducting tracks on a printed circuit board (PCB), that oppose the flow of current. For practical purposes, in electronic circuits, this form of resistance can usually be ignored. With energy or signal transmission (up to a few kilometres), such losses do play a significant role. The resistance of a line is given by the length of line  $l$ , the cross-section of the line  $A$  and a material constant  $\rho$  (Greek letter 'rho'), known as the specific resistance:

$$R_{Line} = \frac{\rho \cdot l}{A} \quad \left| \begin{array}{l} \rho \text{ } [\Omega\text{mm}^2/\text{m}] \\ l \text{ } [\text{mm}] \\ A \text{ } [\text{mm}^2] \end{array} \right.$$

A differentiation is made in the resistors manufactured for use in circuits, between **linear** and **non-linear** types of resistor. The value of linear resistors remains unchanged when the small effects of temperature are ignored. Thus, the current flow depends entirely on the applied voltage.

The value of non-linear resistors reacts to physical variables such as temperature, voltage or light. Here, depending on the applied voltage, they have a desired effect on the current flow.

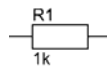
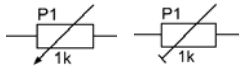
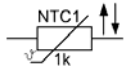
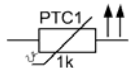
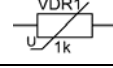

	Property	Description	Symbol
<b>Linear</b>	Fixed value	Resistor	
	Variable	Potentiometer, Trimmer	
<b>Non-linear</b>	Temperature dependent	NTC thermistor	
		PTC thermistor	
	Voltage dependent	Varistor	
	Light sensitive	Photoresistor (LDR)	

Table 3.1.2: Linear and non-linear resistors

Note: NTC = negative temperature coefficient  
 PTC = positive temperature coefficient  
 LDR = light dependent resistor

## Practical Experiments

### 3.2 Linear Resistors

#### 3.2.1 Properties of Linear Resistors

Resistors are considered to be linear when the current flowing through the resistor is dependent only on the applied voltage. The slight influence of temperature in this sense, is ignored. When the relationship between current and voltage is examined [ $I = f(U)$ ], then a straight line (linear) characteristic is produced. The current is proportional to the applied voltage (also refer to section 2.2.1).

Industrially produced resistors always exhibit a deviation between the stated and actual, values. The maximum deviation is quoted as a percentage, either as a numerical value or as a colour code on the resistor.

#### 3.2.2 Recording the Characteristic $I = f(U)$

- **Set the main switch on the Electronic Circuits Board to OFF!**

- Assemble the exercise on the Board (Fig. 3.2.2.1). Connect the outputs of the Variable DC Voltage to the inputs of your circuit. When connecting the test instruments, pay attention to the correct polarity. First, insert the plug-in resistor  $R = 1\text{ k}\Omega$ .

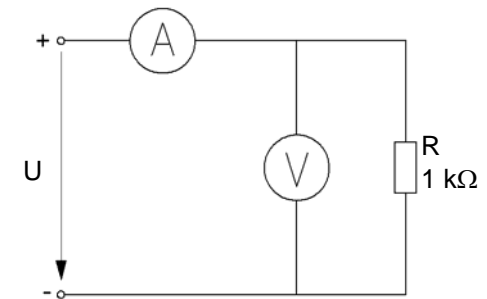


Fig. 3.2.2.1: Recording the characteristic  $I = f(U)$

- For recording the characteristic, set the voltage values as shown in table 3.2.2.2 below and at each setting, measure the current flow through the resistor. Enter the values measured in the table.

	U [Volt]	1	2	3,5	5,5	8	10
<b>R = 1 kΩ</b>	I [mA],						
	P [mW]						
	R [kΩ]						
<b>R = 4,7 kΩ</b>	I [mA],						
	P [mW]						
	R [kΩ]						

Table 3.2.2.2: Recording the characteristic  $I = f(U)$

- Plot the values measured for the first resistor in the chart (Fig. 3.2.2.3) and draw the characteristic of the resistor,  $R = 1\text{ k}\Omega$ .

## Practical Experiments

- Repeat the series of measurements with the resistor  $R = 4,7 \text{ k}\Omega$ . Complete table 3.2.2.2, accordingly.
- Plot the values measured for the second resistor in the chart (Fig. 3.2.2.3) and draw the characteristic,  $I = f(U)$ .

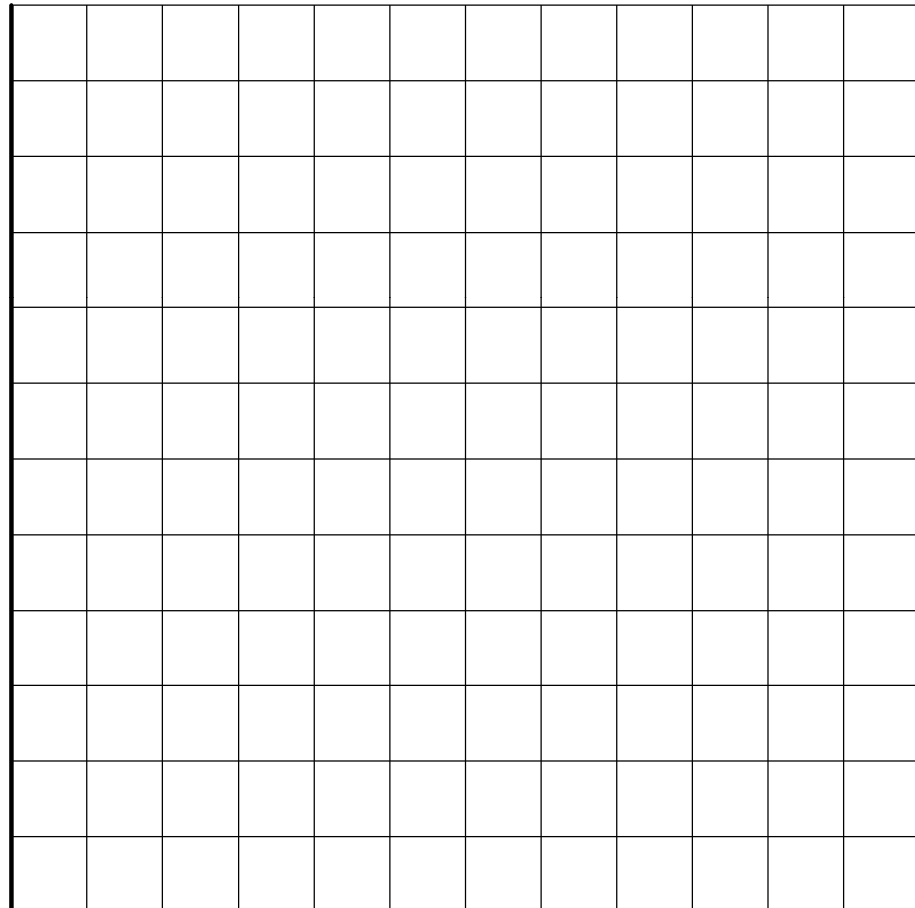


Fig. 3.2.2.3: Characteristics  $I = f(U)$

- Using your measured values, calculate the power  $P$ , converted to heat for both resistors. Enter the calculated values in table 3.2.2.2.

Formula to use:

- Select three pairs of measured values for each of the resistors  $1 \text{ k}\Omega$  and  $4,7 \text{ k}\Omega$  and calculate the actual value of resistance. Enter the calculated values in table 3.2.2.2.

Formula to use:

## Practical Experiments

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- Form the average value of the 3 calculated results.

$$R = 1 \text{ k}\Omega:$$

$$R = 4,7 \text{ k}\Omega:$$

Calculate the deviation of the actual value of resistance from the given value, as a percentage. Is the component within the stated tolerance?

$$R = 1 \text{ k}\Omega:$$

$$R = 4,7 \text{ k}\Omega:$$

- The power converted at the resistor, increases as the voltage across the resistor is increased.  
The maximum output from the voltage source used here, is approximately 30 V. Calculate for both resistors, whether they can be overloaded when a high voltage is applied.

## Practical Experiments

### 3.3 The NTC Resistor

#### 3.3.1 Properties of an NTC Resistor

NTC = Negative Temperature Coefficient

Sometimes referred to as a Thermistor (not in common use today).

Resistors with a negative temperature coefficient (NTC) are manufactured so that their resistance value reduces as the temperature is increased. They conduct better when the resistor is warm. Heating or cooling of the resistor material depends on the ambient temperature and heat produced as a result of the current flow is converted by the resistor itself, and dissipated as warmth to the surrounding air.

Due to the temperature dependence of the resistor, the characteristic  $I = f(U)$  is not linear. It follows an approximate exponential curve, depending on the resistance material.

#### 3.3.2 Recording the NTC Characteristics $I = f(U)$ and $R = f(U)$

The response of an NTC resistor will now be examined. The change in temperature required is produced by the current flowing through the resistor. Of course, the existing temperature of the room will also have an effect on the exercise. This effect is ignored when evaluating the exercise.

- Assemble the exercise circuit on the Board (Fig. 3.3.2.1).

Note: The  $220\ \Omega$  resistor is used for current limiting, a protection resistor for the NTC resistor. The effect of this resistor in the circuit can be ignored.

- For recording the characteristics, set the voltage values as shown in table 3.3.2.2, in sequence commencing with 5 V.

- After setting each voltage, wait a few minutes until the current flow has stabilised. Then, measure the current and enter the values measured in table 3.3.2.2.

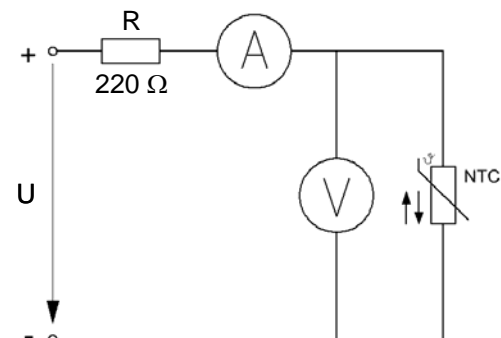


Fig. 3.3.2.1 : Characteristic recording  $I = f(U)$  and  $R = f(U)$

- **NOTE:** Depending on the temperature of the room, your results can differ slightly from those given in the table. With voltages higher than 20 V, the effect of the protection resistor is too great.

U [V]	5	10	15	17	19	20
I [mA]						
$R_{NTC}$ [k $\Omega$ ]						

Table 3.3.2.2: Characteristics,  $I = f(U)$  and  $R = f(U)$  for the NTC resistor at room temperature

## Practical Experiments

- From the values measured for U and I, calculate the values of the resistor and enter the values in the table 3.3.2.2.
- Plot the values of current measured in the chart (Fig. 3.3.2.3) and join the points to give the characteristic  $I = f(U)$ .
- Also, plot the values of U and R in the chart (Fig. 3.3.2.3). The y-axis of the coordinates system is also used as a resistance scale.
- Join the points plotted to give the characteristic  $R = f(U)$ .

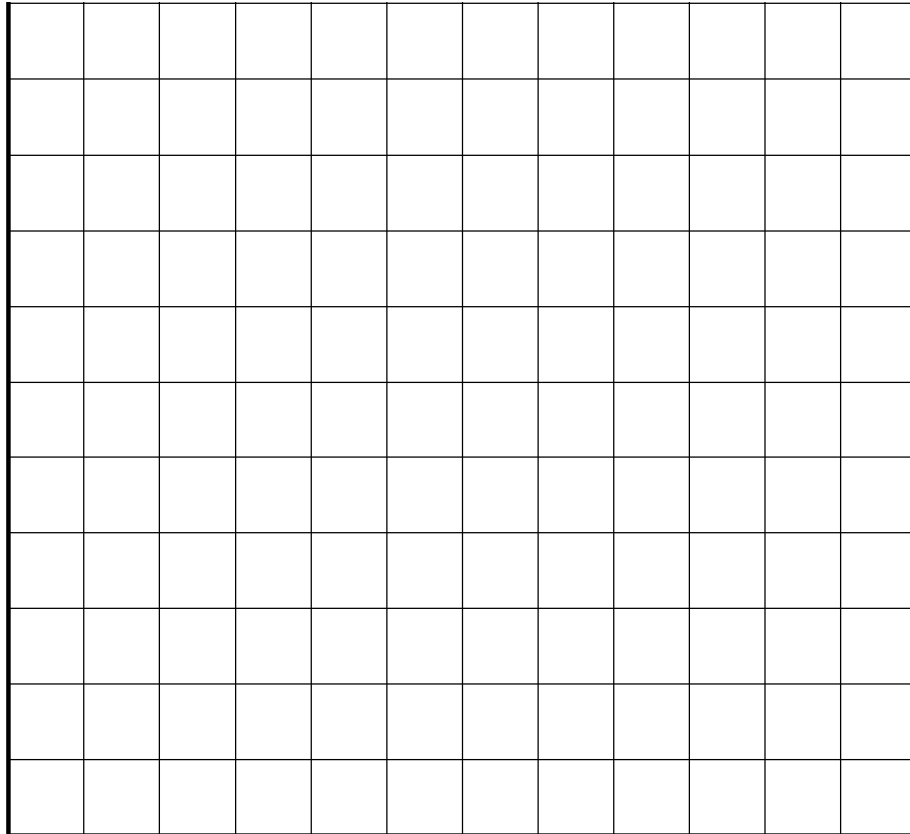


Fig. 3.3.2.3: Characteristics  $I = f(U)$  and  $R = f(U)$  for the NTC resistor at room temperature

- Break the circuit in Fig. 3.3.2.1 by removing a bridging connection. Set the voltage at the output of the source to 20 V. Select a suitable current range on your multimeter corresponding to the expected current flow.
- Now, close the circuit (insert the bridge again) whilst observing the indication on the ammeter. How does the flow of current respond at the instant of closing the circuit, and afterwards?
- Explain what is seen on the basis of the properties of an NTC resistor and reference to Ohm's law.

## Practical Experiments

### 3.4 The PTC Resistor

#### 3.4.1 Properties of a PTC Resistor

PTC = Positive Temperature Coefficient

Resistors with a positive temperature coefficient (PTC) are manufactured so that their resistance value increases as the temperature increases. They conduct better when the resistor is cold. Heating or cooling of the resistor material depends on the ambient temperature and heat produced as a result of the current flow is converted by the resistor itself, and dissipated as warmth to the surrounding air.

Due to the temperature dependence of the resistor, the characteristic  $I = f(U)$  is not linear.

#### 3.4.2 Recording the PTC Characteristics $I = f(U)$ and $R = f(U)$

The response of a PTC resistor will now be examined. The change in temperature required is produced by the current flowing through the resistor. The effect of room temperature on the exercise is ignored.

Metals have the property of increasing their resistance value when they are heated (see also section 3.1). The metallic filament in a lamp for producing light, uses this property and is thus similar to the response of a PTC resistor. For this reason, a lamp is used to replace a resistor when recording the characteristic.

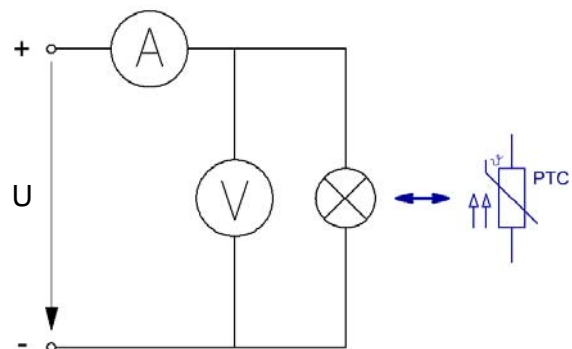


Fig. 3.4.2.1 : Characteristic recording  $I = f(U)$  and  $R = f(U)$

- Assemble the exercise circuit on the Board (Fig. 3.4.2.1).
- For recording the characteristics, set the voltage values as shown in table 3.4.2.2, in sequence commencing with 0 V. At each voltage setting, measure the current and complete table 3.4.2.2.

**NOTE:** Depending on the temperature of the room, your results can differ slightly from those given in the table.

U [V]	0	1	5	10	15	20
I [mA]						
$R_{PTC}$ [ $\Omega$ ]	ca. 50 (Room temperature)					

Table 3.4.2.2: Characteristics,  $I = f(U)$  und  $R = f(U)$  for the PTC resistor at room temperature

## Practical Experiments

- From the values measured for  $U$  and  $I$ , calculate the values of lamp resistance. Complete table 3.4.2.2.
- Draw the characteristics  $I = f(U)$  and  $R = f(U)$  in the chart (Fig. 3.4.2.3).

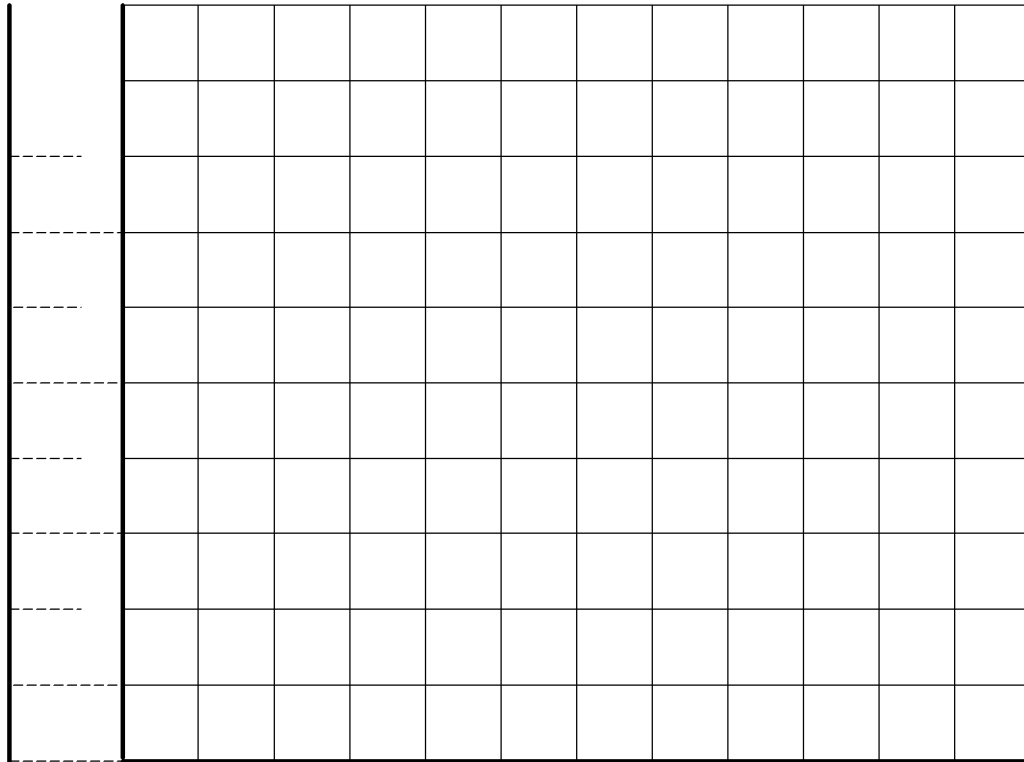


Fig. 3.4.2.3: Characteristics,  $I = f(U)$  and  $R = f(U)$  of the PTC resistor ('lamp')

- What current flows through the lamp at the instant of switching on, when the voltage across the lamp is 12 V? What conclusions can be drawn from the calculation result, with regard to the failure of filament lamps?



## Practical Experiments

### 3.5 Voltage Dependent Resistor (VDR)

#### 3.5.1 Properties of a VDR

Sometimes referred to, as a Varistor

The resistance of a voltage dependent resistor becomes smaller as the voltage across the resistor is increased. These components are often used in electronic circuits to compensate for unwanted increases in voltage. These changes in voltage can be in the form of slow changes in voltage level (e.g. for voltage stabilising). A VDR is also used for compensating fast transitions of voltage (e.g. spark suppression at contacts, over-voltage protection, etc.).

Because of its extreme dependence on voltage, the characteristic of a VDR  $I = f(U)$ , is not linear.

#### 3.5.2 Recording the VDR Characteristics $I = f(U)$ and $R = f(U)$

The response of a VDR will now be examined.

- Assemble the exercise circuit on the Board (Fig. 3.5.2.1.)

Note: The resistor  $R = 1\text{ k}\Omega$  is used for limiting the current, i.e. as protection resistor for the VDR. Its effect in the circuit is ignored.

- For recording the characteristics, set the voltage values as shown in table 3.5.2.2, in sequence commencing with 13 V.
- At each voltage setting, measure the current and complete table 3.5.2.2.

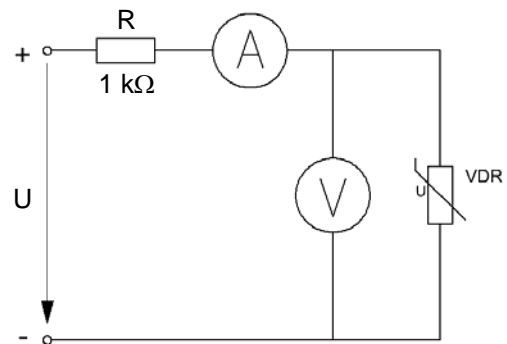


Fig. 3.5.2.1 : Characteristic recording  $I = f(U)$  and  $R = f(U)$

**NOTE: VDR's have large tolerance ratings, due to the methods of manufacture (up to 20 % of the nominal value). Thus, the values in the table are given only as guidelines and can differ from those obtained in your circuit.**

U [V]	13	16	19	20	21	22
I [mA]						
$R_{VDR}$ [kΩ]						

Table 3.5.2.2: Characteristics  $I = f(U)$  and  $R = f(U)$  at the VDR

- From the values measured for U and I, calculate the values of the resistance,  $R_{VDR}$ . Enter the calculated results in the table.
- Plot the values of current in the chart (Fig. 3.5.2.2) and draw the characteristic  $I = f(U)$  by joining the points plotted.

## Practical Experiments

- Also, plot the values for  $U$  and  $R_{VDR}$  in the chart (Fig. 3.5.2.3) and draw the characteristic  $R = f(U)$  by joining the points plotted.

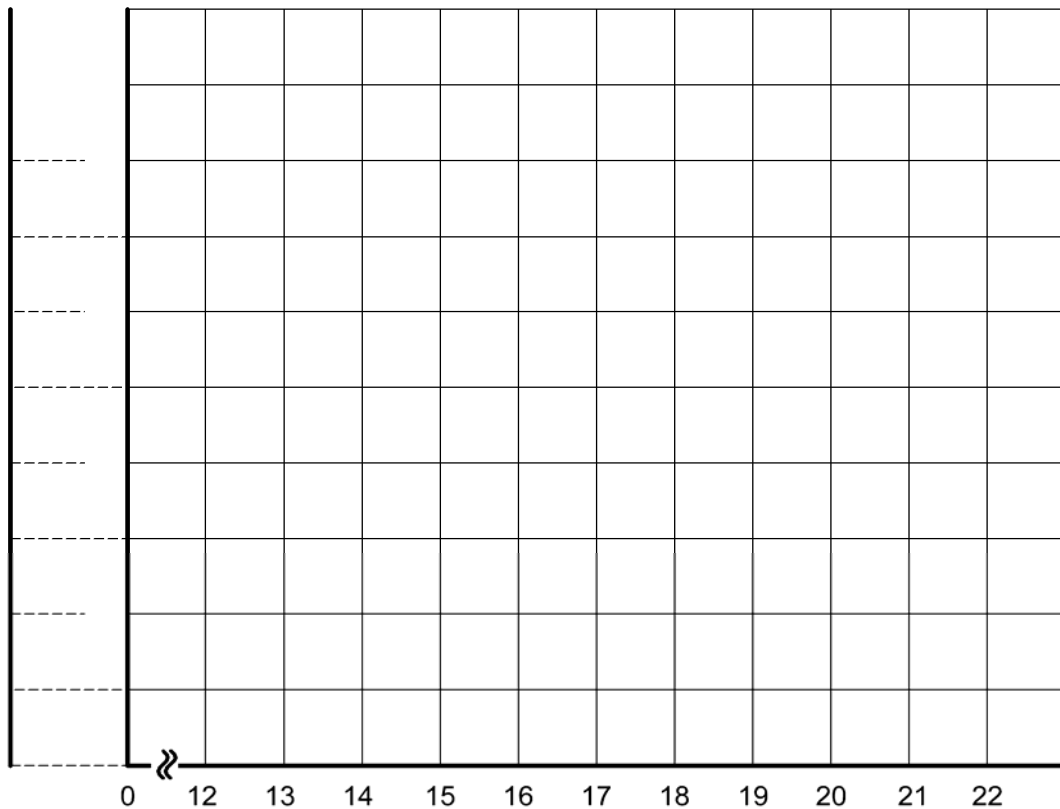


Fig. 3.5.2.3: Characteristics,  $I = f(U)$  and  $R = f(U)$  of the VDR

- By measurement and calculation, determine the power dissipation in the VDR at a voltage of 20,5 V.

<b>U [V]</b>	
<b>I [mA]</b>	

- Calculate the resistance value of the VDR at 20,5 V, using the value of power,  $P$ .

## Practical Experiments

### 3.6 Photoresistor (LDR)

#### 3.6.1 Properties of an LDR

LDR = Light Dependent Resistor

Commonly referred to, as an LDR

Photoresistors reduce in value when the intensity of incident light increases. They are used wherever a change in light intensity is to be detected and used as a signal in electronic circuits. For example, in light barriers, fire detectors, twilight switches, just to name a few.

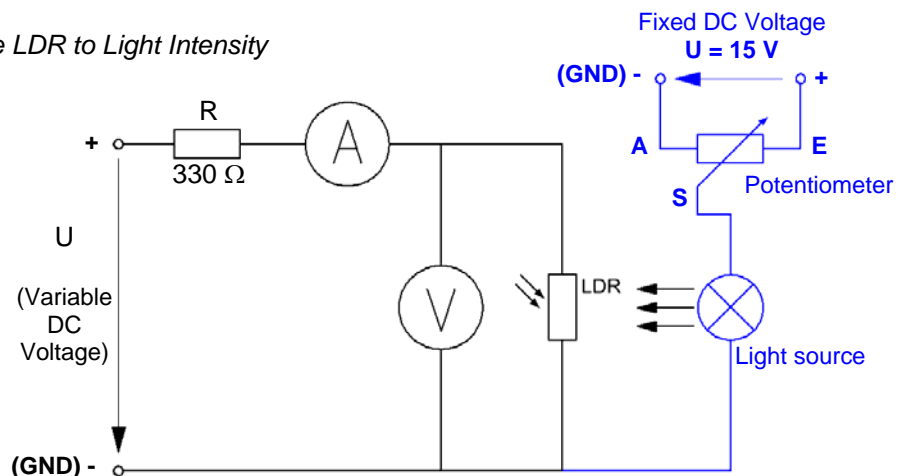
A LDR is manufactured from special semiconductor material that when completely isolated from any light, has a resistance value in excess of  $10\text{ M}\Omega$  (so-called 'dark resistance'). When the component material absorbs light energy, charge carriers are released that produce a flow of current and thus, its conductance increases. A higher level of light energy increases the number of charge carriers released and the current flow is increased. At a maximum illumination, the resistance falls to the value of 'light resistance', in the region of approximately  $100\ \Omega$ .

#### 3.6.2 Examining the Response of the LDR to the Intensity of Light

The response of an LDR will now be examined to changes in the level of light intensity.

- Assemble the exercise circuit on the Board (Fig. 3.6.2.1).

Fig. 3.6.2.1: Response of the LDR to Light Intensity



Note: The circuit drawn in blue is used to produce a variable level of light intensity. A suggested layout for the plug-in components will be found in section 3.6.3.

- Connect the input (E) and output (A) of the potentiometer to the Fixed DC Voltage,  $U = 15\text{ V}$ .

Note: All negative poles on the voltage source, labelled 'GND' on the Board, should be connected together.

- Ensure that the LDR and light source are inserted, close to each other with the light-sensitive side of the LDR facing the light source to obtain optimum illumination. Also, the light source and LDR should be inserted away from the other components, so that the LDR and light can be covered during the exercise.

## Practical Experiments

**NOTE:** The resistor  $R = 330 \Omega$  is used as a protection resistor for the LDR. For the purposes of this exercise, its effect in the circuit is ignored..

- Set the potentiometer, for varying the DC voltage, to '0' (fully CCW).
- Switch the voltage supply on for the Boards and thus the Fixed DC Voltage and check that the intensity of the light source can be smoothly varied by way of the potentiometer.
- Then, set the potentiometer fully CCW (scale value '0').
- Cover the light and LDR (dark cloth, small box, or similar), to prevent as much stray light (or daylight), from influencing the exercise results.
- To begin the exercise, adjust the voltage across the LDR to  $U = 20 \text{ V}$  (check on the multimeter). Since the LDR is dark (dark resistance  $>10 \text{ M}\Omega$ ), there should be almost zero flow of current. Check this by measurement.

The scale values on the potentiometers (0...10), are given as a guide to the strength of illumination, in table 3.6.2.2.

Scale value	0	2	3	4	6	8	10
I [mA]							
$U_{\text{LDR}}$ [U]							
R [k $\Omega$ ]							

Table 3.6.2.2: Response of the LDR to Light Intensity

- Set the potentiometer to the scale values given in table 3.6.2.2. At each setting, measure the current and voltage at the LDR and enter the values in table 3.6.2.2.
  - Calculate the resistance value of the LDR at the various levels of light intensity. Complete table 3.6.2.2 with your results of the calculations.
  - What fundamental statements can be made from the values measured and the calculated resistance, with reference to the intensity of illumination?
- 
- Can you identify an area of table 3.6.2.2, where a relatively small change in the intensity of illumination (scale value), produces a sudden change in resistance of the LDR from a high to a low value?

## Practical Experiments

### 3.6.3 Exercise Assembly on the Electronic Circuits Board

Fig. 3.6.3.1 shows a possible layout of the plug-in components required, taking into account the cover required for the light sensitive LDR together with the light source. The light source used here, is an LED (light emitting diode). This component will be explained and examined, later. The voltage supply, and the intensity of illumination (sometimes referred to as 'luminosity'), is controlled by way of a potentiometer. This component is in effect, a variable resistance, which will be explained in a later section.

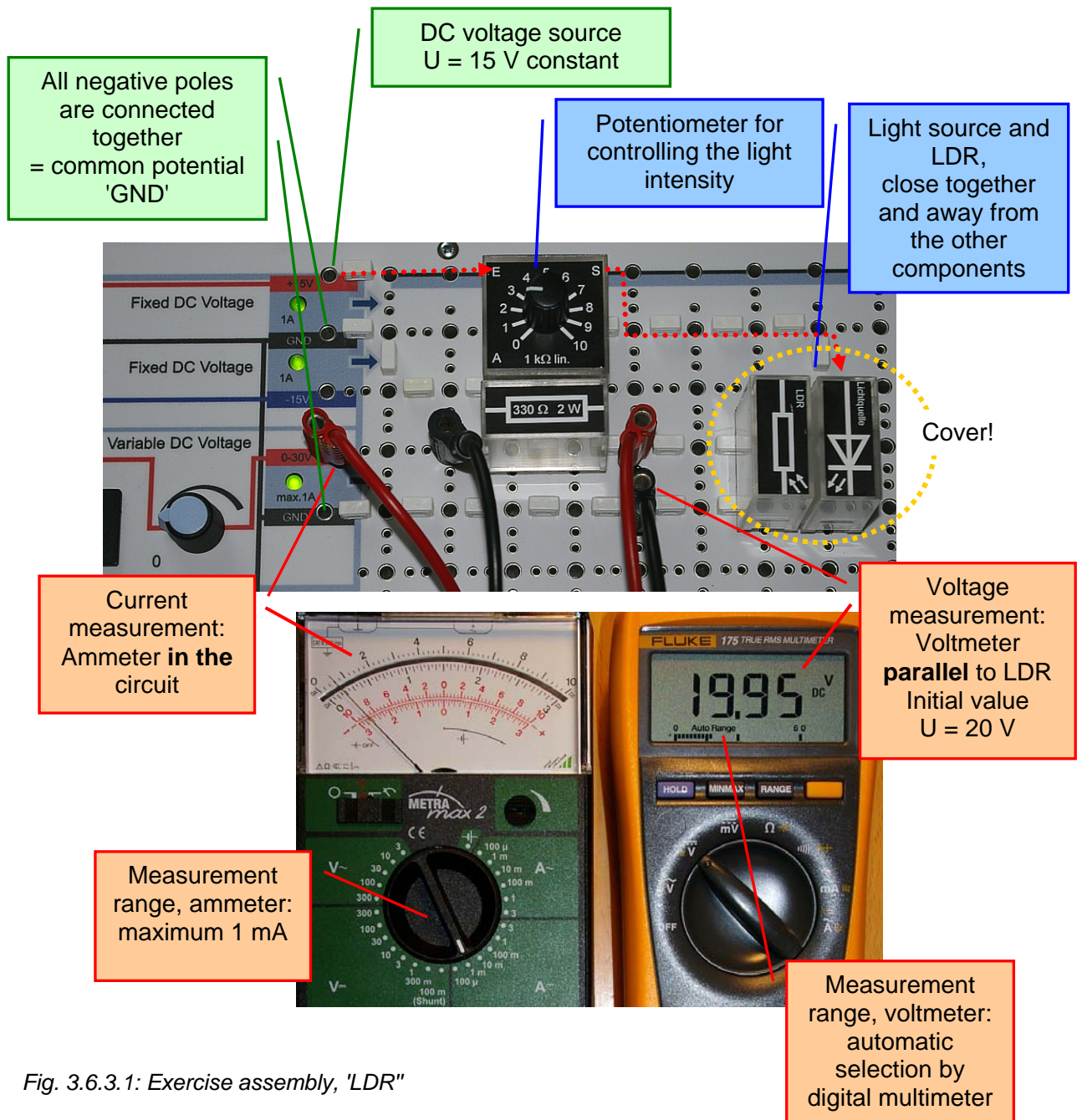


Fig. 3.6.3.1: Exercise assembly, 'LDR'

## Practical Experiments

### 3.7 Series Connection of Resistors

#### 3.7.1 Properties of a Series Circuit

If several resistors are connected in series between the plus and negative poles of a voltage source, then the **flow of current through all resistors is identical**.

Therefore,  $I_{total} = I_{R1} = I_{R2} = I_{R3} = \dots = I_n$  applies.

A voltage can always be measured across a resistor through which a current is flowing. This is known as the 'voltage drop' across the resistor. The **sum of all voltage drops** across resistors  $R_1$  to  $R_n$  in a series circuit, is equal to the **total voltage**  $U_{tot}$  present at the input to the circuit.

Formula:  $U = U_{tot} + U_{R1} + U_{R2} + U_{R3} + \dots + U_{Rn}$

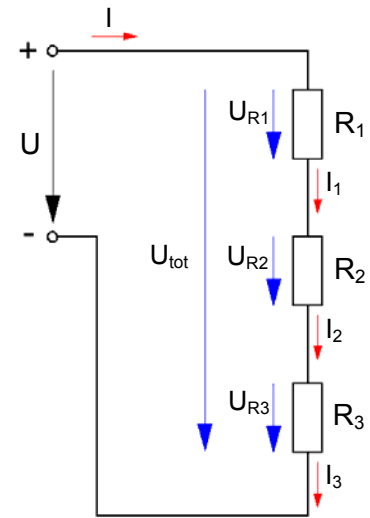


Fig. 3.7.1.1: Series circuit

An external voltage applied to a series circuit of resistors, is divided across the individual resistors. This is often referred to as a 'voltage divider', which is at the same time, an important task of resistors connected in series: 'Tap' a part of an applied voltage.

A series connection of resistors presents a total resistance in opposition to the current flow through the circuit, that can be calculated from Ohm's law:

$$R = \frac{U}{I} \quad \text{After inserting the components of voltage:} \quad R = \frac{U_1 + U_2 + U_3 + \dots + U_n}{I}$$

$$\text{Transforming:} \quad R = \frac{U_1}{I} + \frac{U_2}{I} + \frac{U_3}{I} + \dots + \frac{U_n}{I}$$

The quotient of partial voltage,  $U_n$  and total current  $I$ , corresponds to the associated resistor. Thus, the **total resistor is given by the sum of individual resistors**.

$$R = R_1 + R_2 + R_3 + \dots + R_n$$

In Fig. 3.7.1.1, consider the arrow at the voltage input to the circuit,  $U$  and the arrows of the individual voltages,  $U_n$ . It can be seen that the voltages have opposite polarity (arrow points in opposition). Therefore, it can be said that the addition of all partial voltages in a closed circuit can be considered as '0'. This relationship is known as '**Kirchhoff's second law**':

$$\sum U = 0 \quad \Leftrightarrow \quad U_{R1} + U_{R2} + U_{R3} - U_{ges} = 0$$

## Practical Experiments

### 3.7.2 Proving the Properties of a Series Circuit of Resistors

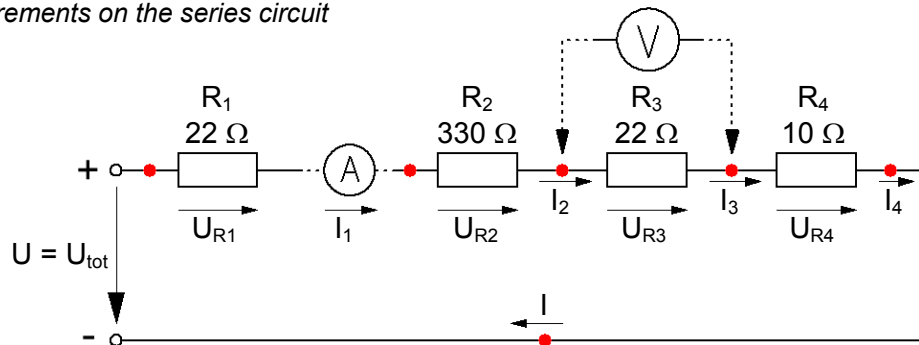
It is to be shown by measurements, that in a series connection of resistors:-

- ... the current is the same at all points in the circuit
- ... the sum of all partial voltages is equal to the total voltage
- ... the sum of individual resistors is equal to the total resistance.

- Assemble the exercise circuit on the Board (Fig. 3.7.2.1).
- Use the fixed voltage source,  $U = 15\text{ V}$  for  $U = U_{\text{tot}}$ .
- Ensure that for current measurements at the test points between the individual resistors, the circuit can be opened.

Note: In section 3.7.4, details are given on how to modify the circuit with a minimum of re-plugging.

Fig. 3.7.2.1: Measurements on the series circuit



- First, check on the voltmeter that the input voltage is 15 V. Enter the value in table 3.7.2.2.
- Now, measure the currents  $I$  and  $I_1$  to  $I_4$  and complete the table.

Current [mA]					Voltage [V]				
$I$	$I_1$	$I_2$	$I_3$	$I_4$	$U$ ( $U_{\text{tot}}$ )	$U_{R1}$	$U_{R2}$	$U_{R3}$	$U_{R4}$

Table 3.7.2.2: Measured values, Series circuit

- Measure the partial voltages across the resistors  $R_1$  to  $R_4$ . Enter the values measured in table 3.7.2.2.
- Formulate a statement with regard to the current measured in the series circuit.



## Practical Experiments

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- Evaluate the measurements of  $U_{R1}$  and  $U_{R3}$ . In your answer, use the term 'voltage drop' (where applicable).
  
- Calculate the total voltage  $U_{tot}$  from the partial voltages measured and evaluate your result.
  
- Verify the nominal values of the individual resistors, by calculation.
  
- Calculate the total resistance of the series circuit from the values of individual resistors.
  
- Calculate the total resistance of the series circuit from the input voltage and current.

### 3.7.3 Tasks / Questions

- Check whether the maximum permissible power dissipation (2 W) has been exceeded at any of the resistors used in the circuit of Fig. 3.7.2.1. Verify this, using only **one** calculation.

Result:



## Practical Experiments

- What is the total power supplied by the voltage source?
- In the circuit in Fig. 3.7.2.1,  $R_3$  is mechanically destroyed. How does this influence the current? What is the resistance value of the damaged resistor?

- In the circuit in Fig. 3.7.3.1, a protection resistor  $R_S$  is connected in series with an NTC. At  $\vartheta = 25^\circ\text{C}$  and  $U_{in} = 20\text{ V}$ , the current flow stabilises at  $I = 4\text{ mA}$ . Determine by calculation, the values of:  $R_{NTC}$ ,  $R_{tot}$ ,  $U_{NTC}$ ,  $U_{RS}$ .

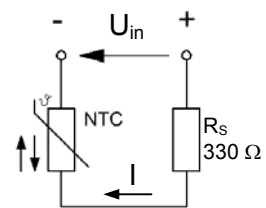


Fig. 3.7.3.1: Series circuit with NTC

- How can the NTC without protection resistor  $R_S$  be damaged? Describe the function of the protection resistor  $R_S$ .

## Practical Experiments

### 3.7.4 Exercise Assembly on the Electronic Circuits Board

Fig. 3.7.4.1 shows a space-saving possibility of assembling the voltage divider. By removing the bridges between the resistors, or between  $R_4$  and GND, the ammeter can be inserted in the circuit.

The plus pole of the constant voltage source  $U = 15\text{ V}$  is connected to the upper row of interconnected sockets. One connection of  $R_1$  is plugged into this row of sockets.

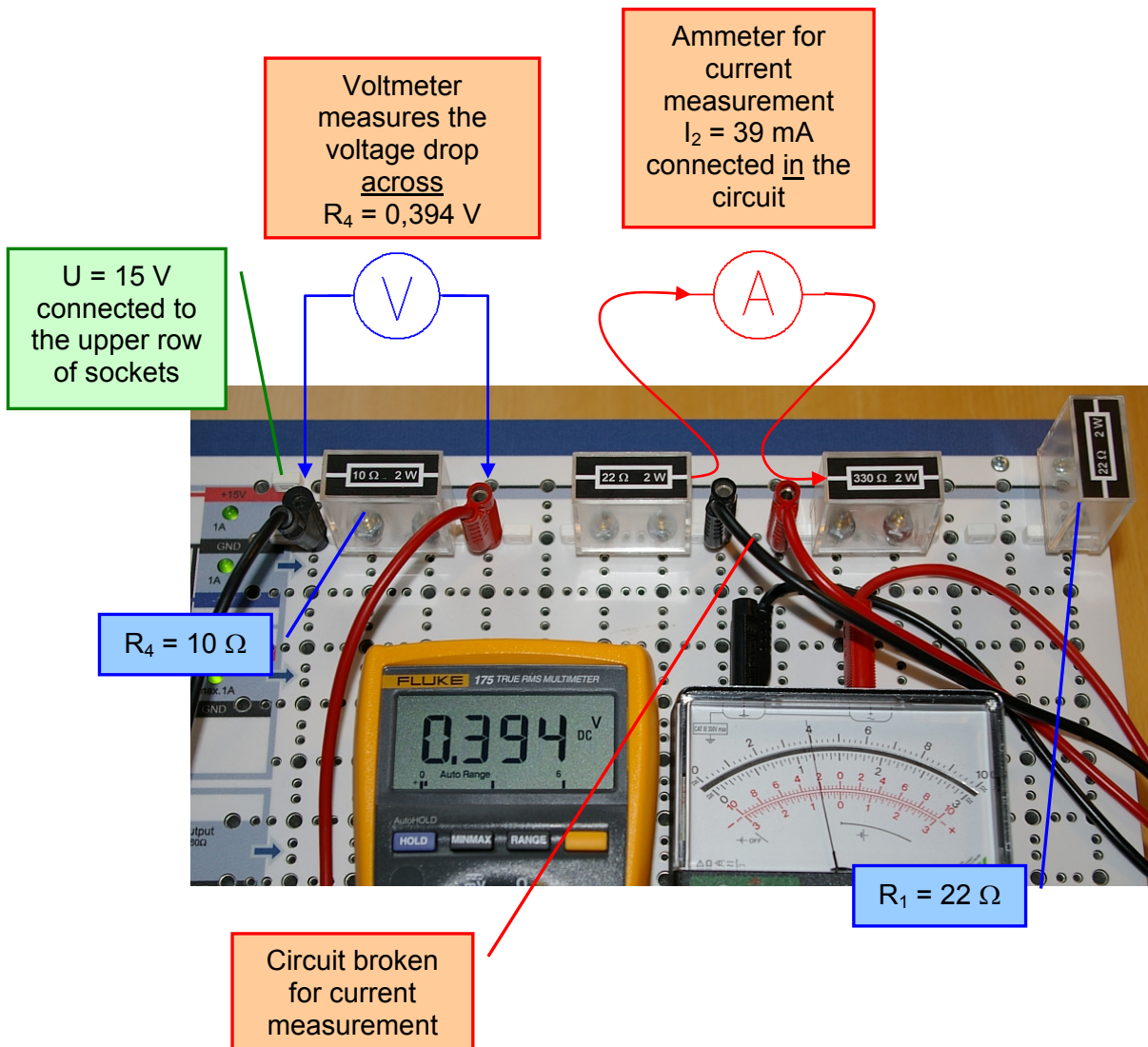


Fig. 3.7.4.1: Exercise layout, 'Series circuit of 4 resistors'

## Practical Experiments

### 3.8 Parallel Connection of Resistors

#### 3.8.1 Properties of a Parallel Circuit

The same voltage is effective across each individual resistor in a parallel circuit as in Fig. 3.8.1.1. All upper ends of the resistors are connected to plus and all lower ends, to the negative pole of the input voltage. Therefore, it applies:

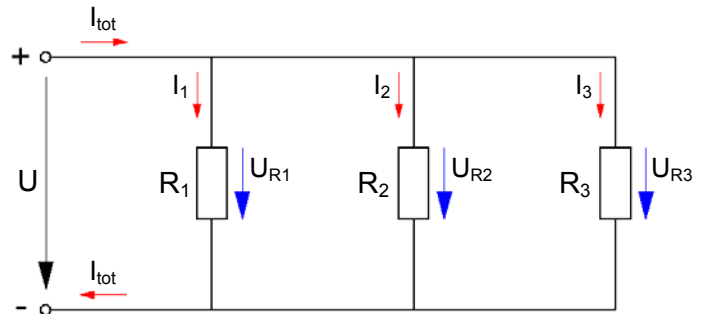


Fig. 3.8.1.1: Parallel circuit of resistors

$$U = U_{R1} = U_{R2} = U_{R3} = U_{Rn}$$

If there is a voltage difference between the ends of a resistor or consumer, a current flows through the component. In a parallel circuit, the current in each branch is given by:

$$I_1 = \frac{U}{R_1} \quad ; \quad I_2 = \frac{U}{R_2} \quad ; \quad I_3 = \frac{U}{R_3} \quad ; \quad I_n = \frac{U}{R_n}$$

The branch currents in a parallel circuit are added to give the total current flow,  $I_{tot}$ :

$$I_{tot} = I_1 + I_2 + I_3 + \dots + I_n$$

The current,  $I_{tot}$  flowing from the plus pole of the input voltage is divided through the individual resistors. Thus the term, '**voltage divider**'. If a resistor is connected in parallel to an existing resistor, the current finds an extra path for a charge carrier balance between the poles of the voltage source.

A total resistance  $R_{tot}$ , has an effect on the voltage that is smaller than the smallest individual resistor. This is given by the formula:

$$R_{tot} = \frac{1}{\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \dots + \frac{1}{R_n}}$$

The relatively complicated formula for a parallel circuit can be simplified for 2 special cases. With only 2 resistors in parallel, the formula becomes:

$$R_{tot} = \frac{R_1 \cdot R_2}{R_1 + R_2} \quad \left| \quad \begin{array}{c} R_1 \\ \hline R_2 \end{array} \right.$$

Easier still, is the calculation of the total resistance if all parallel connected resistors have the same value:

$$R_{tot} = \frac{R}{n} \quad \left| \quad n = \text{Number of equal-value resistors} \right.$$

At any point in a circuit, the sum of the currents flowing to the point,  $I_{to}$  is equal to the sum of the currents flowing away from the point,  $I_{from}$ . This statement is known as '**Kirchhoff's first law**':

Fig. 3.8.1.2 should clarify this statement and Fig. 3.8.1.1 from the current arrows at the side of the resistors.

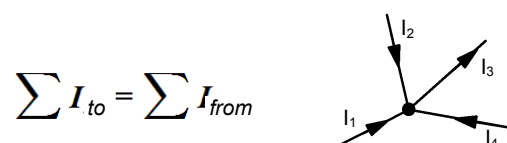


Fig. 3.8.1.2: Kirchhoff's first law

## Practical Experiments

### 3.8.2. Proving the Properties of a Parallel Circuit of Resistors

It is to be shown by measurements, that in a Parallel connection of resistors:-

- ... the voltage across all resistors is the same
- ... the total current equals the sum of all branch currents
- ... the total resistance is always smaller than the smallest individual resistor.

- Assemble the exercise circuit on the Board (Fig. 3.8.2.1).
- Use the fixed voltage source (+15 V) as input voltage  $U$  for the parallel circuit.
- Ensure that for current measurements at the test points between the individual resistors, the circuit can be opened. (A possibility of the layout of the plug-in components will be found in section 3.8.4.)

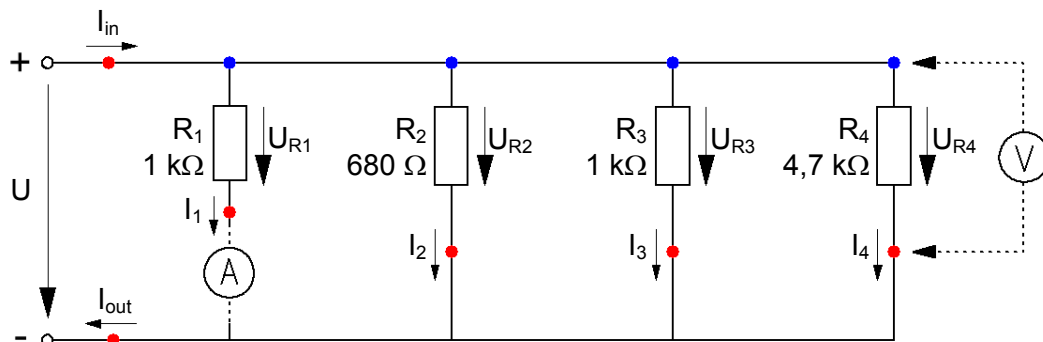


Fig. 3.8.2.1: Measurements on the parallel circuit

- First, check on the voltmeter that the input voltage is 15 V. Enter the value in table 3.8.2.2.
- Now, measure the voltage drop across the resistors ( $U_{R1}$  to  $U_{R4}$ ) and complete the table.

Current [mA]						Voltage [V]				
$I_{in}$ ( $I_{tot}$ )	$I_{out}$ ( $I_{tot}$ )	$I_1$	$I_2$	$I_3$	$I_4$	$U$	$U_{R1}$	$U_{R2}$	$U_{R3}$	$U_{R4}$

Table 3.8.2.2: Measured values, Parallel circuit

- Measure the branch currents in the resistor branches  $R_1$  to  $R_4$ . Enter the values measured in table 3.8.2.2.
- Measure the total current,  $I_{tot}$  before the resistors ( $I_{in}$ ) and after ( $I_{out}$ ). Complete table 3.8.2.2.

## Practical Experiments

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### 3.8.3 Tasks / Questions

- Explain the results of your voltage measurements  $U$  and  $U_{R_1}$  to  $U_{R_4}$  with a summarising statement.
  
- What can be said of the values measured for  $I_1$  and  $I_3$ ? Your explanation should be based on Ohm's law.
  
- Calculate the total current  $I_{\text{tot}}$  ( $= I_{\text{in}} = I_{\text{from}}$ ) from the branch currents and evaluate the result.
  
- Verify the nominal value of the individual resistors by calculation.
  
- Without calculation, what estimate can be made for the value of the total resistance in the circuit,  $R_{\text{tot}}$ ?
  
- Confirm your estimation of  $R_{\text{tot}}$  in the parallel circuit, by calculation.

## Practical Experiments

- Calculate the total resistance of the parallel circuit from the input voltage and the total current measured,  $I_{tot}$ . Compare the result with that from the calculation using nominal values.

- Check whether the maximum permissible power dissipation (2 W) has been exceeded at any of the resistors used in the circuit. Verify this, using only **one** calculation.

Result:

- What is the total power supplied by the voltage source?

- Remove resistors  $R_1 = 1\text{ k}\Omega$  and  $R_2 = 680\ \Omega$  from the circuit (or a bridge, as in Fig. 3.8.3.1).

- Calculate the total resistance for the remaining parallel circuit of  $R_3 = 1\text{ k}\Omega$  and  $R_4 = 4,7\text{ k}\Omega$ , using their nominal values.

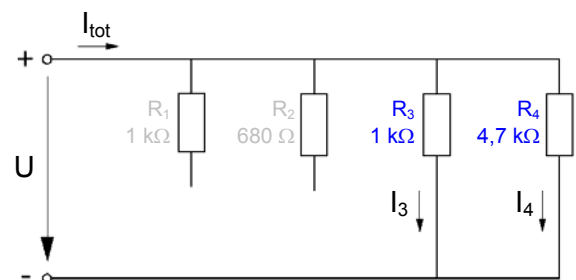


Fig. 3.8.3.1: Two resistors in parallel

## Practical Experiments

- Calculate the total resistance by Ohm's law from  $U$  and the branch currents  $I_3, I_4$ . Are new measurements for  $I_3, I_4$  necessary? Give reasons for your answer.

- How does the total resistance of the circuit change when the bridge for  $R_2$  is inserted again and at the same time, the branch with  $R_3$  opened?

- What value of resistor must be used to replace the three  $1\text{ k}\Omega$  resistors in the parallel circuit of Fig. 3.8.3.2 with a single resistor?

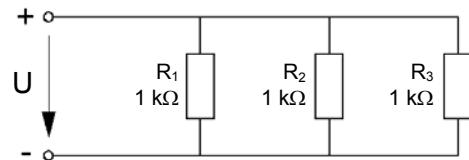


Fig. 3.8.3.2: Parallel circuit of three  $1\text{ k}\Omega$  resistors

- What is the power dissipation of the circuit in Fig. 3.8.3.2, when the input voltage applied is  $15\text{ V}$ ? For the calculation, use only voltage and resistance.

- Assemble the circuit of Fig. 3.8.3.2 on the Board. Use the fixed voltage source of  $U = 15\text{ V}$ . Measure the currents in the resistor branches  $R_1$  to  $R_3$ . Calculate the total current.

$I_1$	$I_2$	$I_3$

- Confirm your previous calculation of dissipated power (from voltage and resistance values), with a check calculation using the value of current measured.

## Practical Experiments

- At an ambient temperature of  $\vartheta = 18^\circ\text{C}$ , the parallel circuit of PTC and  $R_1$  loads the voltage source with a total resistance of  $5\text{ k}\Omega$ . What resistance value has the PTC?

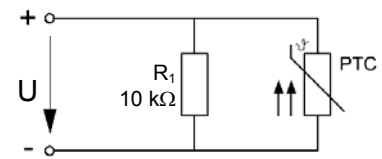


Fig.: 3.8.3.3: Parallel circuit of PTC and  $10\text{ k}\Omega$  resistor

### 3.8.4 Exercise Assembly on the Electronic Circuits Board

Fig. 3.8.4.1 shows a space-saving possibility of assembling the voltage divider. By removing the bridges below the resistors, the ammeter can be inserted in the circuit.

The plus pole of the constant voltage source  $U = 15\text{ V}$  is connected to the upper row of interconnected sockets, that supplies voltage to the upper contact of the resistors.

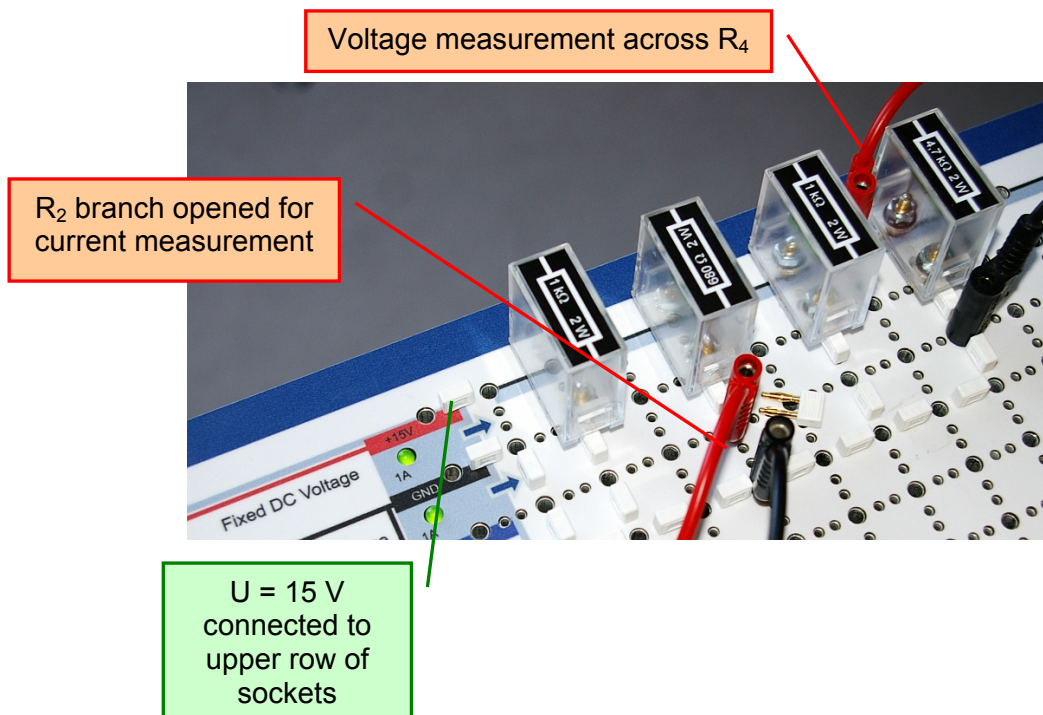


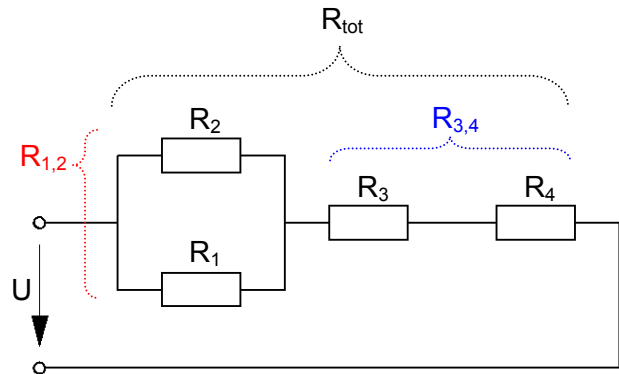
Fig. 3.8.4.1: Exercise assembly, Parallel circuit of 4 resistors



## Practical Experiments

### 3.9 Combinations of Series and Parallel Circuits

Electronic circuits often incorporate a mixture of voltage and current dividing circuits. A simple example is shown in Fig. 3.9.1.1.



#### 3.9.1 Analysis

To simplify the analysis of resistor combinations, it is usual to split the circuit into sections, where each section corresponds to a pure series or parallel connection.

Fig. 3.9.1.1: Combination of series and parallel circuits

For example, if the total resistance of the circuit in Fig. 3.9.1.1 is required first, a so-called equivalent resistance must be formed for  $R_1$  and  $R_2$  ( $R_{1,2}$ ).

$$R_{1,2} = \frac{R_1 \cdot R_2}{R_1 + R_2}$$

The next step is to calculate the resultant value of  $R_{3,4}$ :

$$R_{3,4} = R_3 + R_4$$

Finally, the total resistance  $R_{tot}$  is then given by:

$$R_{ges} = R_{1,2} + R_{3,4}$$

A similar method is also used for voltages and currents

#### 3.9.2 Practical Exercises with Mixed Resistor Circuits

A circuit analysis will be practiced on the example circuit of a combination of series and parallel connections.

##### Resistor network 1

- Assemble the circuit of Fig. 3.9.2.1 on the Electronic Circuits Board. Ensure that it will be possible to open the circuit at the locations required for current measurements (assembly notes will be found in section 3.9.4).
- Set the voltage at the input of the circuit, to  $U = 28$  V. (Check the value on the multimeter and enter the value in table 3.9.2.2).

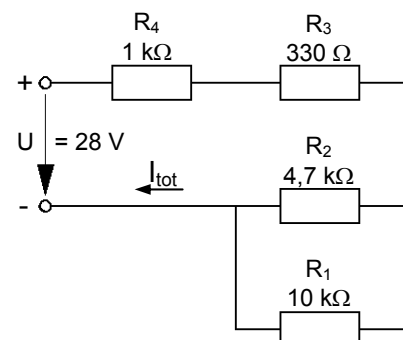


Fig. 3.9.2.1: Resistor network 1

- Measure the voltages and currents and enter the values in table 3.9.2.2.

Current [mA]			Voltage [V]				
$I_{\text{tot}}$	$I_{R1}$	$I_{R2}$	$U$	$U_{R1}$	$U_{R2}$	$U_{R3}$	$U_{R4}$

Table 3.9.2.2: Values measured in resistor network 1

- Using the rules for series and parallel circuits, calculate the total resistance  $R_{\text{tot}}$  of the circuit from the nominal values of the individual resistors.

- Check the nominal values and calculated resistor values ( $R_{\text{tot}}$ ,  $R_{1,2}$ ,  $R_{3,4}$ ) using the measured values from table 3.9.2.2. Explain any deviations.

## Practical Experiments

### Resistor network 2

- Assemble the circuit of Fig. 3.9.2.3 on the Electronic Circuits Board. Ensure that all measurement points for voltage and current, are easily accessible (assembly notes will be found in section 3.9.4).
- Set the voltage at the input of the circuit, to  $U = 18\text{ V}$ . (Check the value on the multimeter and enter the value in table 3.9.2.4).

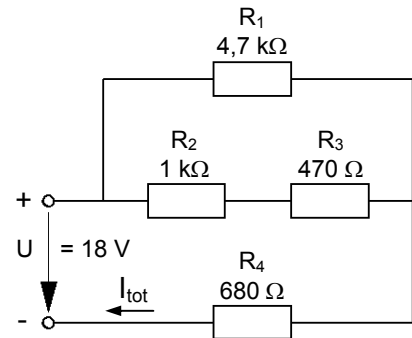


Fig. 3.9.2.3: Resistor network 2

- Measure the voltages and currents and enter the values in table 3.9.2.4.

Current [mA]			Voltage [V]				
$I_{\text{tot}}$	$I_{R1}$	$I_{R2,3}$	$U$	$U_{R1}$	$U_{R2}$	$U_{R3}$	$U_{R4}$

Table 3.9.2.4: Values measured in resistor network 2

- Calculate the total resistance  $R_{\text{tot}}$  of the circuit from the nominal values of the individual resistors.
- Check the nominal values and calculated resistor values ( $R_{\text{tot}}$ ,  $R_{2,3}$ ,  $R_{1,2,3}$ ) using the measured values from table 3.9.2.4.

### 3.9.3 Tasks / Questions

Use the nominal values of resistance for all questions.

- What are the values of total current  $I_{\text{tot}}$  and  $I_{R1}$ , when resistor  $R_3$  in the resistor network of Fig. 3.9.2.1 is damaged (high resistance)
  
- How large does  $R_{\text{tot}}$  become (Fig. 3.9.2.1), when  $R_2$  is bridged with a piece of wire?
  
- In which direction does the total current  $I_{\text{tot}}$  in the circuit of Fig. 3.9.2.3 change, when  $R_2$  becomes high-resistive?
  
- How large is the total resistance  $R_{\text{tot}}$ , when the individual resistor  $R_1$  becomes high-resistive in the circuit of Fig. 3.9.2.3?

Fig. 3.9.3.1 shows the circuit of a light barrier. When the focussed beam of light strikes the LDR, a maximum current flows in the circuit of  $I_{\text{tot}} = 37 \text{ mA}$ . If the light beam is interrupted, the resistance of the LDR increases up to the  $\text{M}\Omega$  range. The voltage across  $R_{\text{LDR}}$  produced by the change in the light intensity, is processed by an evaluation unit that has an input resistance of  $R_e = 1 \text{ k}\Omega$ .

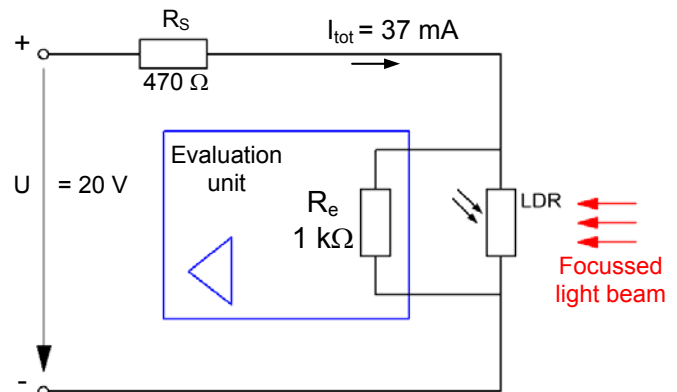


Fig. 3.9.3.1: Light barrier

- For further processing, the evaluation unit requires an explicit voltage change:  $U_{\text{light}} < 5 \text{ V}$  ;  $U_{\text{dark}} > 10 \text{ V}$ . Are these conditions satisfied for evaluating the information from the light barrier?

- To what value does  $R_{LDR,Re}$  fall, when the LDR is illuminated?

### 3.9.4 Exercise Assembly on the Electronic Circuits Board

Figs. 3.9.4.1 and 3.9.4.2 show a practical assembly layout for the circuits of mixed resistor connections. Particular attention has been paid to the accessibility of the test points required for current and voltage measurements.

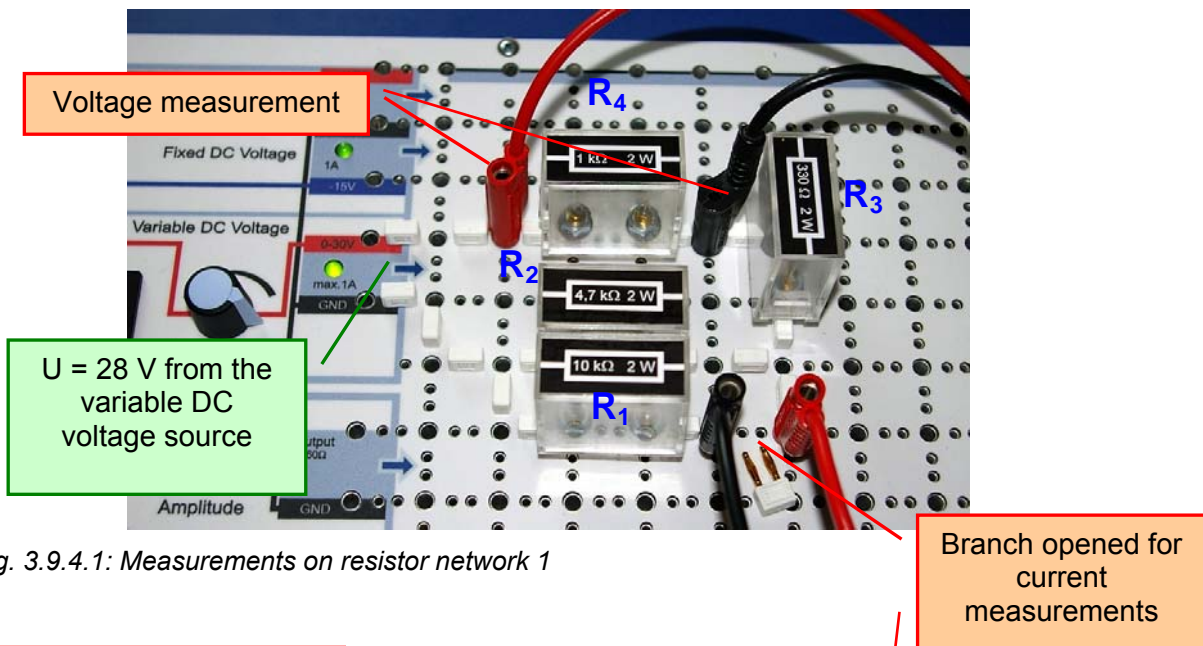


Fig. 3.9.4.1: Measurements on resistor network 1

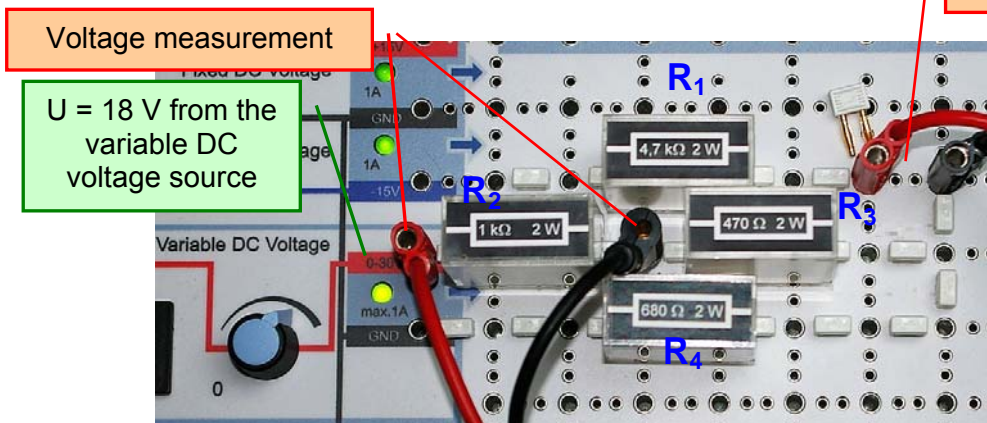


Fig. 3.9.4.2: Measurements on resistor network 2

## Practical Experiments

### 3.10 The Off-load Voltage Divider

#### 3.10.1 Properties of an Off-load Voltage Divider

In electrical engineering and electronics, it is often necessary to split a specific voltage into smaller partial voltages. A voltage divider solves this problem very easily. In its simplest form, it consists of two resistors connected in series (Fig. 3.10.1.1). Two connections form the input for the input voltage ( $U$ ). At the output side, a partial voltage ( $U_2$ ) is available across the resistor.

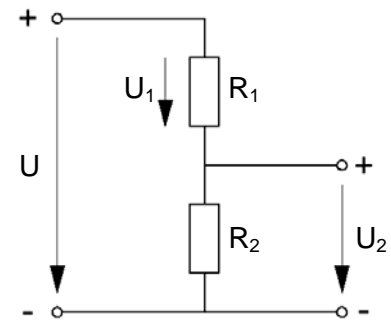


Fig. 3.10.1.1: Off-load voltage divider

Since the same current flows through both resistors, the voltage  $U$ , is divided according to their resistance values:

$$\frac{U_1}{U_2} = \frac{R_1}{R_2}$$

The relationship between the input and output voltages of the circuit can also be expressed by a proportional equation: The voltage  $U_2$ , is proportional to the total voltage  $U$ , as  $R_2$  is proportional to the sum of the resistances.

$$\frac{U_2}{U} = \frac{R_2}{R_1 + R_2} \rightarrow U_2 = U \cdot \frac{R_2}{R_1 + R_2}$$

In practice, a voltage divider is often required that has a variable output voltage. In his case, a potentiometer is used as the output resistor (Fig. 3.10.1.2). A slider in the potentiometer effectively splits the resistance material in two sections, i.e.  $R_1$  and  $R_2$ . By moving the slider, the ratio  $R_1/R_2$  can be varied and thus, the partial voltage available at the output can be adjusted.

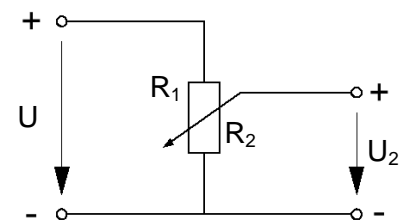


Fig. 3.10.1.2: Potentiometer

#### 3.10.2 Practical Exercises with Off-load Voltage Dividers

##### Voltage divider with fixed resistance ratio

- For the circuit in Fig. 3.10.2.1, calculate the output voltage  $U_2$  and the voltage  $U_1$ .

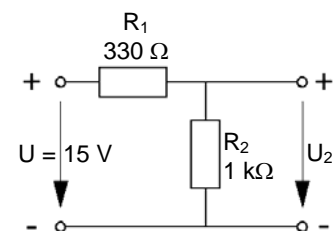


Fig. 3.10.2.1: Voltage divider

## Practical Experiments

Assemble the circuit in Fig. 3.10.2.1 on the Electronic Circuits Board. Apply a voltage of  $U = 15 \text{ V}$  to the input of the voltage divider (check the input voltage on a multimeter).

- Check the calculated voltage values for  $U_1$  and  $U_2$  by measurement.

- How do you explain the small deviations between measured values and calculated values?

### Voltage divider with variable resistance ratio (potentiometer)

- Insert the potentiometer  $P = 1 \text{ k}\Omega$ , into the circuit of Fig. 3.10.2.2 on the Electronic Circuits Board. Use an input voltage of  $U = 12 \text{ V}$  (check the set value, on a multimeter).

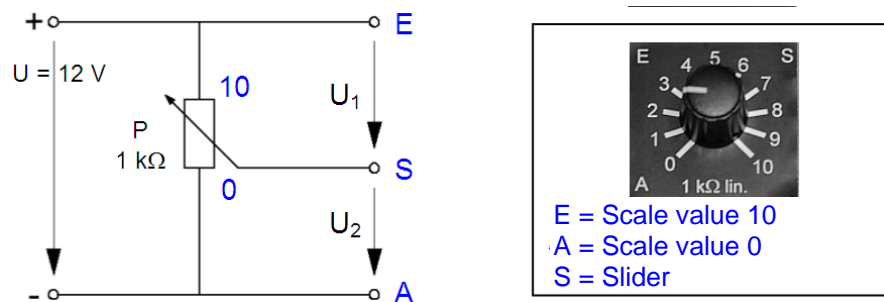


Fig. 3.10.2.2: Potentiometer

- Measure the output voltages  $U_1$  and  $U_2$  in relation to the slider setting (scale values). Enter the values measured in table 3.10.2.3.

Scale	0	1	2	3	4	5	6	7	8	9	10
$U_1$ [V]											
$U_2$ [V]											

Table 3.10.2.3: Voltage measurements at the potentiometer

From the values measured, the characteristics  $U_1 = f(\text{scale value})$  and  $U_2 = f(\text{scale value})$  will now be drawn.

- What form of curve for the characteristics is expected and why?

- Plot the values from the table in the chart (Fig. 3.10.2.4) and draw the characteristics  $U_1 = f(\text{scale value})$  and  $U_2 = f(\text{scale value})$ .

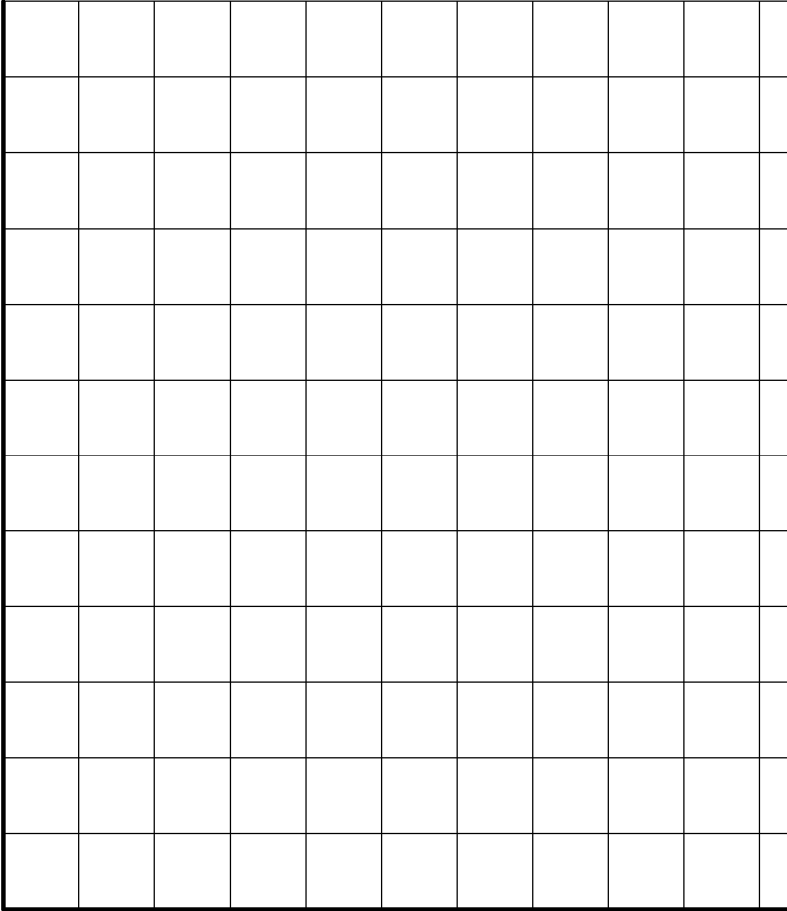


Fig. 3.10.2.4 Potentiometer characteristic

- How do you explain the slight non-linearity of the characteristics?
  
- What is the result of adding the voltage values of both characteristics at any optional setting of the slider? Explain your answer with an example for the '5' setting.
  
- Calculate the resistance of  $R_2$  at a slider setting (scale value) of '2'.



## Practical Experiments

### 3.11 The Loaded Voltage Divider

The partial voltage, output from a voltage divider, is seldom without a load. For a divider to fulfil its purpose, the output voltage  $U_A$  supplies the next circuit where the load current  $I_L$  flows (Fig. 3.11.1). The circuit here, has a load resistor  $R_L$ , that is in parallel to  $R_2$  of the voltage divider (Fig. 3.11.1).

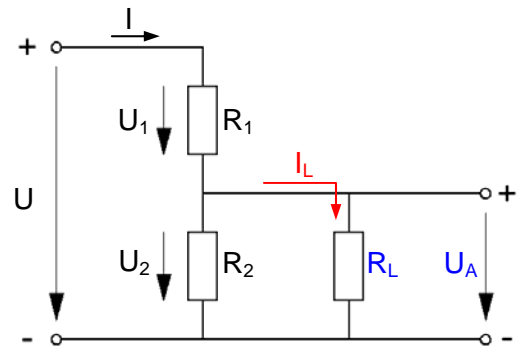


Fig. 3.11.1: Loaded voltage divider

#### 3.11.1 Properties of a Loaded Voltage Divider

A loaded voltage divider represents a combination of a series and a parallel circuit. The equivalent resistance  $R_{2,L}$  of the parallel circuit of  $R_2$  and  $R_L$  can be calculated as shown here:

$$R_{2,L} = \frac{R_2 \cdot R_L}{R_2 + R_L}$$

The output voltage  $U_A$  of a loaded voltage divider can be calculated by using the equivalent resistance  $R_{2,L}$ :

$$\frac{U_A}{U} = \frac{R_{2,L}}{R_1 + R_{2,L}} \Leftrightarrow U_A = U \cdot \frac{R_{2,L}}{R_1 + R_{2,L}}$$

Providing that the load current  $I_L$  is small compared to the current flow through  $R_2$ , the loading causes only a small reduction in the output voltage. To achieve this,  $R_2$  must be much smaller than  $R_L$  ( $R_2 \ll R_L$ ). However, an output resistor  $R_2$  with a very small resistance value causes a very high total current  $I$ , which increase the heat loss in the voltage divider. In practice, the resistors in the voltage divider are selected so that the current flow through  $R_2$  is double the value of  $I_L$ .

#### 3.11.2 Practical Exercises with Loaded Voltage Dividers

##### Loaded voltage divider with fixed resistance ratio

The voltage divider shown in Fig. 3.11.2.1 is to provide half of the input voltage  $U = 12 \text{ V}$  as an output voltage  $U_A = 6 \text{ V}$  (therefore,  $R_1 = R_2$ ). Irrespective of the loading variations due to different consumers ( $R_L$ ), the following conditions should be observed:

1. The output voltage  $U_A$  must not fall below  $5,5 \text{ V}$  with a minimum load resistor of  $R_{L \min} = 10 \text{ k}\Omega$ .
2. The maximum load current  $I_L$ , must not exceed one-fifth of the current flow through  $R_2$  even at the maximum load ( $= R_{L \min}$ ).
3. The power dissipated at the voltage divider should exceed  $100 \text{ mW}$ .

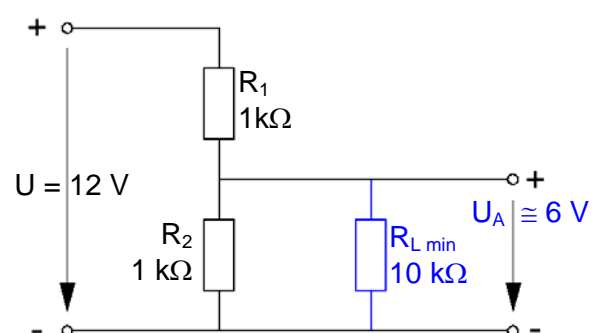


Fig. 3.11.2.1:  
Exercise with a loaded voltage divider

## Practical Experiments

- Assemble the circuit in Fig. 3.11.2.1 on the Electronic Circuits Board (Notes on assembly will be found in section 3.11.3). Apply a voltage of  $U = 12\text{ V}$  to the input of the voltage divider (check the input voltage on a multimeter).
- Check by measurement, the actual values of current and voltage to ensure that the circuit adheres to conditions 1 and 2 (calculate condition 3 on the basis of the values measured).

Table 3.11.2.2: Measurements on a loaded voltage divider

$U$	$U_A$ off-load	$U_A$ loaded ( $10\text{ k}\Omega$ )	$I_L$	$I_{R2}$

- Calculate the output voltage  $U_A$  when the voltage divider is loaded with a resistor of  $R_L = 680\ \Omega$ .

- Replace  $R_L = 10\text{ k}\Omega$  in Fig. 3.11.2.1 with  $R_L = 680\ \Omega$  and check the above calculation by measurement.

$$U_A =$$

### Loaded voltage divider with variable resistance ratio (potentiometer)

- Apply a voltage of  $U = 12\text{ V}$  to the input of the potentiometers  $P = 1\text{ k}\Omega$ , as shown in Fig. 3.11.2.3 (check the set value, on a multimeter).

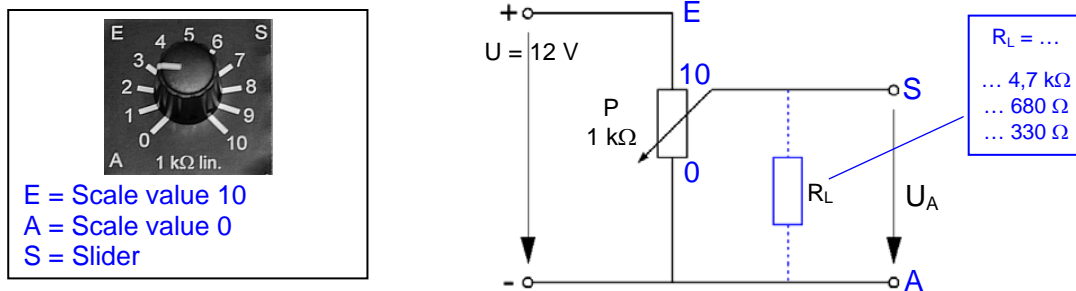


Fig. 3.11.2.3: Potentiometer with loaded output

## Practical Experiments

- The output of the potentiometer will now be loaded with 3 different values of resistance, in sequence (330  $\Omega$ , 680  $\Omega$ , 4,7 k $\Omega$ ). For each resistor, measure the output voltage  $U_A$  as a function of the slider setting (scale value). Enter the values measured into table 3.11.2.4.

Scale	0	1	2	3	4	5	6	7	8	9	10
$U_A$ [V] (330 $\Omega$ )											
$U_A$ [V] (680 $\Omega$ )											
$U_A$ [V] (4,7 k $\Omega$ )											

Table 3.11.2.4: Voltage measurements on a loaded potentiometer

- Plot the values from the table in the chart (Fig. 3.11.2.5) and draw the characteristics  $U_A = f(\text{scale value})$ .

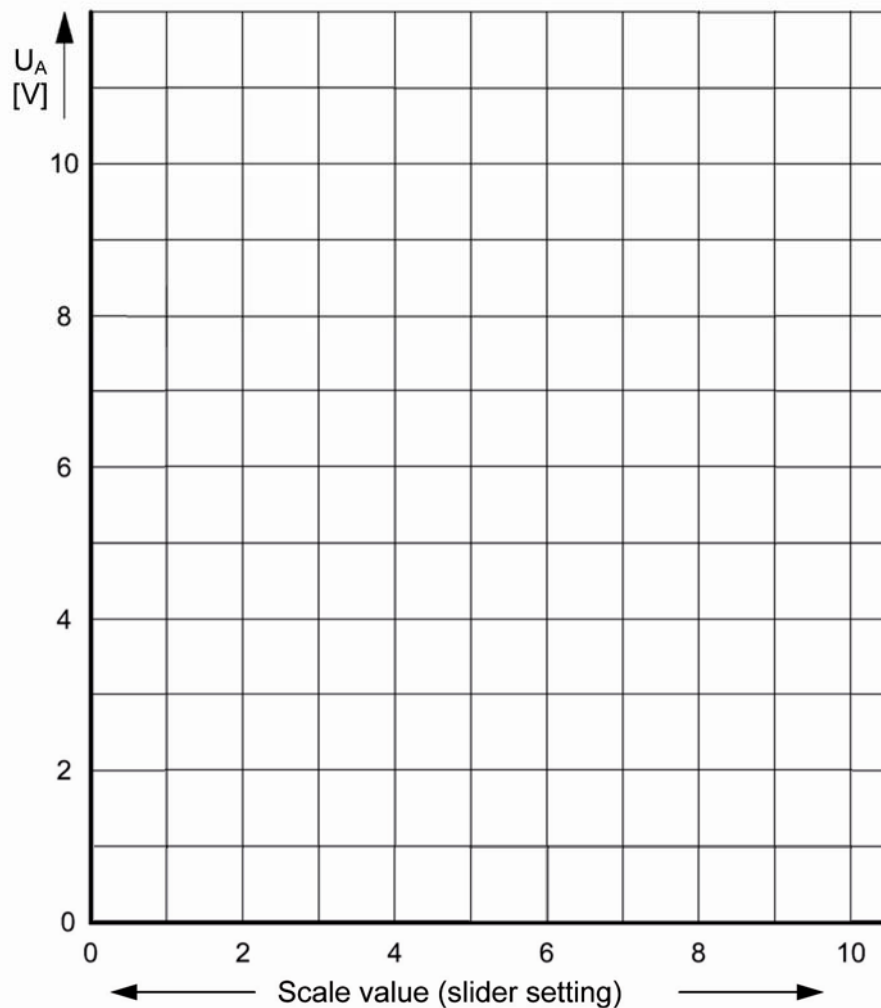


Fig. 3.11.2.5: Characteristics of the potentiometer with different loads

## Practical Experiments

- Explain why the characteristic curves are not congruent.
  
- Calculate the output voltage  $U_A$  at the mid-position of the slider and a load resistor of  $R_L = 680 \Omega$ .
  
- Compare the calculated values with the corresponding measured values in table 3.11.2.4. If the values differ, how do you explain the deviations?

### 3.11.3 Exercise Assembly on the Electronic Circuits Board

#### Loaded voltage divider with fixed resistance ratio

The layout shown in Fig. 3.11.3.1 ensures that all test points are easily accessible. All 'GND' (= earth) connections on the voltage source, should be connected together. Thus, it is possible with this layout, to connect the lower end of the voltage divider to the 'GND' connection of an external voltage source.

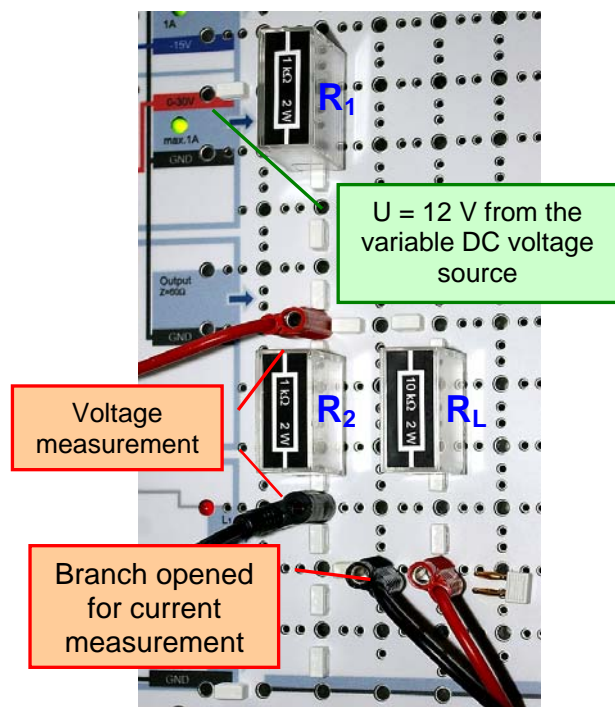


Fig. 3.11.3.1: Measurements on a loaded voltage divider with fixed resistance ratio

**Loaded** voltage divider with variable resistance ratio (potentiometer)

Fig. 3.11.3.2 shows a layout of the plug-in components for recording the characteristics of a loaded potentiometer ( $R_L = 330 \Omega$ ). The fourth, unmarked connection or pin, on the potentiometer is insulated from the housing. Thus, if required, the connections (pins) 'A' or 'S' can be connected to other components, by using this pin. In Fig. 3.11.3.2, the negative pole of the voltage source is connected via 'A' and the insulated pin 4, to the lower end of the load resistor  $R_L$ .

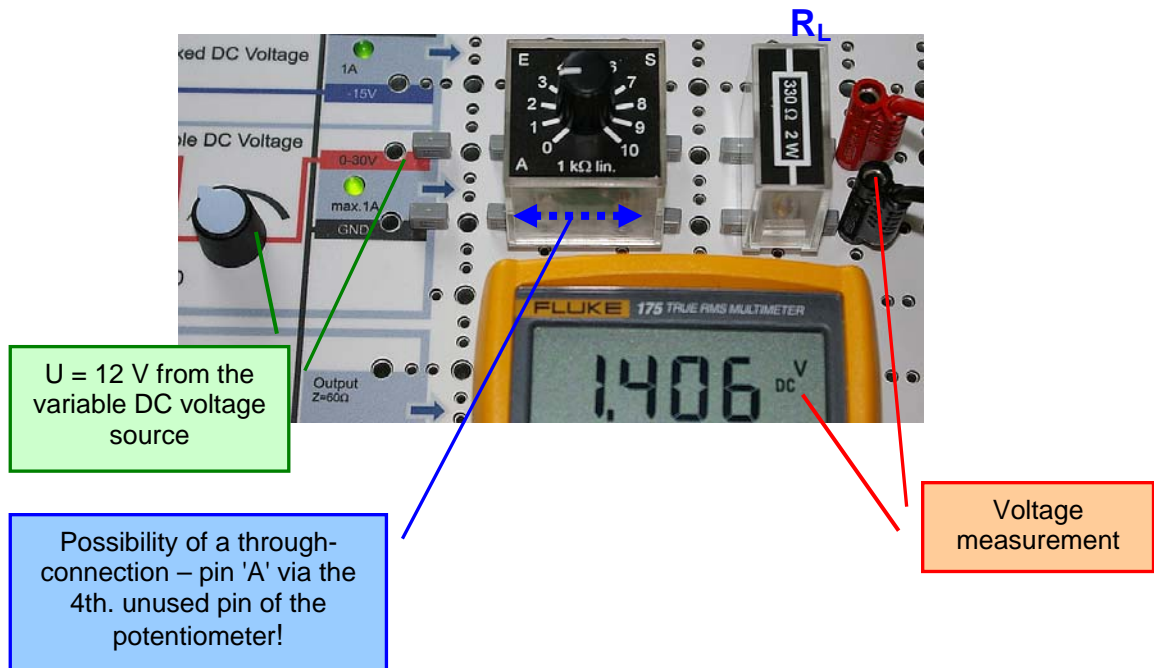


Fig. 3.11.3.2: Measurements on a loaded voltage divider with a potentiometer

## 4. Voltage and Current Error Circuits

### 4.1 Principles of Voltage and Current Measurement

For measuring the basic variables of electric voltage  $U$  (or  $V$ ) and current  $I$ , test meters must be inserted in the circuit. For measuring voltage, a voltmeter is connected in parallel to the consumer (Fig. 4.1.1, right hand side). For measuring the current, the circuit must be broken and an ammeter inserted at the break, i.e. connected in series with the consumer. This ensures that the same current flows through the meter and consumer (Fig. 4.1.1, left hand side). In practice, current measurements are avoided where possible due to the problems associated with inserting an ammeter into the circuit; sometimes, it is not even possible (for example, printed tracks on a PCB).

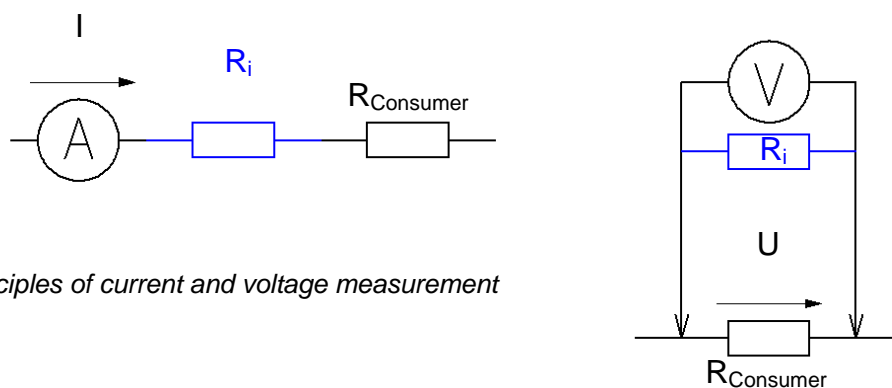


Fig. 4.1.1: Principles of current and voltage measurement

Considering only the physical relationships, both types of measurement will falsify the variables measured. Test meters have an internal resistance  $R_i$ , that influences the resistance ratio's in the circuit (Fig. 4.1.1). Since a voltmeter is connected in parallel to the consumer, its internal resistance must be as large as possible (in the order of  $M\Omega$ , depending on the measurement range selected).

The internal resistance of an ammeter on the other hand, connected in series with a consumer, must be as small as possible (a few  $\Omega$ , depending on the measurement range).

Since the ideal conditions for current ( $R_i = 0$ ) and voltage measurements ( $R_i = \infty$ ) cannot be satisfied in practice, actual values measured are always slightly wrong and usually, the measurement error introduced is small enough to be ignored. Occasionally though, an incorrect measurement can upset logic thinking in the case of fault-finding. It is also possible in isolated cases, that the introduction of a voltmeter in sensitive electronic circuits upsets their function.

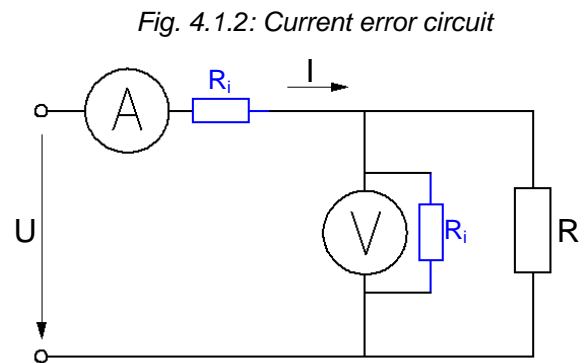
Therefore, careful considerations are essential **before** making any measurements, of the effect of test meters on the test object and the expected results of measurements.

This applies in particular when voltage and current at a consumer, are to be measured at the same time. The method of connecting both test meters depends on the resistance value of the consumer. For low-resistive consumers ( $\Omega$ ), the voltmeter and ammeter are connected as shown in Fig. 4.1.2 (current error circuit). At high-resistive consumers ( $k\Omega$  and more), the connections shown in Fig. 4.1.3 are used (voltage error circuit).

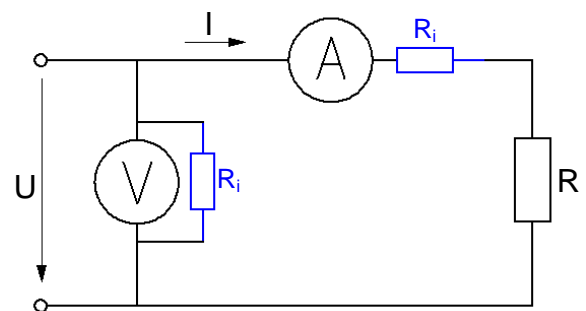
## Practical Experiments

Both variations result in a very small unavoidable measurement error.

In the **current error circuit** the ammeter also indicates the error current flowing through the internal resistance of the voltmeter. Since the resistance of the consumer is very small compared to  $R_i$  ( $R \ll R_i$ ), the current error acceptable.



When the **voltage error circuit** is used, the voltmeter measures the voltage drop across the voltage divider made up of consumer and  $R_i$  of the ammeter. Since  $R_i$  of the ammeter is only a few ohms (or less), and  $R$  is at least a few  $k\Omega$  ( $R \gg R_i$ ), the voltage error can be ignored.



### 4.2 Use of Voltage and Current Error Circuits

The improved measurement accuracy of a current error circuit with low-resistive consumers (here,  $R = 33 \Omega$ ), will be proved by measurements. This will be followed by the proof for a combination of a high-resistive consumer (here,  $R = 10 k\Omega$ ) using a voltage error circuit.

- First, with a digital multimeter, measure the exact value of resistance of the two resistors and enter the values in tables 4.2.1 and 4.2.2. Note: If an accurate test meter is not available, enter the nominal values in the tables.
- Assemble the **current** error circuit in Fig. 4.1.2 on the Board. Set the output of the voltage source to  $U = 5 \text{ V}$ .
- Measure current and voltage for both consumers (resistors) and enter the values measured in table 4.2.1.

R measured	I [mA]	U [V]	R calculated	$\Delta R$

Table 4.2.1: Values measured with a current error circuit

## Practical Experiments

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- Assemble the **voltage** error circuit in Fig. 4.1.3 on the Board. Set the output of the voltage source to  $U = 5 \text{ V}$ .
- Measure current and voltage for both consumers (resistors) and enter the values measured in table 4.2.2.

R measured	I [mA]	U [V]	R calculated	$\Delta R$

Table 4.2.2: Values measured with a voltage error circuit

- Determine the difference  $\Delta R$  between measured and calculated values of resistance. Enter the results in tables 4.2.1 and 4.2.2.
- With which error circuit can the value of the low-resistive consumer / resistance be precisely calculated because the measured values are more accurate?
  
- Which error circuit produces smaller measurement errors for the high-resistive consumer / resistance?



## 5. Equivalent Voltage Sources

Up to now, voltage sources have only been considered as an ideal case. This means that the set voltage or fixed nominal voltage remains the same, irrespective of the operating conditions. To achieve such constant voltage, some form of electronic stabilising circuit is necessary. Voltage sources without or with only slight stabilising, cannot maintain a constant voltage when a load is applied.

To avoid the necessity of examining the sometimes complex internal circuits of a voltage source and the circuit supplied by the voltage, use is often made of the so-called **equivalent voltage source** and apply the decisive properties.

### 5.1 Properties of an Equivalent Voltage Source

All voltage sources can be considered as consisting of a combination of two sections: The actual voltage generator that provides the **source voltage**  $U_0$ , and an **internal resistance**  $R_i$  (Fig. 5.1.1). Thus, the actual voltage available at the output – known as the '**terminal voltage**'  $U_K$  – is reduced by the voltage drop  $U_{Ri}$  across the internal resistance:

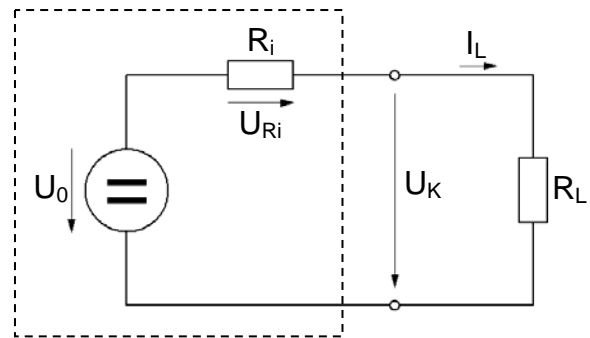


Fig. 5.1.1: Equivalent voltage source

$$U_K = U_0 - U_{Ri} \quad \text{and} \quad U_{Ri} = R_i \cdot I_L$$

$$\Rightarrow U_K = U_0 - R_i \cdot I_L$$

The voltage drop  $U_{Ri}$  across the internal resistance increases according to Ohm's law, when more current is drawn from the voltage source. This is the case when the source is loaded with a small load resistance,  $R_L$ .

The load current  $I_L$  is given by :

$$I_L = \frac{U_0}{R_i + R_L}$$

After substituting the load current equation and transformation, the terminal voltage  $U_K$  can be calculated from:

$$U_K = U_0 \cdot \frac{R_L}{R_i + R_L}$$

A differentiation is made between two limiting conditions; i.e. **off-load** ( $R_L = \infty$ ) and **short circuit** ( $R_L = 0$ ).

When **off-load** (output terminals, open-circuit), there is no flow of load current, thus there is no voltage drop across the internal resistance of the voltage source. In this case, the terminal voltage  $U_K$  corresponds to the source voltage,  $U_0$ .

$$U_K = U_0 \quad | \quad R_L = \infty$$

## Practical Experiments

With a **short circuit** at the output ( $R_L = 0$ ) the internal resistance limits the flow of current. The short circuit current  $I_K$ , is given by:

$$I_K = \frac{U_0}{R_i} \quad | \quad R_L = 0$$

**In practice, short circuit** ( $U_K = 0$ ) and **off-load** ( $I_L = 0$ ) operation have no significance. The two limiting conditions are used merely to define the end points of a characteristic for the voltage source (Fig. 5.1.2). All real applications with a loading resistance  $R_L$ , between '0' and 'infinity' also lie on the characteristic.

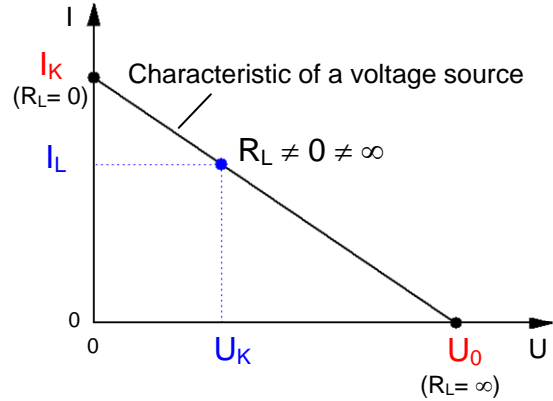


Fig. 5.1.2: Characteristic of a voltage source

### 5.2 Practical Exercises with an Equivalent Voltage Source

First, the characteristic of an equivalent voltage source will be recorded. Since the Board incorporates only stabilised voltages, an equivalent voltage source will be simulated by an external  $R_i = 33 \Omega$  (Fig. 5.2.1). The output of the variable voltage supply is set to 3 V and used as the source voltage  $U_0$ .

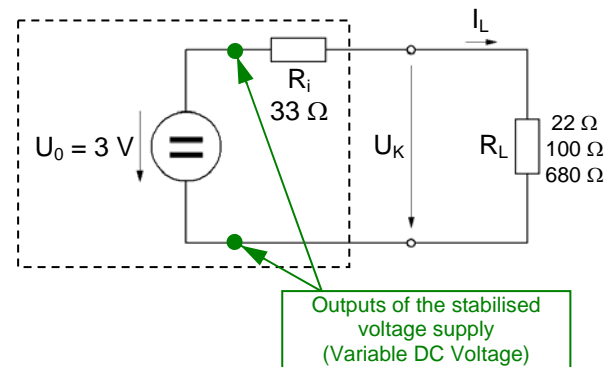


Fig. 5.2.1: Simulation of an equivalent voltage source

- Simulate the equivalent voltage source on the Board, as shown in Fig. 5.2.1.
- In off-load operation, measure the source voltage  $U_0$  and the terminal voltage  $U_K$ . Enter the values in table 5.2.2.
- For short circuit operation, measure the short-circuit current,  $I_K$  and the source voltage  $U_0$ . Consider how short circuit and current measurements can be completed with the same circuit layout. Enter the measured values in table 5.2.2.

Off-load		Short circuit		$R_L = 22 \Omega$		$R_L = 100 \Omega$		$R_L = 680 \Omega$	
$U_0$ [V]	$U_K$ [V]	$U_0$ [V]	$I_K$ [mA]	$U_K$ [V]	$I_L$ [mA]	$U_K$ [V]	$I_L$ [mA]	$U_K$ [V]	$I_L$ [mA]

Table 5.2.2: Values measured on the equivalent voltage source

## Practical Experiments

- Explain the values measured for the source voltage  $U_0$  and the terminal voltage  $U_K$  in off-load operation.
- From the measured values, draw the characteristics for off-load and short circuit conditions at the equivalent voltage source, in Fig. 5.2.3.

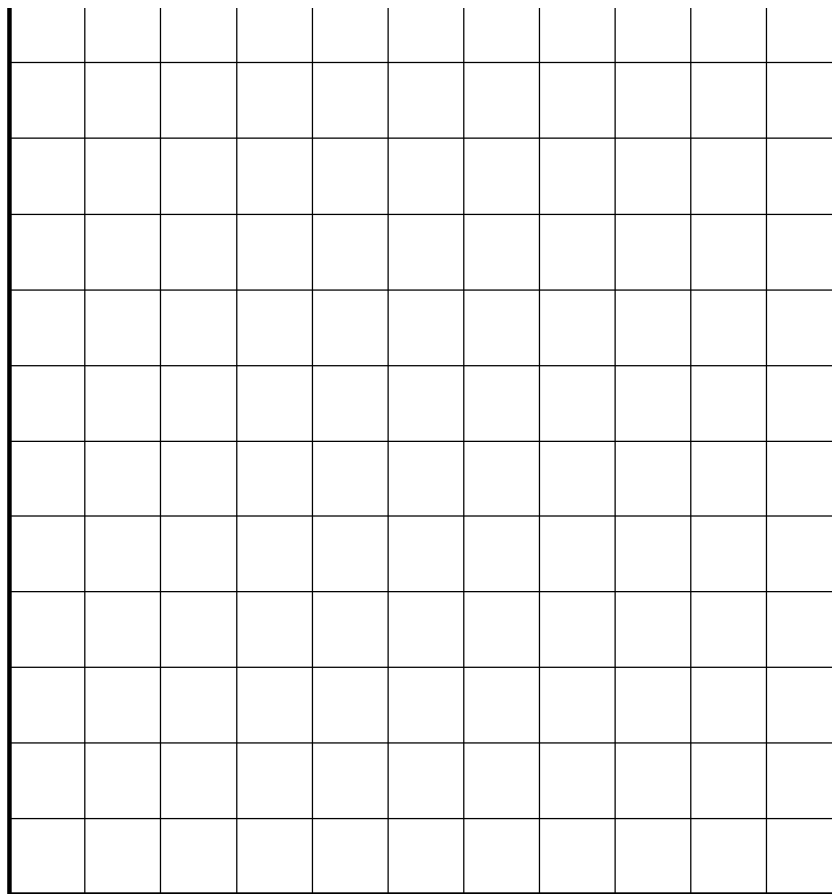


Fig. 5.2.3: Characteristic of the equivalent voltage source

- Now, measure the terminal voltage  $U_K$  and load current  $I_L$  for the 3 consumers,  $R_L = 22 / 100 / 680 \Omega$ . Enter the values measured in table 5.2.2.
- Mark the points for the 3 loading conditions on the characteristic in Fig. 5.2.3.
- Calculate the voltage drop across the internal resistance ( $U_{R_i}$ ) for a consumer of  $R_L = 22 \Omega$ .

## Practical Experiments

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- The voltage source under examination, has an internal resistance  $R_i$  of  $33 \Omega$ . What changes occur in the characteristic when an equivalent voltage source with a smaller value of  $R_i$  is examined?
  
- A real, unbalanced voltage source with an internal resistance of  $R_i = 3 \Omega$ , has a source voltage of  $U_0 = 15 \text{ V}$ . How large is the short circuit current  $I_K$  and what would probably happen if the output of the voltage source was inadvertently short circuited?
  
- Electronic circuits require a supply voltage. This voltage must not fall below a specific value, otherwise the circuit will not function correctly, or not at all. An example is the button cell in a digital wristwatch. When the cell voltage falls, the display goes off.  
Assuming that a button cell has the same values as those shown on the characteristic in Fig. 5.2.2. How would you comment on the ability of the supplied circuit to function under the following conditions?
  - a. The load resistor of the circuit,  $R_L$  is  $22 \Omega$
  - b. The button cell is loaded by  $R_L = 680 \Omega$
  
- Assuming that a circuit supplied by a button cell, tolerates the fall in voltage that occurs in case 'a.' above, without any loss of functionality. Is a button cell suitable for supplying a voltage where the resistance of the consumer is only  $22 \Omega$ ? Give reasons for your answer.

## 6. Interconnection of Voltage Sources

### 6.1 Symbols Used for Voltage Sources

DC voltage sources, the internal construction of which is of no significance, are represented by standard circuit symbols.

The symbol shown in A of Fig. 6.1.1 is used for galvanic elements, where chemical reaction is converted to electrical energy. It symbolises a **primary cell** (battery) or an **accumulator**. In contrast to primary cells, accumulators can be recharged.

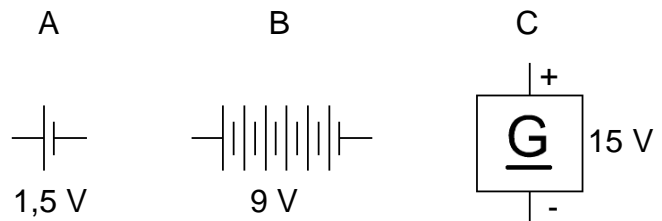


Fig. 6.1.1: Circuit symbols for voltage sources

When several primary cells are connected in series to increase the terminal voltage, the symbol shown in Fig. 6.1.1 B.

If DC voltages are generated by other forms of electrical energy, the symbol shown in Fig. 6.1.1 C is used. The 'G' stands for Generator and the line under the G indicates that a DC voltage is generated.

### 6.2 Series Connection of Voltage Sources

#### 6.2.1 Properties of Series Connected Voltage Sources

When voltage sources are connected in series, the total terminal voltage is higher. The partial voltages are added only when poles with opposite polarity are connected together. In Fig. 6.2.1.1, the negative pole of source 1 is connected to the plus pole of source 2. The two poles not connected, then form the output terminals across which the load resistance  $R_L$  is connected.

When the voltages are connected correctly in series:

$$U_{tot} = U_1 + U_2 + U_3 + \dots + U_n$$

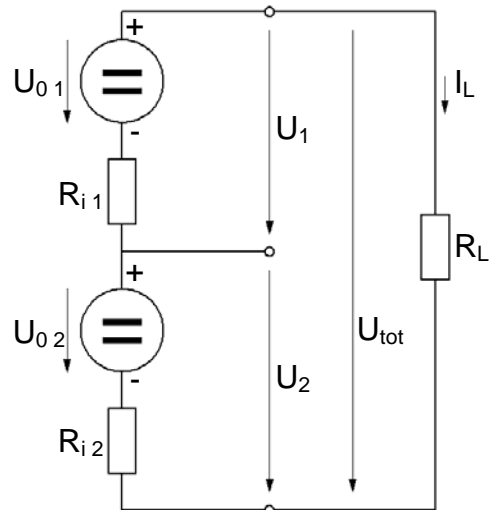


Fig. 6.2.1.1: Series connection of voltage sources

When voltage sources connected in series are operated off-load, then the total voltage  $U_{tot}$  is given by the sum of all individual source voltages,  $U_{0n}$ :

$$U_{tot} = U_{0,tot} = U_{01} + U_{02} + U_{03} + \dots + U_{0n}$$

## Practical Experiments

As to be expected in a series circuit, the internal resistances  $R_i$  add to give the total internal resistance,  $R_{i\ tot}$ :

$$R_{i\ tot} = R_{i1} + R_{i2} + R_{i3} + \dots + R_{in}$$

When a consumer is connected, the load current  $I_L$  is limited by its resistance  $R_L$  and the sum of all internal resistors,  $R_{i\ tot}$  :

$$I_L = \frac{U_{tot}}{R_L + R_{i\ tot}} = \frac{U_1 + U_2 + U_3 + \dots + U_n}{R_L + R_{i1} + R_{i2} + R_{i3} + \dots + R_{in}}$$

### 6.2.2 Series Connection of Voltage Sources as an Exercise

One of the poles of the DC voltage sources on the Electronic Circuits Board connected together. This forms the reference point known as Ground, 'GND' (or 'earth'). In Fig. 6.2.2.1 the reference point GND, is shown between the DC voltage generators by its standard circuit symbol.

The negative pole of **Source 1 (red)** and the plus pole of **Source 2 (blue)** are connected to GND. This then gives a series circuit of both voltages when a load is connected across the 'free' poles (Fig. 6.2.2). individual voltages ( $U_1$ ,  $U_2$ ) add to produce the total voltage  $U_{tot} = 30\ V$  which causes the load current  $I_L$  to flow in the consumer ( $R_L = 4,7\ k\Omega$ ).

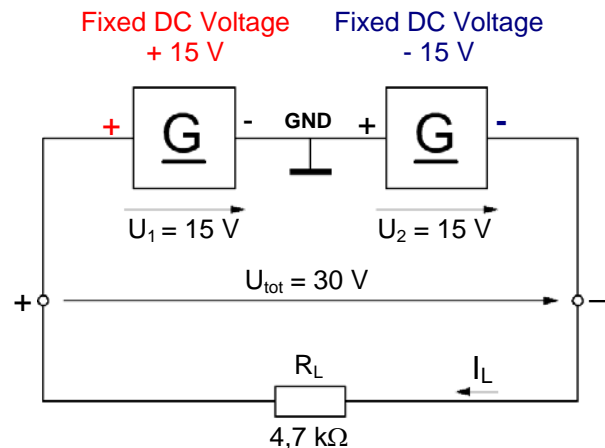


Fig. 6.2.2.1: Series circuit of 2 voltage sources

- Connect the two Fixed DC Voltage together as shown in Fig. 6.2.2. Connect a load resistor of  $R_L = 4,7\ k\Omega$  at the output ( $U_{tot} = 30\ V$ ) The correct assembly layout is shown in section 6.2.3.
- Switch the supply to the Board on and measure the values required to complete table 6.2.2.2.

U1 [V]	U2 [V]	U <sub>tot</sub> [V]	I <sub>L</sub> [mA]

Table 6.2.2.2: Series circuit of voltage sources

- Calculate the actual value of load resistance,  $R_L$ .

## Practical Experiments

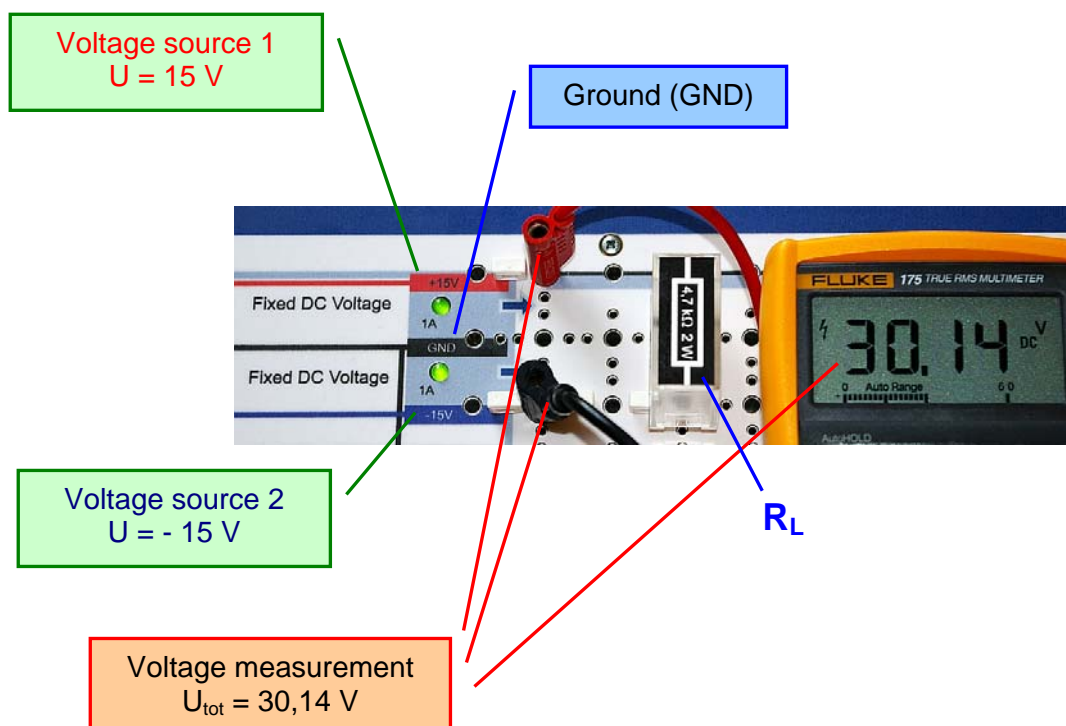
What power is dissipated at the consumer (load resistor)? What power is delivered by each individual voltage source?

- Which current direction – technical or physical – is indicated for the load current,  $I_L$  in Fig. 6.2.2.1 and why?

### 6.2.3 Exercise Assembly on the Electronic Circuits Board

Fig. 6.2.3.1 shows the correct method of connecting the 2 Fixed DC Voltage sources in series for addition of the individual voltage outputs.

Fig. 6.2.3.1: Series connection of 2 fixed voltage sources



## Practical Experiments

### 6.3 Parallel Connection of Voltage Sources

#### 6.3.1 Properties of Parallel Connected Voltage Sources

Low-resistive consumers draw a high current from a voltage supply. High currents however, produce large losses at the internal resistance of the source and in some cases, could cause a break down of the output voltage. By connecting voltage sources in parallel, the total internal resistance of the voltage sources  $R_{i\ tot}$ , is reduced which results in the output (terminal) voltage remaining almost constant, even with a large flow of current.

Fig. 6.3.1.1 shows that in a parallel connection, similar poles are connected together. Thus, the branch currents  $I_1$  to  $I_n$  are added to give the load current  $I_L$ :

$$I_L = I_1 + I_2 + I_3 + \dots + I_n$$

Basically, the output of each voltage source,  $U_{0n}$  must be the same:

$$U_{01} = U_{02} = U_{03} = \dots = U_{0n}$$

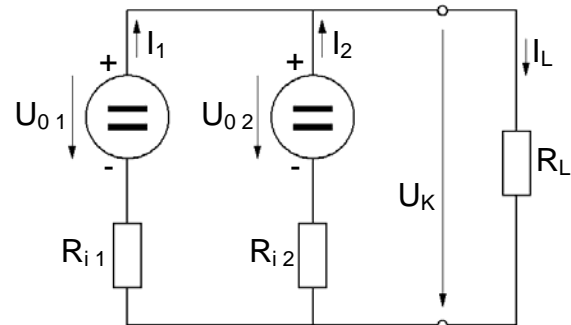


Fig. 6.3.1.1: Parallel circuit of voltage sources

If there are differences in potential, then an unwanted flow of compensating current is produced between the voltage sources. This in turn, produces internal heat losses at the internal resistance  $R_{in}$ , even when off-load.

The familiar equation for parallel circuits can be used for calculating the total internal resistance,  $R_{i\ tot}$ .

Multiple parallel connection:

$$\frac{1}{R_{i\ tot}} = \frac{1}{R_{i1}} + \frac{1}{R_{i2}} + \frac{1}{R_{i3}} + \dots + \frac{1}{R_{in}}$$

Twofold parallel connection:

$$R_{i\ tot} = \frac{R_{i1} \cdot R_{i2}}{R_{i1} + R_{i2}}$$

Identical sources:

$$R_{i\ tot} = \frac{R_i}{n}$$

#### 6.3.2 Parallel Connection of Voltage Sources as an Exercise

Two voltage sources on the Board are connected in parallel for examining their properties by measurement. Their internal resistance will be simulated by connecting an 'external  $R_i$ ' (Fig. 6.3.2.1).

- First, set the output of the Variable DC Voltage source to  $U_{02} = 15\text{ V}$ . Then, switch the Board off again.

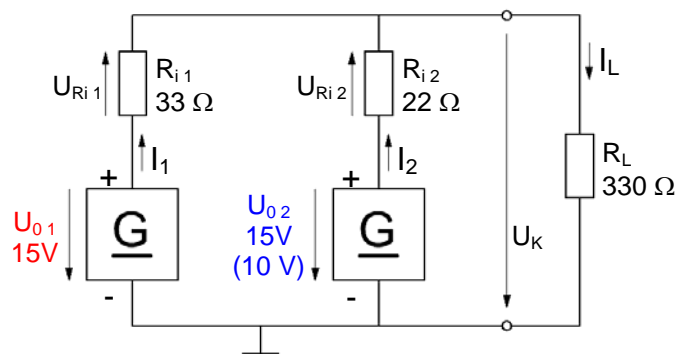


Fig. 6.3.2.1: Parallel circuit of voltage sources



## Practical Experiments

- Assemble the circuit in Fig. 6.3.2.1 on the Board. Use the Fixed DC Voltage as source voltage  $U_{01} = 15\text{ V}$  and the Variable DC Voltage as  $U_{02} = 15\text{ V}$ .
- Measure the values to complete table 6.3.2.2 with equal source voltages ( $U_{01} = U_{02}$ ).

$U_{01} = U_{02}$	$U_{Ri1}$ [V]	$U_{Ri2}$ [V]	$U_K$ [V]	$I_1$ [mA]	$I_2$ [mA]	$I_L$ [mA]
<b>Off-load</b>					X	X
<b><math>R_L = 330\ \Omega</math></b>						

Table 6.3.2.2: Measurements at parallel connected voltage sources ( $U_{01} = U_{02}$ )

- Why does a small compensating current flow between the two voltage sources when operated off-load?
- What relationship exists between the values of current measured ( $I_1$ ,  $I_2$  and  $I_L$ ), when the consumer,  $R_L = 330\ \Omega$  is connected?
- Why are the voltage drops across the internal resistances  $R_{i1}$  and  $R_{i2}$  almost identical, although the current flows through each  $I_1$  and  $I_2$ , are different?
- Calculate the total internal resistance,  $R_{i\text{tot}}$  from the measured values in table 6.3.2.2.
- Check the calculation of total internal resistance,  $R_{i\text{tot}}$  using the equation from section 6.3.1 and the nominal values for  $R_{i1}$  and  $R_{i2}$ .
- Measure the terminal voltage,  $U_K$  again with a load of  $R_L = 330\ \Omega$ . The value obtained should correspond to the value measured in table 6.3.2.2. With the supply voltage switched on, withdraw  $R_{i2} = 22\ \Omega$  from the circuit, to supply the consumer with only  $U_{01}$ . What value is the terminal voltage  $U_K$ ? Explain the change.

- Now set the source voltage  $U_{02}$  to 10 V. The output of the Variable DC Voltage source must remain 'open circuit'.
- Connect the two (different) voltage sources ( $U_{01} \neq U_{02}$ ) in parallel as in Fig. 6.3.2.1 and measure the values to complete table 6.3.2.3.

$U_{01} \neq U_{02}$	$U_{Ri1}$ [V]	$U_{Ri2}$ [V]	$U_K$ [V]	$I_1$ [mA]	$I_2$ [mA]	$I_L$ [mA]
<b>Off-load</b>					X	X
<b><math>R_L = 330 \Omega</math></b>						

Table 6.3.2.3: Measurements at parallel connected voltage sources ( $U_{01} \neq U_{02}$ )

- How can the comparatively high value for  $I_1$  in off-load operation, be explained?
- What relationship exists between your measured values of current  $I_1$ ,  $I_2$  and  $I_L$ , when the consumer  $R_L = 330 \Omega$  is connected?
- Is it appropriate to supply a consumer (e.g. an electronic circuit), from a parallel connection of two differing sources of voltage?

6.3.3 Exercise Assembly on the Electronic Circuits Board

Fig. 6.3.3.1 shows the correct method of connecting the 2 voltage sources Fixed DC Voltage and Variable DC Voltage, in a parallel circuit.

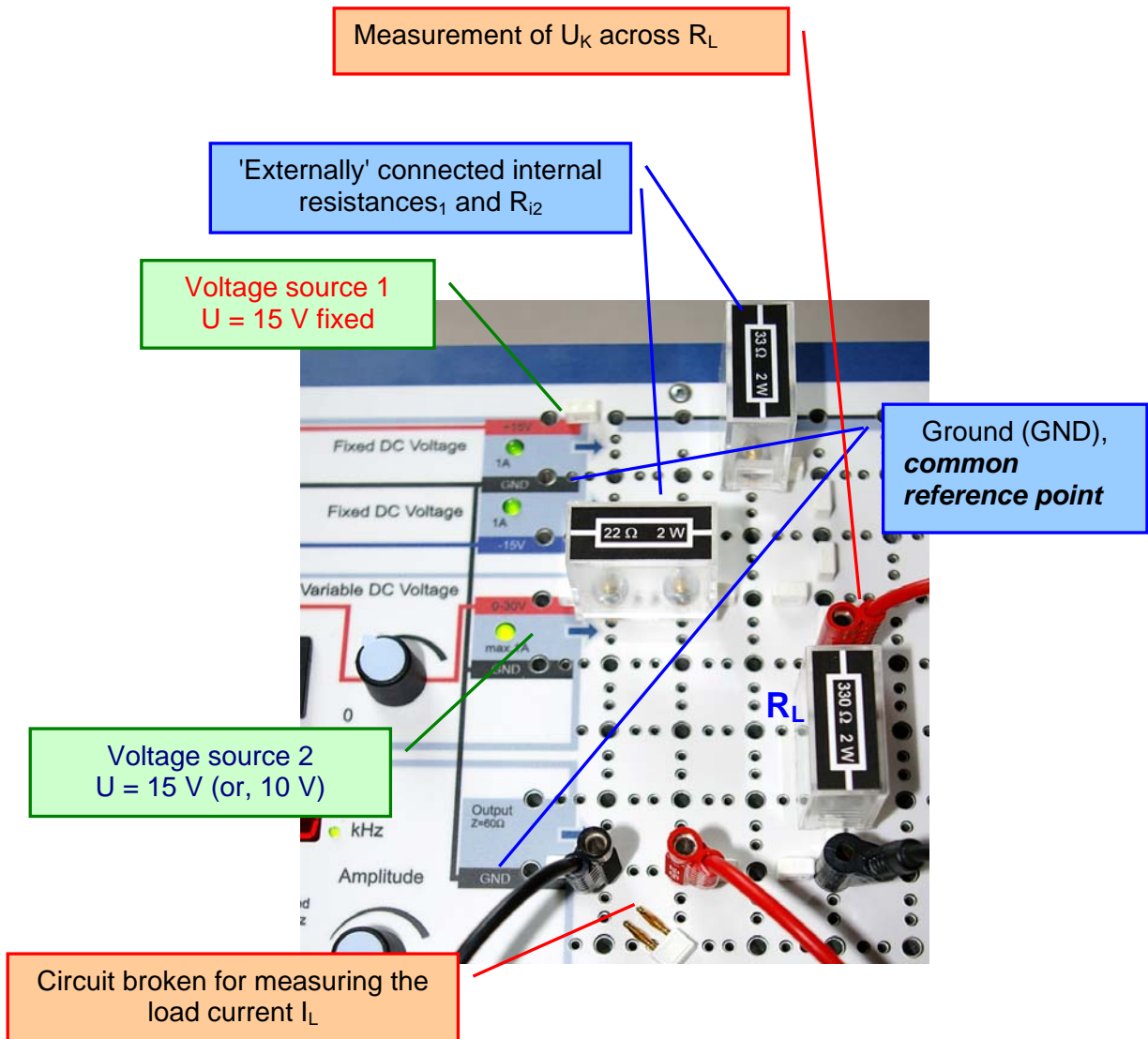


Fig. 6.3.3.1: Parallel circuit of 2 voltage sources on the Board

## 7. Electrical Energy and Power

### 7.1 Energy and Power in an Electrical Circuit

Consider the example of operating a garden pump, to pump 100 litres of underground water up to garden level. This involves a certain amount of 'work' and the 'power' invested in the work will be felt when this has been accomplished in the old-fashioned way, i.e. by mechanical means using a pump handle. Also, it is clear that the efforts involved must be sustained over a certain period of time until the amount of water required, has been pumped. Therefore, work or 'energy' can be defined as 'power' that must be available for a specified time:

$$\text{Work} = \text{Power} \times \text{Time} \quad \Rightarrow \quad W = P \cdot t$$

If the pump is to be fitted with an electric drive, a voltage U, must be connected to the input terminals that will then cause a current I to flow. In electric circuits, power is calculated from the product of voltage U and current I (unit: Watt, W):

$$P = U \cdot I$$

As long as the current flows, energy is consumed, i.e. power for a specified time. Thus, the energy or work W, in an electric circuit is calculated as:

$$W = U \cdot I \cdot t$$

The unit of electrical energy or work, is the 'watt-second' (Ws) or 'kilowatt-hour' (kWh = 1.000 W x 3600 s).

The electrical work consumed in a household is measured on a meter (kWh meter) and depending on existing contract agreements, must be paid for quarterly or annually. The electrical energy provider is not really interested on how this energy has been used:

- The work W can be the sum of smaller amounts, added over a long period (e.g. filament lamps).
- The same quantity of work can also result from using one consumer for a short time (e.g. an oven or electric heater).

From the examples it is clear the electric power P used for producing a certain amount of work, is usually converted to other forms of energy. Voltage and current produce movement (electric motor), sound waves (loudspeaker), light (lamps), warmth (electric heating) or cooling (refrigerator or freezer). However, when operating electric or electromechanical equipment, there are always unwanted power losses, such as the already known thermal power dissipation at resistances ( $P_v$ ).

Electric power P is calculated from the known variables:

$$P = U \cdot I$$

or substituting current:  $P = U \cdot I \quad \text{and} \quad I = \frac{U}{R} \quad \Rightarrow \quad P = \frac{U}{R} \cdot U \quad \Rightarrow \quad P = \frac{U^2}{R}$

or Substituting voltage:  $P = U \cdot I \quad \text{and} \quad U = R \cdot I \quad \Rightarrow \quad P = R \cdot I \cdot I \quad \Rightarrow \quad P = I^2 \cdot R$

## Practical Experiments

### 7.2 Practical Exercises, Power and Work in an Electric Circuit

The practical exercises following will show the relationships between the basic variables voltage  $U$ , current  $I$ , resistance  $R$  and the electric power. A series of measurements will be recorded in the circuit shown in Fig. 7.2.1 and represented in a graph. The resistor components used in the circuit,  $100\ \Omega$ ,  $220\ \Omega$  and  $330\ \Omega$ , all have a maximum power dissipation of  $P_V = 2\ \text{W}$ .

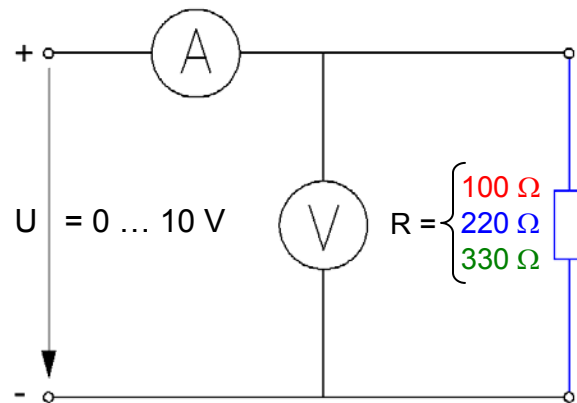


Fig. 7.2.1: Circuit with resistors

- By calculation, first ensure that the intended input voltage of  $U = 0 \dots 10\ \text{V}$  does not exceed the maximum power dissipation of the resistors.

- Assemble the circuit in Fig. 7.2.1 on the Electronic Circuits Board for recording the measurements.

- Measure the values of current as a function of voltage and resistance. Enter the values measured in table 7.2.2.

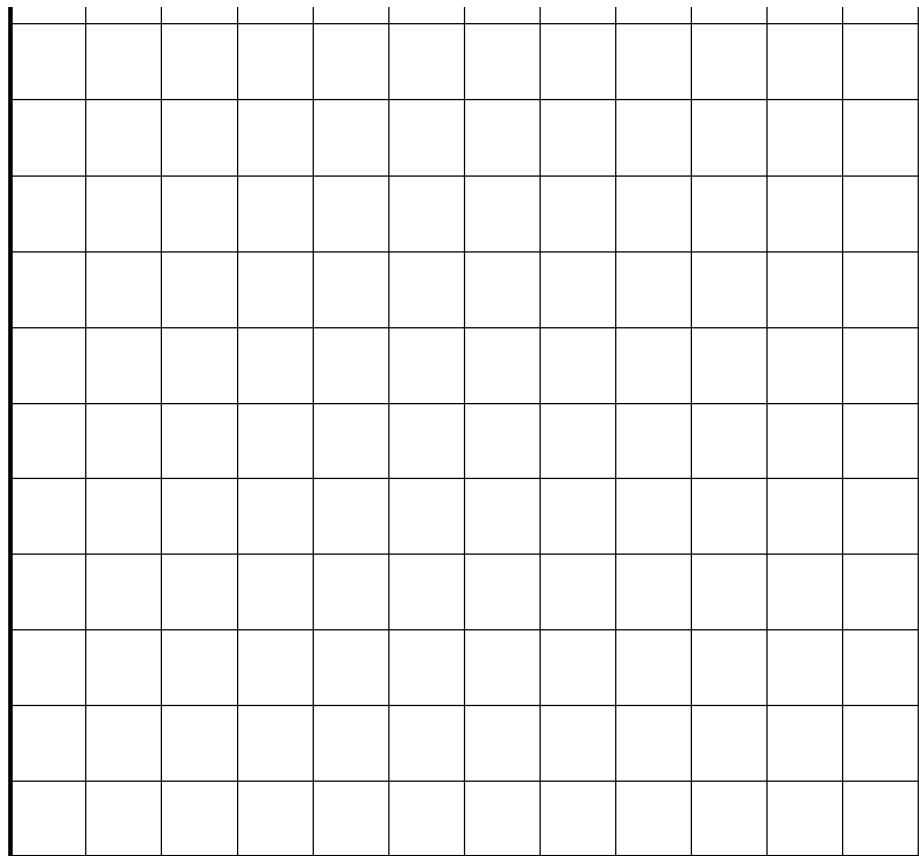
	U [V]	1	3	4	5	7	8	10
R = 100 Ω	I [mA]							
	P [mW]							
R = 220 Ω	I [mA]							
	P [mW]							
R = 330 Ω	I [mA]							
	P [mW]							

Table 7.2.2: Values measured at various resistors

## Practical Experiments

- Complete the values for power  $P$ , in table 7.2.2 by calculation.
- Now, the power characteristic  $P = f(U)$  will be drawn, using the measured values from the table. What basic curve shape do you expect to produce for the characteristic? Give reasons for your answer.
  
- Plot the measured values in the chart (Fig. 7.2.3). draw the characteristics  $P = f(U)$  for each of the 3 resistors.

Fig. 7.2.3:  
Characteristics  
 $P = f(U)$



- What is the significance of the parabolic shape ( $y = a x^2$ ) of the characteristic for the power transformed at a consumer?

- What conclusion can be drawn from a comparison of the 3 characteristics?
- In a voltage – current graph (Fig. 7.2.5), all points corresponding to a power of 2 W are to be plotted to produce a graph ('power hyperbola'). Using the voltage values given in table 7.2.4 and a constant power of  $P = 2\text{ W}$ , calculate the current flow at each value of voltage. Which formulae should be used?

Formula:

<b>U [V]</b>	<b>2</b>	<b>2,5</b>	<b>3</b>	<b>3,5</b>	<b>5</b>	<b>7</b>	<b>9</b>	<b>10</b>
<b>I [A]</b>								

Table 7.2.4: Voltage and current at a constant power of  $P = 2\text{ W}$

- Plot the values of U and I in the chart (Fig. 7.2.5) and join the plotted points to produce the power hyperbola for a 2 W resistor.

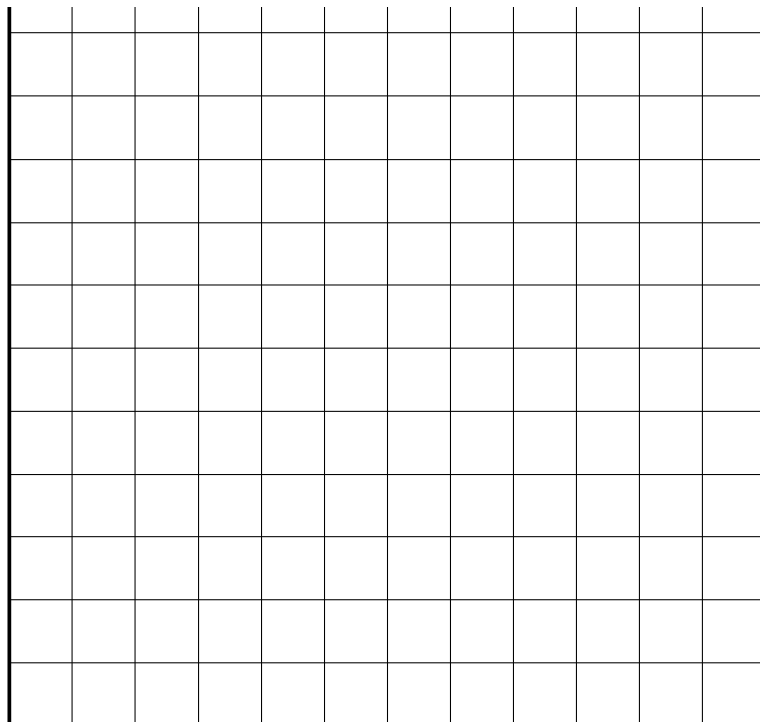


Fig. 7.2.5: Power hyperbola, 2 W

A power hyperbola graph can be used to determine the maximum permissible voltage drop at a 2 W resistor. First, the characteristic  $I = f(U)$  of the relevant resistor, must be drawn in the graph Fig. 7.2.5. The intersecting point of the resistance characteristic and the hyperbola corresponds to the maximum voltage and also shows the value of current flow.

## Practical Experiments

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- Draw the resistance characteristic  $I = f(U)$  for the  $22 \Omega$  resistor in the graph (Fig. 7.2.5), using 2 voltage values.
  
- What is the maximum value of voltage that may exist across the  $22 \Omega$  resistor on the Electronic Circuits Board, so that the maximum power dissipation ( $P_V = 2 \text{ W}$ ) of the component is not exceeded? Determine this value and the current flowing, from the graph in Fig. 7.2.5.
  
- Check the values by calculation.
  
- Insert a resistor of  $R = 22 \Omega$  in the circuit as in the circuit, Fig. 7.2.1. Set the voltage drop across this resistor to the maximum permissible  $6,63 \text{ V}$  as accurately as possible and check that the current flow is in fact,  $0,3 \text{ A}$ .

Assume that today is Friday and you have forgotten to switch off the Electronic Circuits Board before leaving for the weekend. How much power  $W$  in Watt-seconds [Ws] has been consumed if the voltage  $U_{\max} = 6,63 \text{ V}$  was switched on for exactly 3 days at the resistor  $R = 22 \Omega$ ?

- Convert the result to kilowatt hours [kWh].



## 8. Efficiency and Electrical Power

### 8.1 Definition and Significance of Efficiency

Energy (power) can neither be generated nor lost. Reference to energy generators means really, systems that convert one form of energy to another. For example, 'generation' of water-power to drive turbines that generate voltage. Here, the turbines first convert the potential (displacement) energy stored in the water, to torque that is then passed on to a generator. The generators transform the mechanical power to electrical power.

The electrical power obtained after this double conversion process, is not however, 100% of the original potential (displacement) energy stored in the water. Some of the energy is lost on secondary, unwanted conversion processes. For example, heat produced by friction is lost to the surrounding air, wherever there is mechanical movement. Thus, any machine, all equipment, even the biological system of the human body, suffer specific losses when 'operating' to produce some form of power.

In short, the power consumed for operating an equipment is always greater than that supplied to the User. This applies in a similar fashion to electromechanical equipment or electrical circuits. The **efficiency** of an electrical / electronic system is defined as the quotient of **delivered effective power  $P_{del}$**  and **supplied operating power  $P_{sup}$** .

Formula: 
$$\eta = \frac{P_{del}}{P_{sup}} \quad \left| \begin{array}{l} P_{del} \text{ and } P_{sup} \text{ in W} \\ \eta = \text{Numerical value} < 1 \text{ or a percentage} < 100 \end{array} \right.$$

In the same way, the efficiency can be calculated from the ratio of delivered work to the work used.

Then, 
$$\eta = \frac{W_{del}}{W_{sup}} \quad \left| \begin{array}{l} W_{del} \text{ and } W_{sup} \text{ in Js} \\ \eta = \text{Numerical value} < 1 \text{ or a percentage} < 100 \end{array} \right.$$

A few examples of possible efficiency:

Machine, Process, etc.	Energy applied	Useful energy	Efficiency, $\eta$
Hydroelectric power station	Potential (displacement) energy	Electrical	80 to 90 %
Coal power station	Fossil, Chemical	Electrical	25 to 50 %
Wind power station	Wind	Electrical	Up to 50 %
Filament lamp	Electric	and Light	3 to 5 %
Electric motor	Electric	Mechanical	20 to 99 %

Table 8.1.1: Examples of efficiency

## Practical Experiments

### 8.2 Practical Exercises on Efficiency

An electronic circuit is supplied with a DC voltage of 7 V by way of an 8 m long cable and the same length of return cable. The cable has an ohmic resistance of  $R = 2 \Omega$  per meter. Thus, the total resistance of the cable is  $2 \cdot 8 \text{ m} \cdot 2 \Omega = 32 \Omega$ . The circuit supplied by the DC voltage has an internal resistance of  $R_i = 680 \Omega$ .

This application is simulated with resistors on the Electronic Circuits Board as shown in Fig. 8.2.1. The cable resistance is distributed equally along the supply and return cables. Since there are no other resistors available, the total resistance of the cable simulation (Fig. 8.2.1) is made up with 2 resistors from the E12 preferred value range.

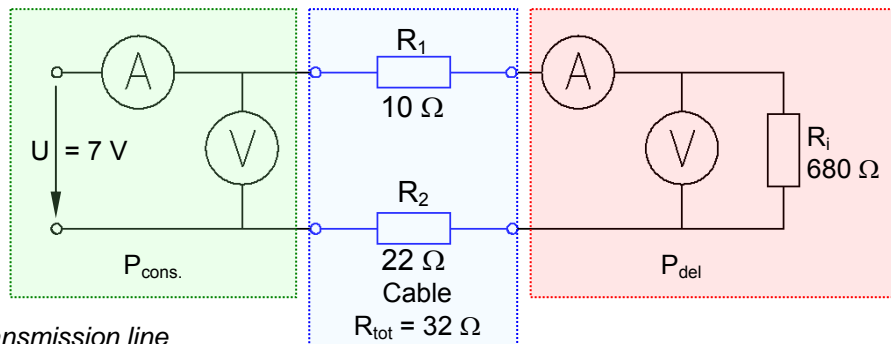


Fig. 8.2.1: Simulation of a transmission line

- Assemble the simulation circuit shown in Fig. 8.2.1 on the Electronic Circuits Board.
- Measure the values of voltage and current at the input and output terminals of the 'cable' and enter the values in table 8.2.2.

Cable input (supplied power)		Cable output (delivered power)	
$U_{in} =$	$I_{in} =$	$U_{out} =$	$I_{out} =$

Table 8.2.2: Values measured at the cable terminals

- From the measured values, calculate the efficiency of the transport of energy on the cable.

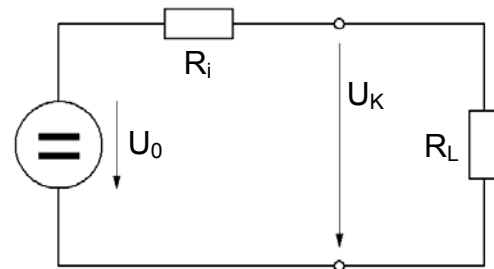
## 9. Power, Voltage and Current Matching

### 9.1 Derivation and Significance of Loading Conditions

In electrical and electronic circuit engineering, it is often necessary to couple standalone (independent) sections of a circuit, together. Here, the output of one circuit delivers power to the input of the next circuit.

Fig. 9.1.1 shows this principle with the example of a DC voltage source that supplies a load resistor  $R_L$ . The ratio between the internal resistance  $R_i$  and the load resistor  $R_L$  determines how much of the original voltage  $U_0$  is dropped across the load resistor  $R_L$  and is available as terminal voltage  $U_K$ . Thus, at the same time, current and power transferred are also determined. The power delivered from the voltage source, to the load resistor, is a maximum when  $R_i = R_L$ ; the power can assume any value between maximum and zero when  $R_i \neq R_L$ . Two (possible, but theoretical) limiting cases will be explained here:

Fig. 9.1.1: Loading on a voltage source



**$R_L = \infty$  ; Off-load:** The output terminals of a voltage source are open-circuit, i.e. no load is connected ( $U_K = U_0$ ). The larger the load resistance compared to the internal resistance ( $R_L \gg R_i$ ), the closer are the conditions for off-load operation. In off-load operation, no power is delivered to the consumer since there is no flow of current:

$$P = U \cdot I = U_K \cdot 0 = 0$$

**$R_L = 0$  ; Short circuit:** If the output terminals of a voltage source are short-circuited with a wire bridge, the maximum possible current flows, the short-circuit current. This current is limited only by  $R_i$ . In this case, out of necessity, the terminal voltage completely collapses ( $U_K = 0$ ), which is why no power is transferred to the consumer. The smaller the load resistance compared to the internal resistance ( $R_i \gg R_L$ ), the closer the ratio's approach the conditions of a short circuit.

$$P = U \cdot I = 0 \cdot I_{\max} = 0$$

These limit cases of loading conditions, have little significance in practical circuit engineering. The matching conditions are therefore, differentiated as follows:

**$R_L = R_i$  ; Power matching:** In the case of the maximum power  $P$ , delivered to the consumer, half of the source voltage  $U_0$  is dropped across  $R_L$  and half, across  $R_i$ .

**$R_L \gg R_i$  ; Voltage matching:** A large part of the source voltage is available at the load resistance, there is a small flow of load current. This case tends towards the conditions for an off-load state ( $R_L \rightarrow \infty$ ).

**$R_L \ll R_i$  ; Current matching:** The consumer draws a relatively high current from the voltage supply. The terminal voltage falls to less than half of the source voltage. Current matching tends towards the conditions of the short-circuit ( $R_L \rightarrow 0$ ).

## Practical Experiments

### 9.2 Practical Exercises for Loading Conditions

Power, voltage and current matching, also the limit cases of short circuit and off-load, should be examined by way of the characteristic at the consumer. Of particular importance, is to show by measurements, that with power matching when  $R_L = R_i$ , the highest amount of power is delivered to the consumer.

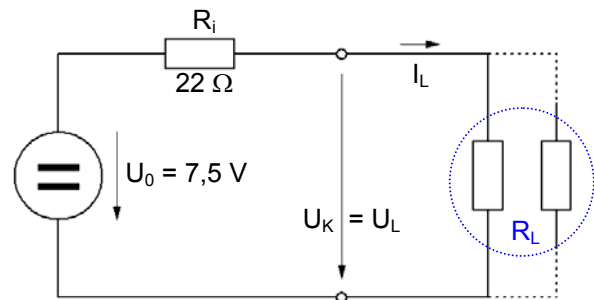


Fig. 9.2.1: Voltage source with consumer

Since the voltage sources on the Electronic Circuits Board all incorporate voltage stabilisation ( $R_i = 0 \Omega$ ), an internal resistance of  $R_i = 22 \Omega$  will be simulated by an external resistor (Fig. 9.2.1). The load  $R_L$  is formed with individual resistors, in both a series and parallel circuit (Fig. 9.2.1 and Table 9.2.2).

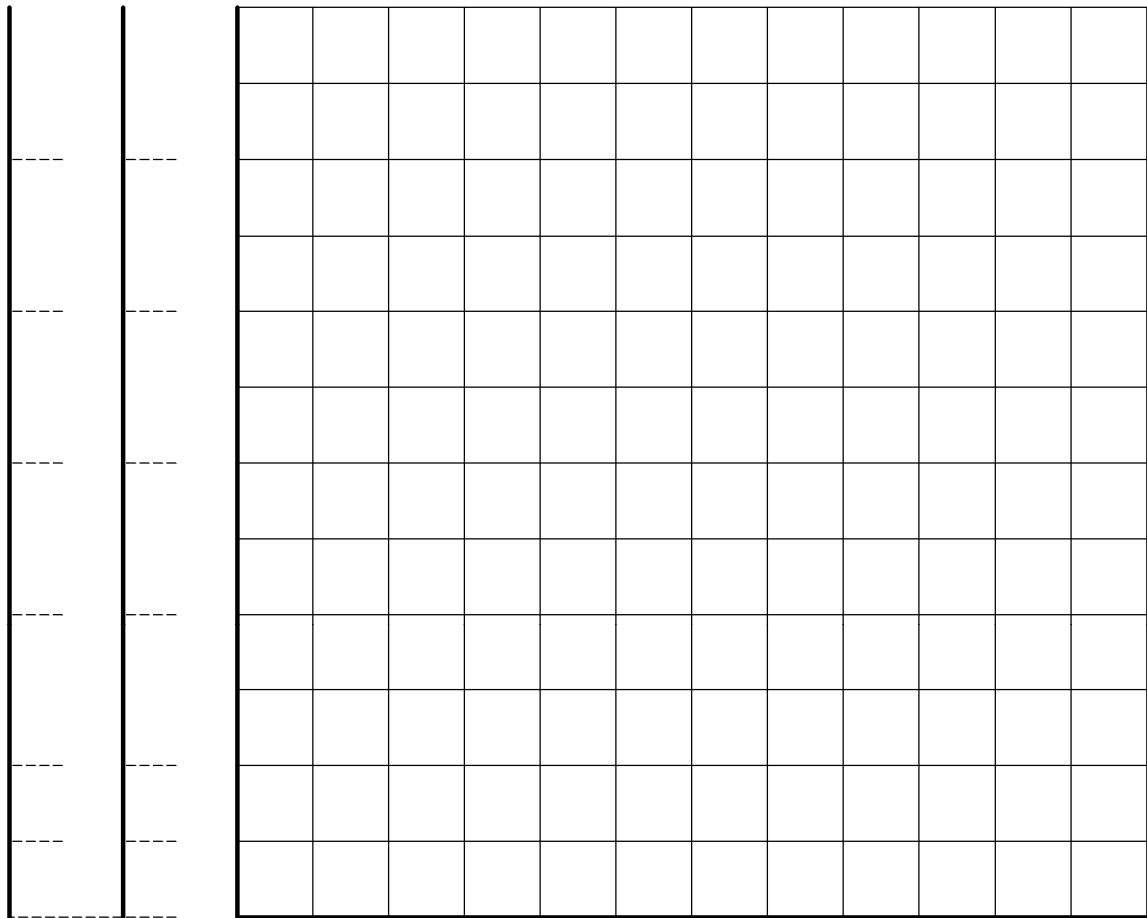
- Calculate the equivalent resistance values for the series and parallel circuits and enter the values in table 9.2.2.
- Have the following values of resistor to hand:  $10 \Omega$ ,  $2 \times 22 \Omega$ ,  $33 \Omega$ ,  $100 \Omega$ ,  $220 \Omega$ . Assemble the circuit in Fig. 9.2.1 on the Electronic Circuits Board.
- Start the series of measurements with the limit values 'off-load', i.e. with open circuit output terminals at the voltage source.
- Measure the load current  $I_L$  and terminal voltage  $U_K$  for each of the loading conditions ( $R_L$ ). given in table 9.2.2. Enter the measured values in the table.

					Series 10+33 $\Omega$	Parallel 100//220 $\Omega$		
$R_L$ [ $\Omega$ ]	0	10	22	33			100	$\infty$
$I_L$ [mA]								
$U_K$ [V]								
P [mW]								

Table 9.2.2: Measurements for determining the power matching

- From the measured values, calculate power delivered  $P$  to each consumer ( $R_L$ ). Enter the measured values in the table.
- Using the measured values, draw the characteristics  $I_L = f(R_L)$ ,  $U_{L(K)} = f(R_L)$  and  $P = f(R_L)$  in the chart (Fig. 9.2.3).

Fig. 9.2.3: Characteristics  $I_L = f(R_L)$ ,  $U_{L(K)} = f(R_L)$  and  $P = f(R_L)$



- What conclusion can be drawn from the power characteristic  $P = f(R_L)$  with regard to power matching?
- Where are the limit cases 'off-load' and 'short circuit' located on the characteristics?
- In which areas of the graph are the conditions for voltage matching and current matching?

## 10. Types of Current (Voltage) and their Characteristics

### 10.1 Types of Current (Voltage)

The discussions up to now, have dealt exclusively with electrical processes based on the flow of a **direct current (DC)**. A property of DC is the **constancy with respect to time of the magnitude of the current**. This causes a **continual flow of current in one direction** in an electrical circuit. The magnitude and direction of the DC current is caused by a constant **DC voltage**. At various instants of time ( $t_1, t_2$ , etc.), stable conditions can be measured at the terminals of a DC voltage source, in the circuit and at the consumer<sup>1</sup>. Fig. 10.1.1 shows the voltage and flow of current over a period of several seconds.

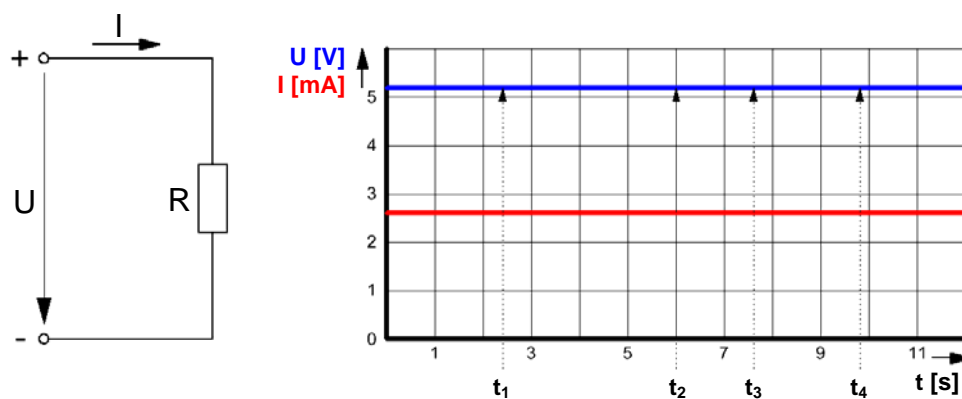
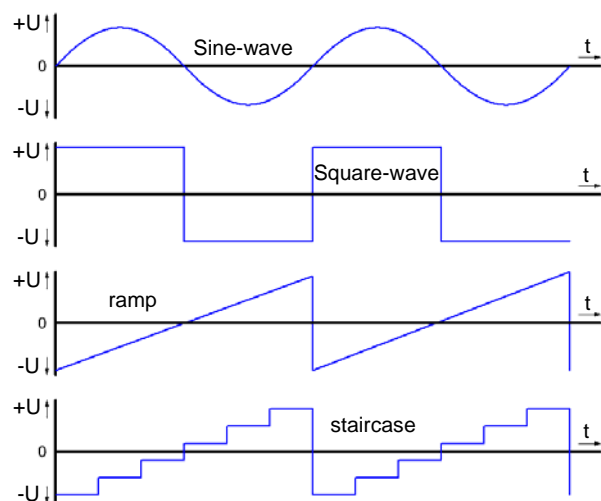


Fig. 10.1.1: Time characteristic of DC voltage and current

The term **alternating current** is used when the current in a circuit periodically changes in magnitude and direction. This alternating current (AC) is caused by an alternating voltage applied to the circuit. Fig. 10.1.2 shows various forms of AC voltage that have been displayed on an oscilloscope, used in circuits depending on the required effect or function of the circuit. The voltage curves shown are known as '**sine-wave**' (or sinusoidal), '**square-wave**', '**ramp**' (or sawtooth) and '**staircase**' voltages. For all voltages above the zero axis (+U) a varying current flows according to the magnitude (or '**amplitude**') of the voltage, in the same direction. When the voltage changes to the area below the zero axis (-U), the current flows in the opposite direction.

Fig. 10.1.2: Examples of alternating voltages



<sup>1</sup> The slow excursions of electrical properties caused by unwanted physical influences such as the temperature variations in a resistor, are ignored.

## Practical Experiments

### 10.2 Characteristics of Sine-wave Voltages (and Current)

#### 10.2.1 Derivation of the Characteristics

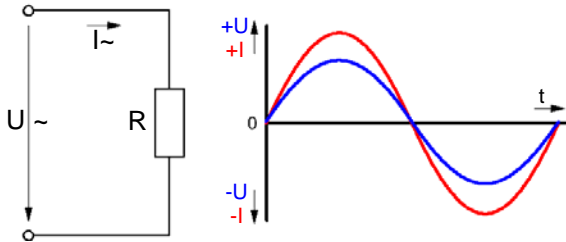
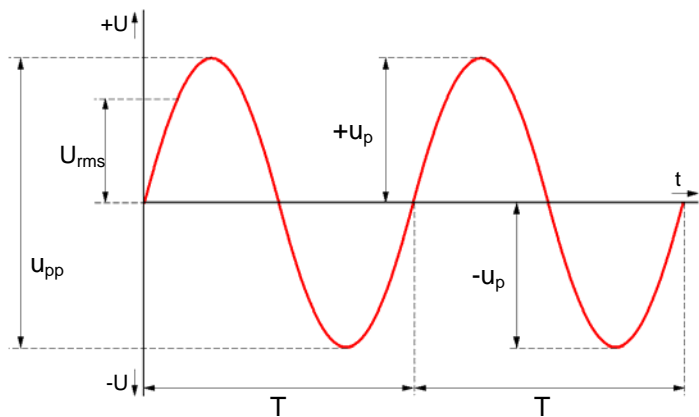


Fig. 10.2.1.1: Voltage and current, 'in phase'

At pure ohmic consumers, such as a simple resistor, the responses of voltage and current follow the same conditions with respect to time (Fig. 10.2.1.1). Voltage and current are said to be '**in phase**'. The descriptions of the characteristics that follow assume corresponding temporal conditions for voltage and current.

The amplitude between the zero axis and maximum value, is known as the **peak value ( $u_p$ )** of the sine-wave (Fig. 10.2.1.2) and can be a positive ( $+u_p$ ) or negative ( $-u_p$ ) value. The voltage between the peak values (Fig. 10.2.1.2) is known as the **peak-to-peak value ( $u_{pp}$ )**. These properties of the voltage can be displayed and measured on an oscilloscope. If an alternating voltage (or current), is measured with a voltmeter (or ammeter), the indicated value corresponds to the effective value of voltage (or current). This effective value is more often referred to as the **root mean square value ( $U_{rms}$  or  $I_{rms}$ )**. The following relationships between rms values and peak values for sine-wave voltages or currents:

Fig. 10.2.1.2: Characteristics of a sine-wave voltage



$$U_{rms} = \frac{1}{\sqrt{2}} \cdot u_p \cong 0,707 \cdot u_p \quad ; \quad I_{rms} = \frac{1}{\sqrt{2}} \cdot i_p \cong 0,707 \cdot i_p$$

From the sine-waves shown in Figs. 10.2.1.1 and 10.2.1.2, the regular recurrence of maxima, minima and crossing of the zero axis, exhibit a *periodic response*. This 'period of oscillation', or **periodic time,  $T$**  specifies the length of time after which the voltage or current wave is repeated. Using this periodic time  $T$ , the **frequency,  $f$**  of an alternating voltage can be determined. Thus:

$$f = \frac{1}{T} \quad \left[ 1Hz = \frac{1}{1s} = 1s^{-1} \right]$$

1 Kilohertz	=	1 kHz	=	1.000 periods/s
1 Megahertz	=	1 MHz	=	$10^6$ periods/s
1 Gigahertz	=	1 GHz	=	$10^9$ periods/s

The unit of frequency is the Hertz (named after the German physicist *Heinrich Rudolf Hertz* in 1935). Commonly used units are also kilo-, Mega- or Gigahertz.

## Practical Experiments

The same characteristic quantities (i.e.  $U_{\text{rms}}$ ,  $u_p$ ,  $T$ ,  $f$ ) are used in part, for other waveforms of voltage (square-wave, ramp, etc.). It must be remembered here, that the relationship between the effective voltage  $U_{\text{rms}}$ , and the peak voltage  $u_p$  depends on the shape of the voltage waveform.

For various other calculations, especially on non-ohmic components, the **angular frequency**  $\omega$  is used, given by the periodic time  $T$  or frequency,  $f^2$ :

$$\omega = 2 \cdot \pi \cdot \frac{1}{T} \quad \Rightarrow \quad \omega = 2 \cdot \pi \cdot f \quad \left[ 1 \frac{\text{rad}}{\text{s}} \right]$$

Occasionally in calculations, the **instantaneous value**  $u$  or  $i$  of a sine-wave is required. Here, the following equations are used:

$$u = u_p \cdot \sin \omega \cdot t \quad ; \quad i = i_p \cdot \sin \omega \cdot t$$

Current requires time to flow from one pole through a circuit, to the other pole. Assuming a sufficiently long cable, there are several minima, maxima and zero passes of an alternating current present along a connection cable, simultaneously. The longer the cable (or, the higher the frequency), the more complete periodic time intervals are formed along the cable at the same time. The distance bridged by one periodic time  $T$  is known as the **wavelength**,  $\lambda$ . The name stems from the wave shape of a sine-wave oscillation. The wavelength  $\lambda$  is given by the quotient of the velocity of propagation of a wave  $v$  and the frequency  $f$ :

$$\lambda = \frac{v}{f} \quad ; \quad \lambda_{\text{space}} = \frac{c}{f}$$

Under certain conditions, electrical energy can also radiate (or propagate) in free space in the form of waves, without any conducting connection (e.g. radio waves, mobile telephone, etc.) In this case, the velocity of propagation is the same as the speed of light,  $c$  ( $\sim 300.000 \text{ km/s}$ )<sup>3</sup>. In conducting materials, the velocity of propagation of electrical waves is approximately 30% less than the speed of light in free space.

### 10.2.2 Characteristic Quantities of a Sine-wave Voltage in a Practical Exercise

The characteristic quantities are to be measured and their inter-relationships proved, in a circuit consisting of an AC voltage source (generator  $G$   $\sim$ ) and a load resistor  $R_L$ .

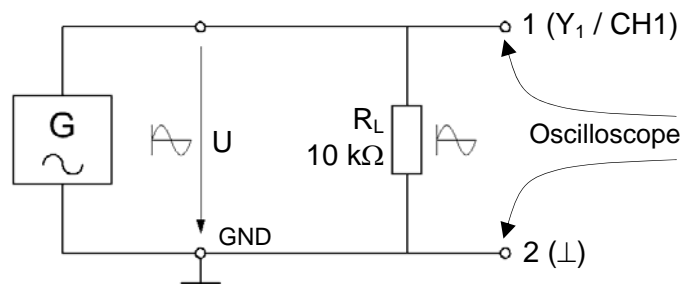


Fig. 10.2.2.1: Sine-wave generator with load resistor,  $R_L$

- Assemble the circuit in Fig. 10.2.2.1 on the Electronic Circuits Board (notes on assembly will be found in section 10.2.3).

<sup>2</sup> The unit 'rad' (radian) indicates that the value is the magnitude of an angle (in circular measurements)

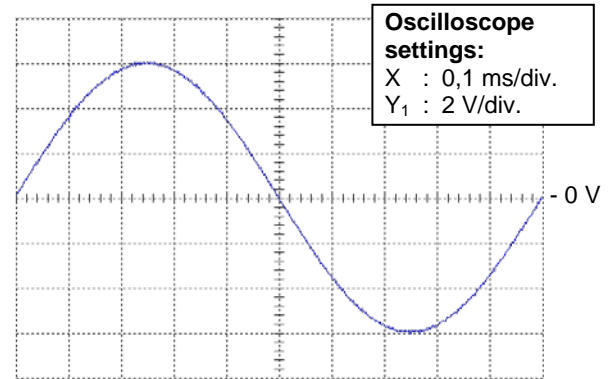
<sup>3</sup> Strictly speaking, the propagation velocity of waves of electrical energy is equal to the speed of light, only in a vacuum.



## Practical Experiments

- Connect channel 1 ( $Y_1$  or CH1) of your oscilloscope – as in Fig. 10.2.2.1 – to test terminals (outputs) 1 and 2 of the circuit.
- Set the output of the function generator on the Electronic Circuits Board, between the sockets 'Output' and 'GND', to the sine-wave voltage shown in Fig. 10.2.2.2. With the given values of timebase and amplitude, the sine-wave should be displayed on the oscilloscope as shown in Fig. 10.2.2.2.

Fig. 10.2.2.2: Sine-wave voltage on the oscilloscope



- Measure the values required to complete table 10.2.2.1, from the oscilloscope display. Measure the instantaneous value of voltage  $u$ , 0,6 ms after the start of a period.

Table 10.2.2.3: Measurements on the oscilloscope

$+u_p$	$-u_p$	$u_{pp}$	$u$ (after 0,6 ms)	$T$

- Calculate the following quantities from the values in the table:  $i_s$ ,  $U_{rms}$ ,  $I_{rms}$ ,  $f$ ,  $\omega$ ,  $\lambda$ .

- Check the instantaneous value of voltage,  $u$ , read from the oscilloscope, by calculation.

## Practical Experiments

Check the calculated value of effective voltage,  $U_{\text{rms}}$  with the multimeter.

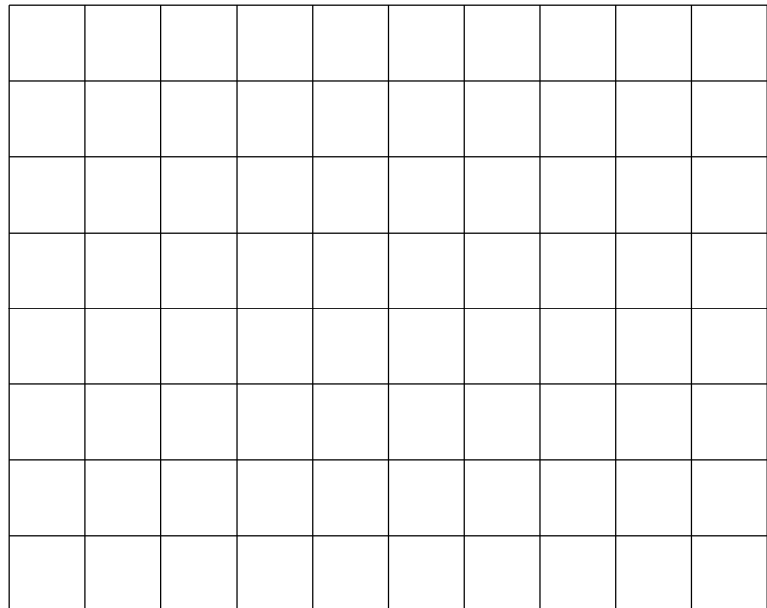
$$U_{\text{rms}} =$$

- At the output of the function generator, a sine-wave voltage of  $U_{\text{rms}} = 8 \text{ V}$  at a frequency,  $f = 250 \text{ Hz}$  should be present. First, calculate  $u_p$ ,  $u_{pp}$  and  $T$ .

- Adjust the frequency of the function generator to  $f = 250 \text{ Hz}$ . Use the meter on the function generator when adjusting the frequency. Adjust the effective voltage,  $U_{\text{rms}} = 8 \text{ V}$ , whilst measuring with the multimeter at the same time.
- First, check the calculated characteristic quantities of the output AC voltage on the oscilloscope. Draw the sine-wave in the chart below (Fig. 10.2.2.4).

Fig. 10.2.2.4:  
Oscilloscope display, 250 Hz sine-wave, 8 V rms

<p><b>Oscilloscope settings:</b>  <math>X : 1 \text{ ms/div.}</math>  <math>Y_1 : 5 \text{ V/div.}</math></p>
---



- What time elapses after the start of a period, before the sine-wave signal reaches a voltage of 5 V? Calculate the value and check the result on the oscilloscope.

## Practical Experiments

### 10.2.3 Exercise Assembly on the Electronic Circuits Board

The Function Generator on the Electronic Circuits Board is used for the exercises. It incorporates 4 possibilities of adjustment (Fig. 10.2.3.1):

- The 'Waveform' of the alternating voltage can be selected by the push-button switch 'Press to change'.
- The frequency is adjusted by way of the control marked 'Frequency' (range, 0 Hz to 210 kHz, stages depending on range).
- By pressing the control knob 'Frequency', the frequency is immediately latched at 1 kHz ('Fixed 1 kHz').
- The amplitude of the output voltage can be varied over the range 0 to  $\sim 7 V_{\text{rms}}$  with the 'Amplitude' control.

Fig. 10.2.3.1 shows the connections for the oscilloscope or multimeter for measuring the output AC voltage of 1 kHz.

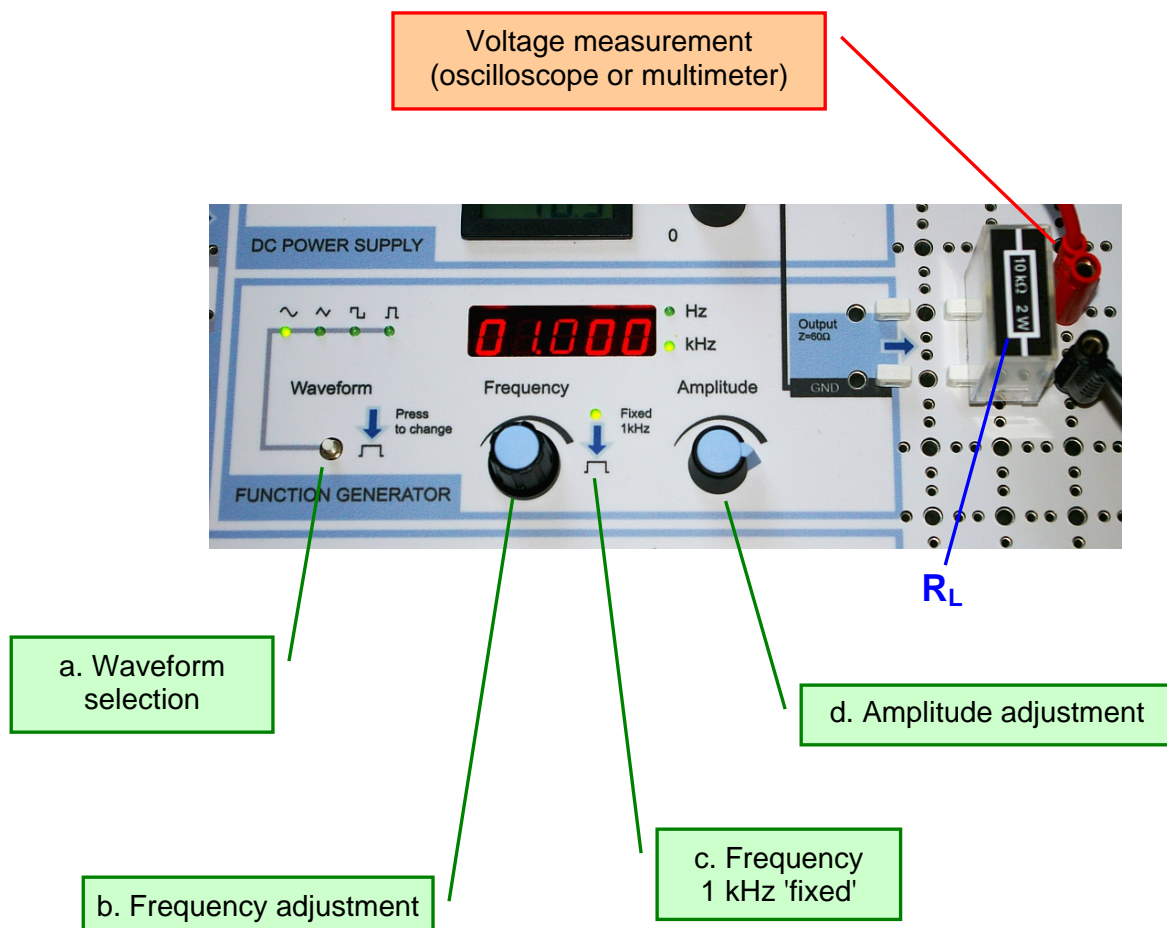


Fig. 10.2.3.1: Adjustment facilities on the function generator on the Electronic Circuits Board

## Practical Experiments

### 10.3 Characteristics of Square-wave Voltages

#### 10.3.1 Derivation of the Characteristics

As with sine-wave voltages, the **periodic time, T** specifies the length of time after which the voltage wave is repeated (Fig. 10.3.1.1). Thus, the same expressions applies for the frequency:

$$f = \frac{1}{T} \quad \left[ 1\text{Hz} = \frac{1}{1\text{s}} = 1\text{s}^{-1} \right]$$

Of more interest with square-wave voltages, are the sections of the wave-form known as **pulse duration  $t_i$**  and **interpulse period  $t_p$** . The 'pulse duration' is the time taken for the voltage to rise in a positive direction until the fall in a negative direction (Fig. 10.3.1.1). The 'interpulse period' is similarly defined in the opposite direction. The pulse duration  $t_i$  and interpulse period  $t_p$  are added to give the periodic time, T. The ratio of  $t_i$  to T is known as the **duty factor, g**. Quite often the term **duty cycle** is used although this applies more to a train of square-wave pulses:

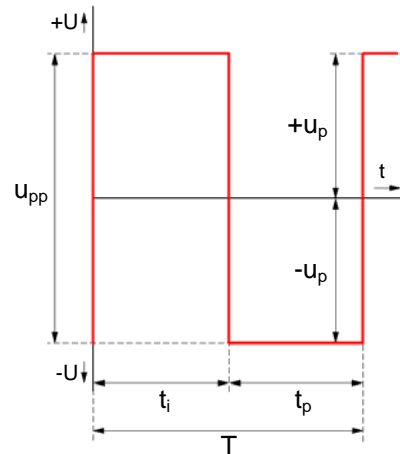


Fig. 10.3.1.1:  
Characteristics of a  
square-wave voltage

$$T = t_i + t_p \quad ; \quad g = \frac{t_i}{T}$$

If the pulse duration  $t_i$  and interpulse period  $t_p$  are the same length, the duty factor g is then 0,5. Also, if the duration of both peak values are of the same magnitude ( $\pm u_p$ ) then reference is made to a '**symmetrical square-wave voltage**' (Fig. 10.3.1.1).

**Peak values ( $\pm u_p$ )** and **peak-to-peak values ( $u_{pp}$ )** are given as with a sine-wave voltage, between maximum, minimum and zero axis (c.f. Figs. 10.2.1.2 and 10.3.1.1).

With *symmetrical* square-wave voltages the effective value,  $U_{rms}$  corresponds to the peak value  $u_p$ . This is easier to understand if one imagines the negative section to be folded up to the positive side of the zero axis.

The same statement applies to the current flows ( $i_{pp}$ ,  $i_p$ ,  $I_{rms}$ ) caused by square-wave voltages.

#### 10.3.2 Characteristic Quantities of a Square-wave Voltage in a Practical Exercise

The characteristic quantities will now be derived from measurements on a symmetrical square-wave voltage circuit as shown in Fig. 10.3.2.1.

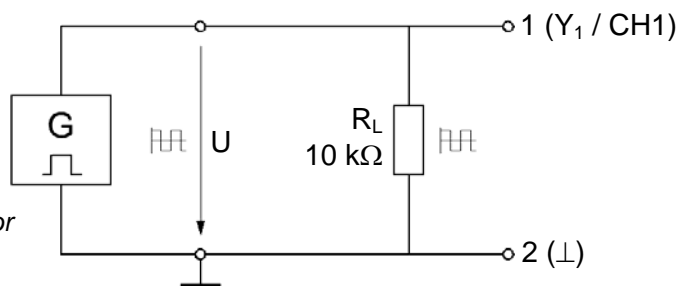


Fig. 10.3.2.1: Circuit with square-wave generator

- Assemble the circuit in Fig. 10.3.2.1 using the function generator, on the Electronic Circuits Board.
- Connect channel 1 ( $Y_1$  or CH1) of your oscilloscope to outputs 1 and 2 of the circuit.

## Practical Experiments

- Set the output of the function generator to a symmetrical square-wave voltage with the following values:  $f = 625 \text{ Hz}$ ,  $U_{\text{rms}} = 6 \text{ V}$ . To check the settings, use the frequency meter on the Board and a voltmeter.

- Display the square-wave voltage on the oscilloscope and draw the waveform in the chart given in Fig. 10.3.2.2.

Fig. 10.3.2.2: Square-wave voltage on the oscilloscope

- Measure the values of  $u_{\text{pp}}$ ,  $u_p$ ,  $T$ ,  $t_i$  and  $t_p$  from the oscilloscope display.


**Oscilloscope settings:**  
 $X : 0,4 \text{ ms/div.}$   
 $Y_1 : 2 \text{ V/div.}$

$u_{\text{pp}} = \quad ; \quad | + u_p | = | - u_p | =$

$T = \quad ; \quad t_i = \quad ; \quad t_p =$

- Calculate the peak current  $i_p$  and the duty factor of the square-wave voltage.

- Check the set frequency by calculation.

- What is the relationship between the peak value  $u_p$  read on the oscilloscope, and the value of effective voltage  $U_{\text{rms}}$  measured previously on the multimeter?

- Calculate the effective current,  $I_{\text{rms}}$

-

- Check the rms value of current by measurement on an ammeter.

$I_{\text{rms [meas.]}} =$

## Practical Experiments

### 10.4 Characteristics of Delta Voltages

#### 10.4.1 Derivation of the Characteristics

The main interest in a delta (or 'triangular') voltage, centres on the *linear* swing of the voltage between the **peak values (+/-u<sub>s</sub>)**. The relationships between peak values and **peak-to-peak value u<sub>pp</sub>** are the same as those for sine- and square-wave. Fig. 10.4.1.1 shows a *symmetrical delta* voltage. Here, the **rise time t<sub>ri</sub>** is the same as the **fall time t<sub>fa</sub>**. Both add together to give the **periodic time, T**. The effective voltage U<sub>rms</sub> is calculated from:

$$U_{rms} = \frac{1}{\sqrt{3}} \cdot u_p$$

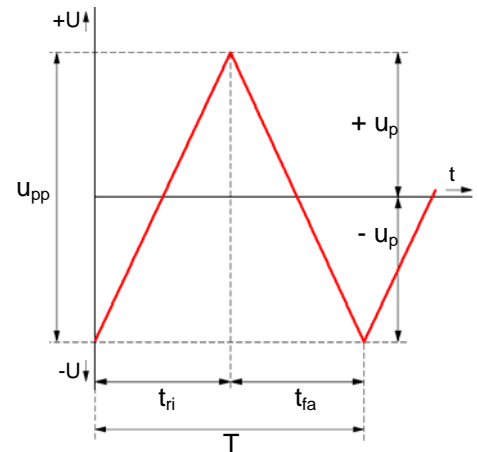


Fig. 10.4.1.1: Characteristics of a delta voltage

A common variation of a delta voltage is the ramp (or sawtooth), Fig. 10.4.1.2. The rise is made as linear as possible, with a very short fall time. One use of a ramp voltage is the deflection of the x-axis on an oscilloscope or the horizontal sweep of a TV picture. After the rise of the ramp, the fall time should be almost immediate ( $t_{fa} \cong 0$ ) and the voltage returns to its original value.

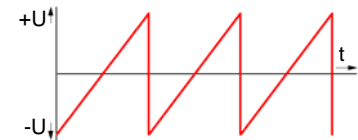


Fig. 10.4.1.2: Ramp (or sawtooth) voltage

#### 10.4.2 Characteristic Quantities of a Delta Voltage in a Practical Exercise

- Assemble the circuit in Fig. 10.4.1.2 on the Electronic Circuits Board.

- Set the output of the function generator to a symmetrical **delta voltage**,  $f = 180 \text{ Hz}$ ,  $u_p = 3,5 \text{ V}$ . Use the frequency meter on the Board and an oscilloscope.

- Measure the delta voltage on the oscilloscope. Draw the waveform in Fig. 10.4.2.1.

Fig. 10.4.2.1: Delta voltage on the oscilloscope

- On the waveform drawn, measure the values  $T$ ,  $t_{ri}$  and  $t_{fa}$ . Check  $f$  and  $U_{rms}$  by calculation.


T =                      ; t<sub>ri</sub> =                      ; t<sub>fa</sub> =

**Oscilloscope settings:**  
X : 1 ms/ div.  
Y<sub>1</sub> : 1 V/ div.

## Practical Experiments

### 11. Active Power of Alternating Voltages

#### 11.1 Derivation of AC Power

When an AC voltage is applied to an ohmic consumer, the voltage produces an 'in-phase' current (Fig. 11.1.1). The power  $P$  produced is given by the product of voltage  $U$  and current  $I$ . Usually however, the useful or **active power**  $P_{act}$  is of interest:

$$P_{act} = U_{rms} \cdot I_{rms} \Rightarrow P = U \cdot I$$

$$\Rightarrow P = \frac{U^2}{R} \Rightarrow P = I^2 \cdot R$$

The active power should always be assumed when  $P$  is given without any other details. The suffix 'act' is usually omitted. The **instantaneous power**  $p$  is required only in exceptional cases. Here, lower case letters are used:

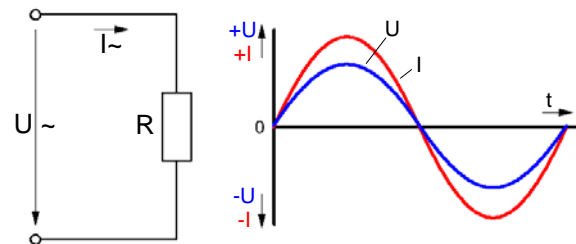


Fig. 11.1.1: Voltage and current, in phase

$$p = u \cdot i \quad (\text{instantaneous values})$$

The active power of sine-wave voltages is calculated from the peak values, as follows:

$$P_{act} = U_{rms} \cdot I_{rms} \Rightarrow P_{act} = \frac{1}{\sqrt{2}} \cdot u_p \cdot \frac{1}{\sqrt{2}} \cdot i_p = \frac{1}{\sqrt{2} \cdot \sqrt{2}} \cdot u_p \cdot i_p = \frac{1}{2} \cdot u_p \cdot i_p$$

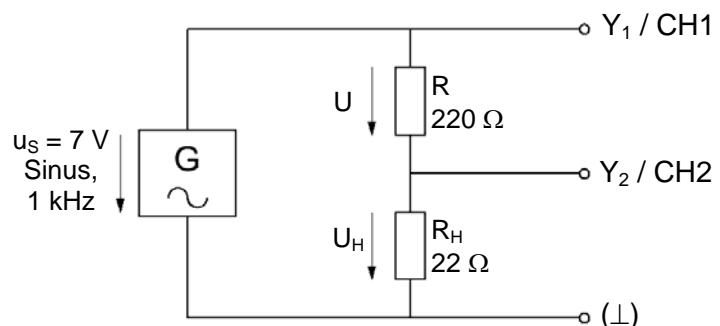
The power converted at an ohmic consumer, in AC techniques, is known as the **active power**, because real energy is released and work performed. In contrast, there is the term 'reactive power' – this will be explained later.

#### 11.2 Active Power of a Sine-wave Voltage in a Practical Exercise

The instantaneous and active values of active power will now be determined by measuring voltage and current on an oscilloscope and drawing the waveforms displayed. An oscilloscope can display only voltages present at its input. Therefore, the current measurement is made, indirectly from the voltage drop across an extra resistor ( $R_H$ ).

The series circuit in Fig. 11.2.1 uses the fact that the same current flows through resistors  $R$  and  $R_H$ . Thus, the voltage drop across  $R_H$  represents the magnitude of current and this can be displayed on the oscilloscope. The voltages  $U+U_H$  and  $U_H$  are connected to channels  $Y_1$  and  $Y_2$ . To allow both single voltages  $U$  and  $U_H$  to be displayed simultaneously, the reference point (Ground), must be connected between the 2 resistors. This is only possible with differential input oscilloscope or multimeter. To display the actual value of  $U$  we should subtract the value  $U_H$  from the value of  $U+U_H$ .

Fig. 11.2.1: Measurement circuit for active power



To display the actual value of  $U$  we should subtract the value  $U_H$  from the value of  $U+U_H$ .

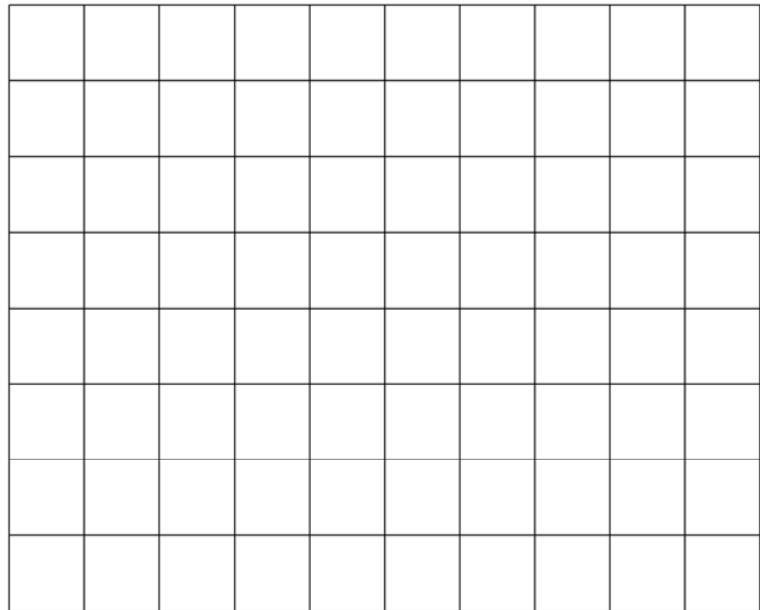
## Practical Experiments

- Assemble the circuit in Fig. 11.2.1 on the Electronic Circuits Board. Connect the outputs of the circuit to the channel inputs of the oscilloscope (assembly and measurement details are in Fig. 11.3.1).
- Set the function generator to sine-wave voltage,  $u_p = 7 \text{ V}$ ,  $f = 1 \text{ kHz}$ .
- Draw the displayed voltage waveforms  $U+U_H$  and  $U_H$  (represents  $I$ ) in the chart (Fig. 11.2.2).

Fig. 11.2.2: Displayed voltage and power waveforms

**Oscilloscope settings:**  
 X : 0,1 ms / div.  
 Y<sub>1</sub> : 2 V / div.  
 Y<sub>2</sub> : 0,5 V / div.

- Measure, on the waveform drawn, the instantaneous values of  $u$  and  $u_H$ . Enter the measured values in table 11.2.3.
- From the measured values, calculate the instantaneous values of current,  $i$  and power,  $p$ . Complete the table with the calculated results.



- Plot the calculated instantaneous values of the power  $p$  in the chart (Fig. 11.2.2.) and draw the power curve (extend the y-axis if necessary).

Time [ms]	$u+u_H$ [V]	$u_H$ [V]	$u$ [V]	$i$ [mA]	$p$ [mW]
0					
0,1					
0,15					
0,25					
0,35					
0,4					
0,5					
0,6					
0,65					
0,75					
0,85					
0,9					
1					

Table 11.2.3.:  
Instantaneous values,  
 $u$ ,  $u_H$ ,  $i$ ,  $p$



## Practical Experiments

- Interpret the shape of the power curve drawn in Fig. 11.2.2.
- How much active power is dissipated at resistor,  $R$ ?
- What is the active power at a resistor of  $R = 330 \Omega$ , when a symmetrical square-wave voltage  $u_{pp} = 10 \text{ V}$  is applied?
- How much power is dissipated in heat by an ohmic resistor  $R = 22 \Omega$ , when a symmetrical delta voltage can be seen on an oscilloscope of  $u_p = 9 \text{ V}$ ?

### 11.3 Assembly and Measurements on the Electronic Circuits Board

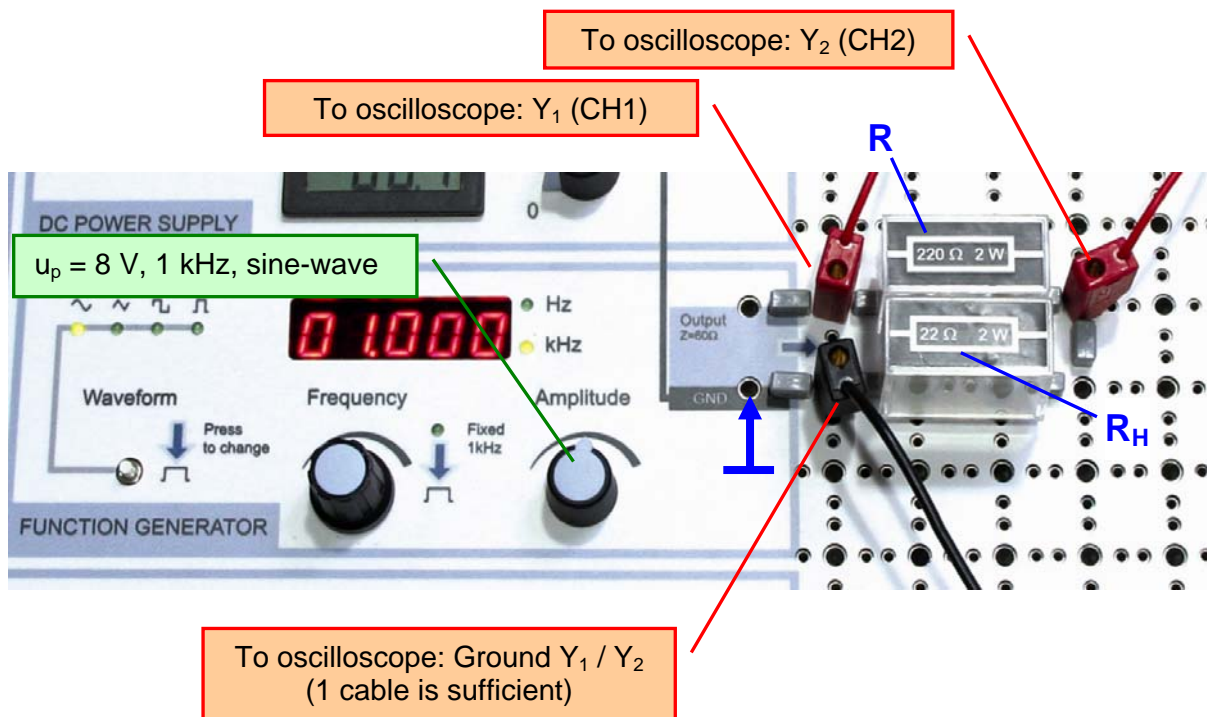


Fig. 11.3.1: Assembly and measurements, Active power, on the Electronic Circuits Board

## 12. Three-phase AC

### 12.1 Origin and Function of Three-phase AC

Electrical energy is usually fed to domestic and industrial consumers by way of a 4-wire network. This 4-wire technique originates from the energy provider (generators in an electrical power station) and a simplified diagram is shown in Fig. 12.1.1 (see also, the diagram on the front panel of the Electronic Circuits Board at the lower left. Three coils (phase windings), offset by  $120^\circ$  form a star circuit. The common connection of the coils is known as the star point and forms the **neutral line N** connection. The three phases, each connected to the other end of the windings, form the **phase lines L1, L2 and L3**. Between each phase line and neutral, there is a sinusoidal AC voltage of  $U_{rms} = 230\text{ V}$ . A sinusoidal AC voltage of  $U_{rms} = 400\text{ V}$  can be measured between any pair of phase lines.

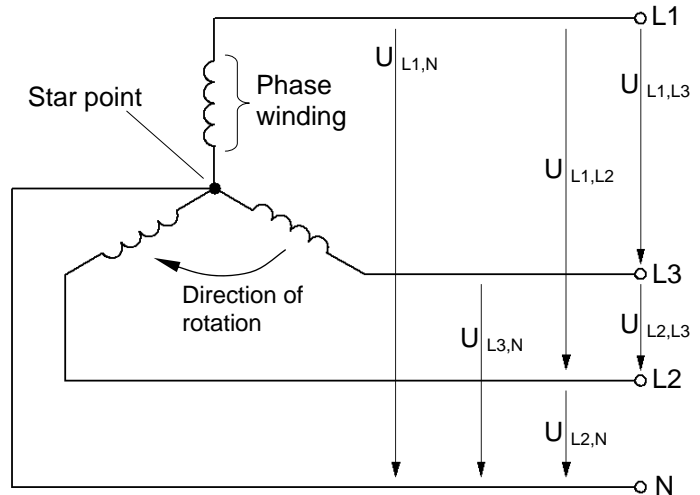


Fig. 12.1.1: Generation of three-phase AC

A three-phase network has 3 **phase voltages** and 3 **line voltages** available (Fig. 12.1.1):

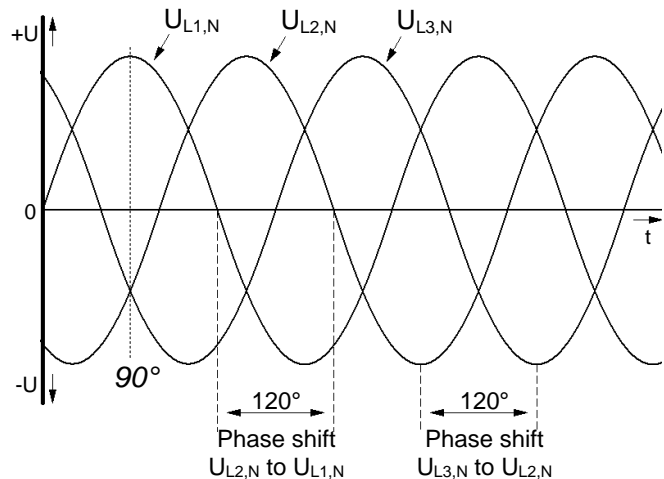
$$\begin{array}{l}
 U_{L1,N} \\
 U_{L2,N} = 230\text{ V (phase voltage)} \\
 U_{L3,N}
 \end{array}
 \quad \left| \quad
 \begin{array}{l}
 U_{L1,L2} \\
 U_{L2,L3} = 400\text{ V (line voltage)} \\
 U_{L1,L3}
 \end{array}$$

The following mathematical relationship exist between the rms values of line and phase voltages:

$$U_L = \sqrt{3} \cdot U_{ph} \quad ; \quad [400\text{V} \approx \sqrt{3} \cdot 230\text{V}]$$

Fig. 12.1.2: Line chart of a three-phase alternating voltage

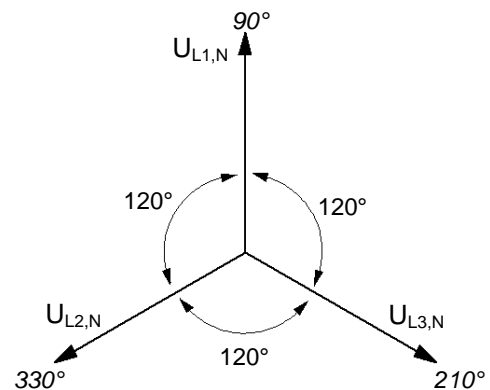
The phase voltages  $U_{L_n,N}$  have a phase shift of  $120^\circ$  (one-third of a period) which corresponds to the offset of the stationary generator coils. Fig. 12.1.2 shows the sinusoidal shape of the voltages whereby  $U_{L1,N}$  starts at the zero axis with a positive half-wave.



## Practical Experiments

The **line chart** (Fig. 12.1.2) is not very often used in practice. A more straightforward representation of the phase shift between the voltages  $U_{L1/2/3,N}$  can be shown using a **vector diagram** (Fig. 12.1.3). The length of each vector corresponds to its maximum amplitude. The vectors rotate at the frequency,  $f$  about the centre point. The phase voltage  $U_{L2,N}$  **lags** the phase voltage  $U_{L1,N}$  by  $120^\circ$ ; in contrast, the phase voltage  $U_{L3,N}$  **leads** by  $120^\circ$ . The instantaneous values of voltage are given by the sine value of the vector angle, multiplied by the length of the vector.

Fig. 12.1.3: Vector diagram of 3-phase AC

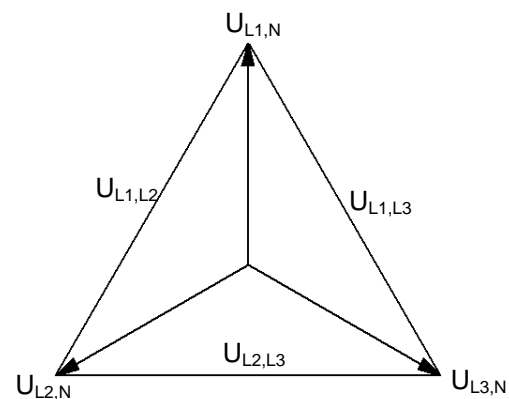


In Fig. 12.1.3,  $U_{L1,N}$  has just reached its maximum amplitude ( $\sin 90^\circ = 1$ ).  $U_{L2,N}$  on the other hand, shows half of the negative maximum voltage ( $\sin 330^\circ = -0,5$ ), at the next fall in amplitude. Also,  $U_{L3,N}$  corresponds to half of the negative maximum voltage ( $\sin 210^\circ = -0,5$ ), but the amplitude is increasing. This 'snapshot' of the phase relationship ( $U_{L1,N} = 90^\circ$ ), for comparison of the 2 methods of representation, is also indicated in Fig. 12.1.2.

Fig. 12.1.4: Line voltages as a vector diagram

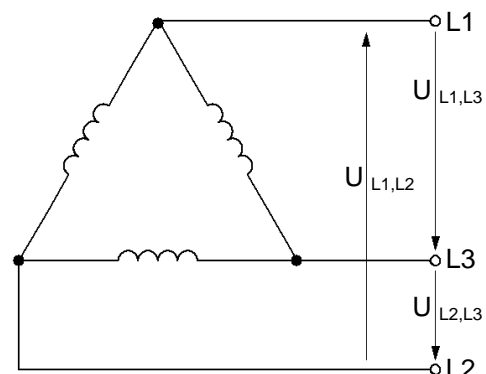
The relationships can also be shown easier, between phase and line voltages, using a vector diagram (Fig. 12.1.4). The lines joining the ends of the phase vectors show the line voltages. Their length is longer than the individual phase vectors, by the so-called 'concatenation' factor (the interlinking factor,  $\sqrt{3}$ ). Thus:

$$U_L = \sqrt{3} \cdot U_{ph}$$



In addition to the basic form 'star', the phase windings in a 3-phase AC network can also be connected in a 'delta' circuit (Fig. 12.1.5). In this case, the line voltages  $U_{Lm,Ln}$  are sometimes referred to as the 'delta voltage'. In a public network they are normally 400 V.

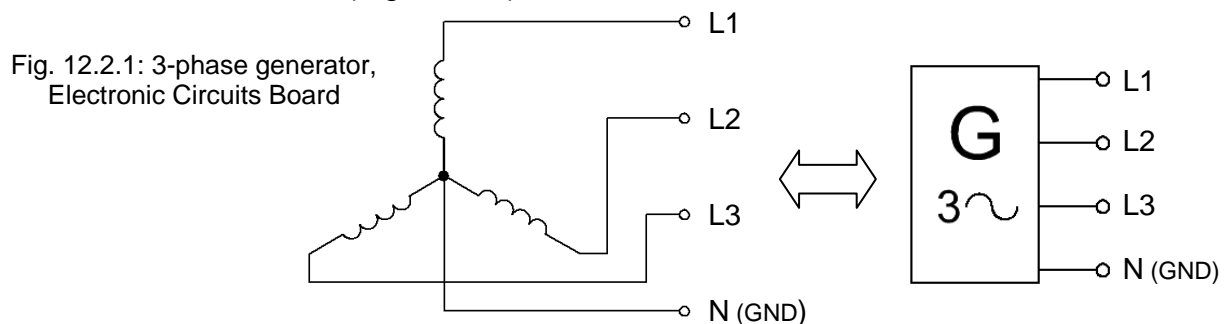
Fig. 12.1.5: Delta circuit



## Practical Experiments

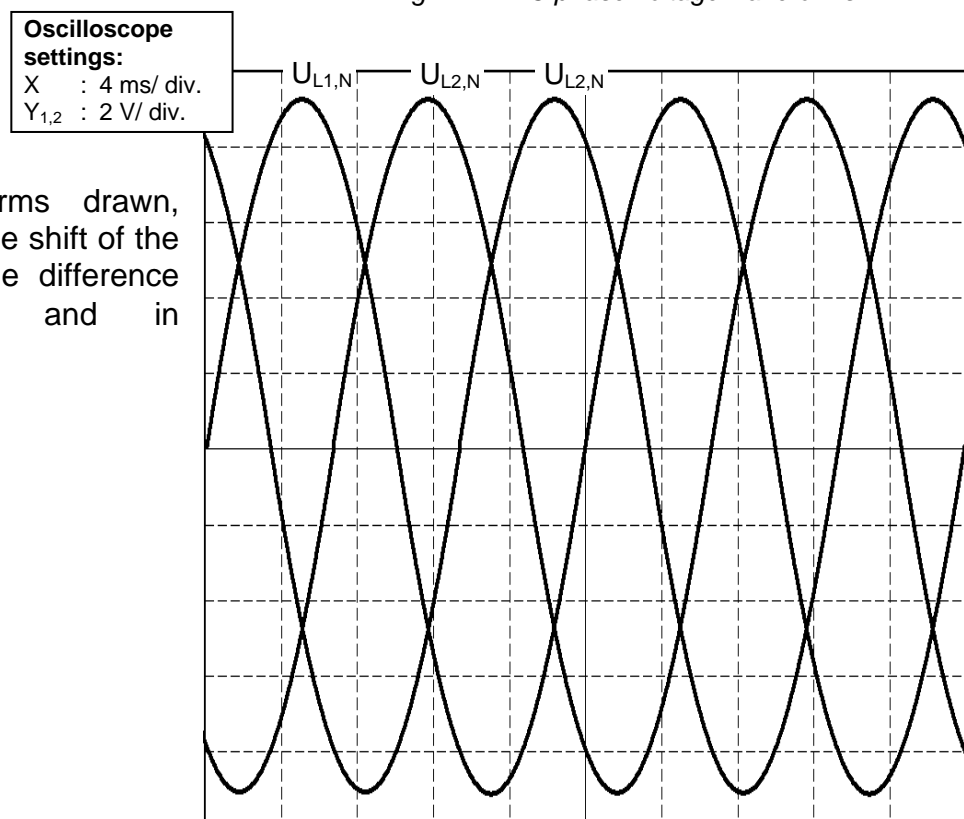
### 12.2 Measurements on a Three-phase System

The relationships between the characteristic quantities of three-phase systems will now be examined by way of various measurements at the three-phase generator on the Electronic Circuits Board (Fig. 12.2.1).



- Display the phase voltages L1 to L3 ( $U_{L1,N}$  to  $U_{L3,N}$ ) of the 3-phase generator on the oscilloscope and draw the voltage waveforms in the chart below (Fig. 12.2.2). Pay attention to the correct phase relationships between the individual voltages. (You will need 2 measurement processes when using a 2-channel oscilloscope).

Fig. 12.2.2: 3-phase voltage waveforms



- On the waveforms drawn, measure the phase shift of the voltages. Give the difference as angle  $\varphi$  and in milliseconds.

- Calculate the frequency,  $f$  of the phase voltages.

## Practical Experiments

- Measure the phase and line voltages with the multimeter.

Phase voltage

$$U_{L1,N} =$$

$$U_{L2,N} =$$

$$U_{L3,N} =$$

Line voltage

$$U_{L1,L2} =$$

$$U_{L2,L3} =$$

$$U_{L1,L3} =$$

- What is the peak value  $u_p$  of the phase voltage  $U_{L1,N}$ ?

- Calculate the peak value  $u_p$  of the line voltage  $U_{L1,L3}$ .

- Calculate the interlinking factor.

### 12.3 Consumers in a Star Circuit

#### 12.3.1 Current and Power Distribution in a Star Circuit

Fig. 12.3.1.1 shows three consumers, connected in a star circuit to the four lines of a 3-phase network. The phase voltages L1 to L3 ( $U_{L1,N}$  to  $U_{L3,N}$ ) cause the **line currents (phase currents)  $I_1$  to  $I_3$**  to flow in the three branches. Their value is calculated from Ohm's law, as shown:

$$I_n = \frac{U_{Ln}}{R_n}$$

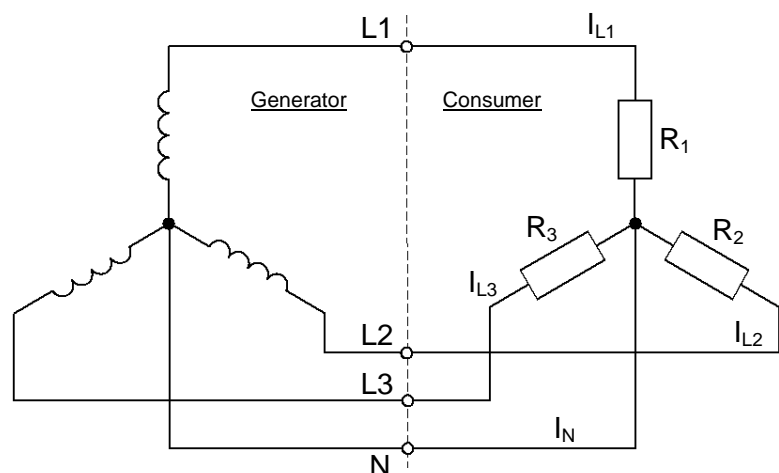


Fig. 12.3.1.1: Consumer in a star circuit

With a **symmetrical** consumer star connection, i.e. when  $R_1 = R_2 = R_3$ , equal line currents flow in the branches. In the line diagram of the phase voltages (see section 12.1, Fig. 12.1.2) it can be seen that the instantaneous sum of the 3 phase voltages is equal to zero. From Ohm's law, this also applies to the resultant currents.

## Practical Experiments

Also, according to Kirchhoff's 1st. law, "The algebraic sum of the currents meeting at a point in a network is zero". For this reason, **in the neutral line N with symmetrical, or balanced loading, there is no flow of current ( $I_N = 0$ )**.

If one of the consumers changes in value, the star circuit then becomes **asymmetric** and a compensating current flows in the neutral line.

The total power  $P_{tot}$  dissipated at the consumers, is given by the sum of the individual powers,  $P_{Rn}$ :

$$P_{tot} = P_{R1} + P_{R2} + P_{R3}$$

The product of phase voltage  $U_{Ln}$  and phase current  $I_{Ln}$  corresponds to the power in the phase,  $P_{Rn}$ :

$$P_{Rn} = U_{Ln} \cdot I_{Ln}$$

For symmetrical loading in a star circuit, the calculation of total power is simplified to:

$$P_{tot} = 3 \cdot P_{ph} = 3 \cdot U_{ph} \cdot I_{ph}$$

### 12.3.2 Measurements on Symmetrical and Asymmetrical Star Circuits

- Load the three-phase generator on the Electronic Circuits Board with 3 resistors connected in a star circuit, as in Fig. 12.3.2.1. First, use 3 resistors of the same value, each 1 k $\Omega$  (assembly details are given in section 12.3.3).
- Measure the phase and line voltages, as well as the current flow in the start circuit. Enter the values measured in table 12.3.2.2.

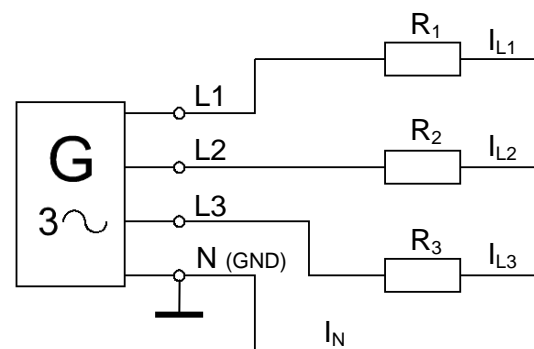


Fig. 12.3.2.1: Measurements on the star circuit

Phase voltage [V]			Line voltage [V]			Line current [mA]				Loading:
$U_{L1,N}$	$U_{L2,N}$	$U_{L3,N}$	$U_{L1,L2}$	$U_{L2,L3}$	$U_{L1,L3}$	$I_{L1}$	$I_{L2}$	$I_{L3}$	$I_N$	
										symmetrical ( $R_1 = R_2 = R_3$ )
										asymmetrical $R_1 = 1 \text{ k}\Omega$ , $R_2 = 470 \Omega$ , $R_3 = 100 \Omega$

Table 12.3.2.2: Voltage and current values measured in the star circuit

- Calculate the phase powers and the total power for the symmetrical star circuit ( $R_1 = R_2 = R_3$ ).



Evaluate the measured values of the neutral line current,  $I_N$ .

- Replace 2 of the resistors in the star circuit:  $R_2 = 470 \Omega$ ,  $R_3 = 100 \Omega$ .
- Repeat the voltage and current measurements on the now, asymmetrical star circuit and enter the values measured in table 12.3.2.2.
- Calculate the phase powers and the total power for the asymmetrical star circuit.

### 12.3.3 Star Circuit Exercise Assembly on the Electronic Circuits Board

The three-phase generator on the Electronic Circuits Board provides the 3 phase voltages  $L_1$ ,  $L_2$ ,  $L_3$ . The LED's at the sockets light to indicate an overload of current (limit value 150 A); normally, the LED's remain switched off (Fig. 12.3.3.1).

Fig. 12.3.3.1 shows the asymmetrical star circuit. The on-going phase voltage  $L_1$  ( $U_{L1,N}$ ) is measured across  $R_1 = 1 \text{ k}\Omega$ . The connection between centre point of the star ('node') and the neutral line  $N$  of the generator is broken and an ammeter is inserted in the circuit to measure the current (Fig. 12.3.3.1).

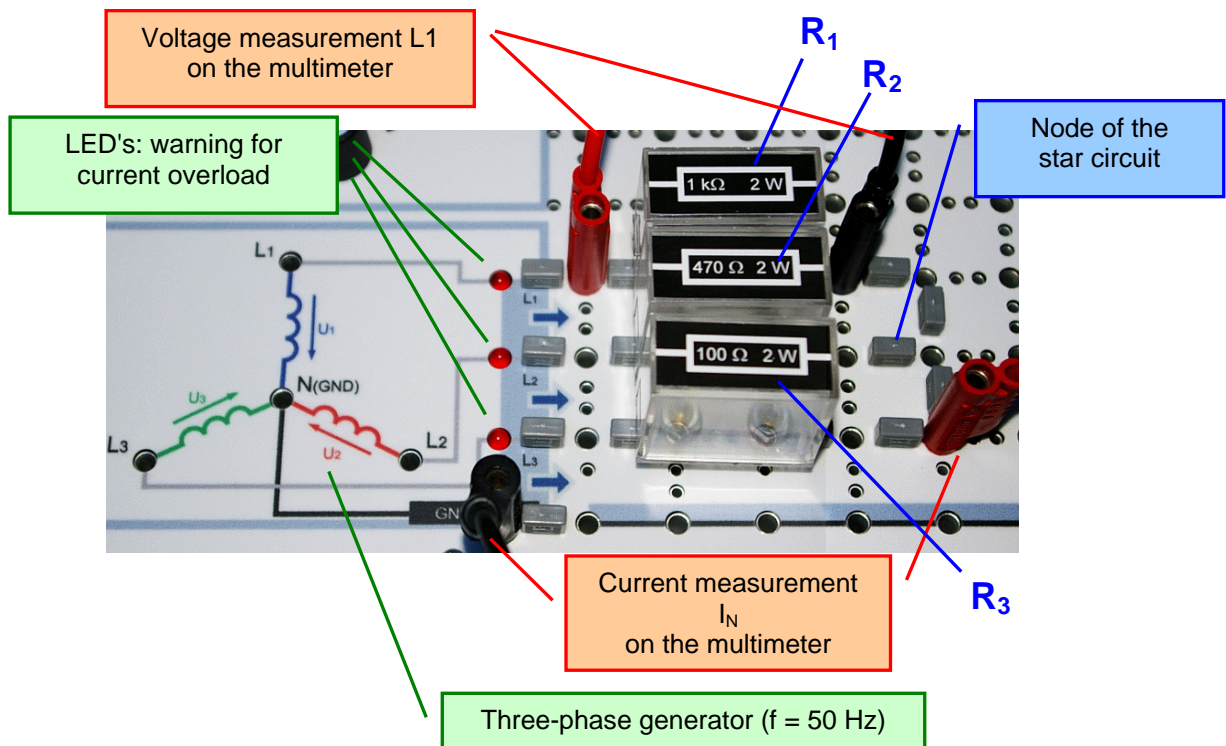


Fig. 12.3.3.1: Measurements at the 3-phase generator on the Electronic Circuits Board

## Practical Experiments

### 12.4 Consumers in a Delta Circuit

#### 12.4.1 Current and Power Distribution in a Delta Circuit

Fig. 12.4.1.1: Consumer in a delta circuit

When 3 consumers are connected in a delta circuit (Fig. 12.4.1.1), the loads are supplied directly from the line voltages. The neutral line is no longer required. Thus, phase voltage (across the consumer) and the line voltage are identical.

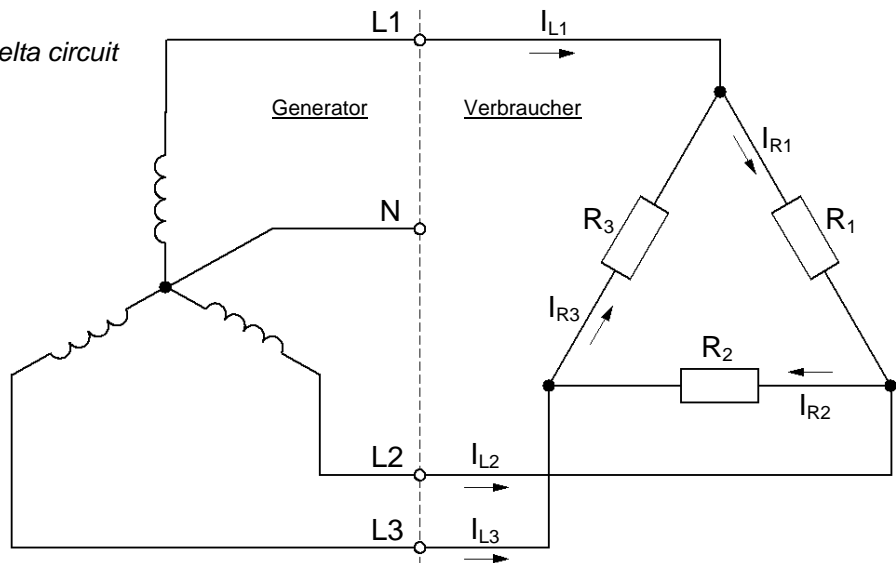
The line currents  $I_{Ln}$

branch at the delta nodes as phase currents  $I_{ph}$  ( $I_{Rn}$ ). With identical line voltages and symmetrical loading :

The total power  $P_{tot}$  in the delta circuit is calculated as the sum of the individual powers dissipated at the consumers (phase power,  $P_{Rn}$ ):

In the case of symmetrical loading and equal line voltages (= phase voltages), the equation for calculating the total power,  $P_{tot}$  simplifies to:

According to the general equation for power, the phase power is:



$$I_{ph} (I_{Rn}) = \frac{I_{Ln}}{\sqrt{3}}$$

$$P_{tot} = P_{R1} + P_{R2} + P_{R3}$$

$$P_{tot} = 3 \cdot P_{ph} = 3 \cdot U_{ph} \cdot I_{ph}$$

$$P_{Rn} = U_{Ln} \cdot I_{Rn}$$

#### 12.4.2 Measurements on Symmetrical and Asymmetrical Delta Circuits

- Load the three-phase generator on the Electronic Circuits Board with 3 resistors connected in a delta circuit, as in Fig. 12.4.2.1. First, use 3 resistors of the same value, each 1 k $\Omega$  (assembly details are given in section 12.4.3).
- Measure the line voltages, phase and line currents. Enter the values measured in table 12.4.2.1.

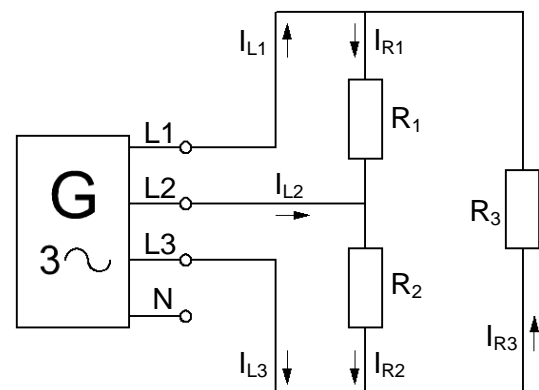


Fig. 12.4.2.1: Measurements on the delta circuit



## Practical Experiments

Line voltage [V]			Line current [mA]			Phase current [mA]			Loading:
$U_{L1,L2}$	$U_{L2,L3}$	$U_{L1,L3}$	$I_{L1}$	$I_{L2}$	$I_{L3}$	$I_{R1}$	$I_{R2}$	$I_{R3}$	
									symmetrical ( $R_1 = R_2 = R_3$ )
									asymmetrical $R_1 = 1\text{ k}\Omega$ , $R_2 = 470\ \Omega$ , $R_3 = 100\ \Omega$

Table 12.4.2.2: Voltage and current values measured in the delta circuit

- Calculate the total and phase powers for the symmetrical delta circuit ( $R_1 = R_2 = R_3$ ).
- Replace 2 of the resistors in the delta circuit:  $R_2 = 470\ \Omega$ ,  $R_3 = 100\ \Omega$ .
- Repeat the voltage and current measurements on the now, asymmetrical delta circuit and enter the values measured in table 12.4.2.2.
- Calculate the total power and phase powers for the asymmetrical delta circuit.

### 12.4.3 Delta Circuit Exercise Assembly on the Electronic Circuits Board

Fig. 12.4.3.1 shows the asymmetrical delta circuit ( $R_1 \neq R_2 \neq R_3$ ). A large area should be used for the assembly to allow easy access for measuring the current. As shown, in the  $R_1 = 1\text{ k}\Omega$  phase, an ammeter is connected in series for measuring the phase current  $I_{R1}$ . A voltmeter measures the line voltage  $U_{L1,L3}$  across  $R_3$  (Fig. 12.4.3.1).

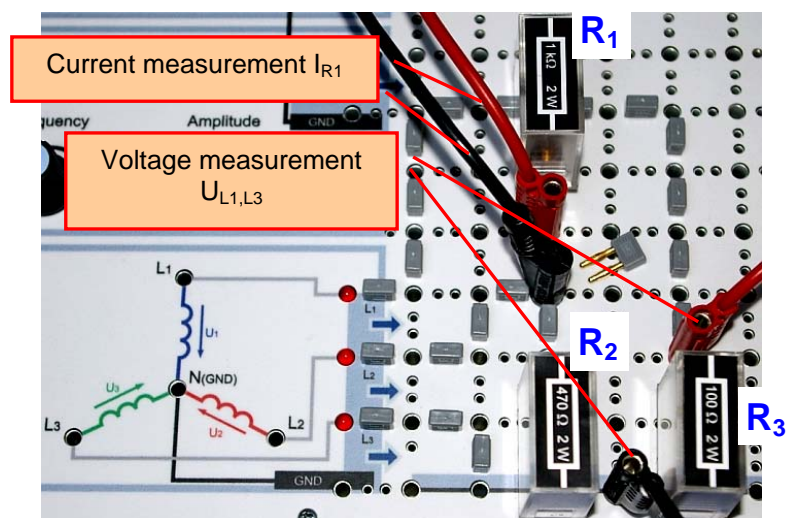


Fig. 12.4.3.1: Recording the measurements in a delta circuit

## Practical Experiments

### 12.5 Faults in Three-phase Circuits

#### 12.5.1 Measurements on Faulty Star Circuits

Considering the exercise assembly of a **symmetrical star circuit** in Fig. 12.5.1.1, there are 3 possible faults with a characteristic effect. Table 12.5.1.2 summarises these faults.

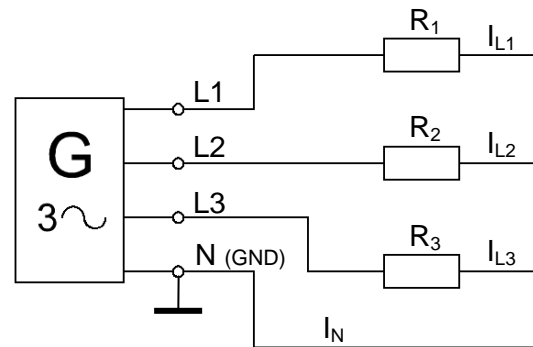
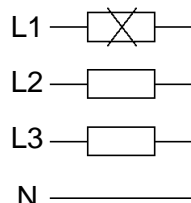
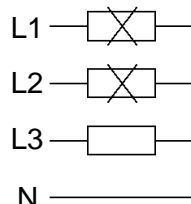
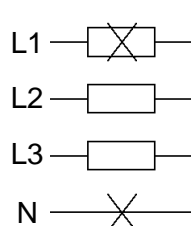


Table 12.5.1.2: Possible faults in a star circuit

Fig. 12.5.1.1: Star circuit

	Fault	Effect	Resulting circuit
1	Break in <b>one</b> line, L1 to L3 <u>or</u> one of the consumers, R <sub>1</sub> to R <sub>3</sub> <u>or</u> a failure of one of these voltages.	Power consumption $P_{\text{tot}}$ falls by <b>one-third</b> (example shown: $I_{L1} = 0$ )	
2	Failure of <b>two</b> circuit branches as described in 1.	No flow of current in two of the 3 lines (example shown: $I_{L1} = 0$ and $I_{L2} = 0$ ). Power consumption $P_{\text{tot}}$ falls by <b>two-thirds</b>	
3	Break in the <b>neutral line N</b> <u>and</u> break in <b>one</b> line as described in 1.	2 consumers in series are fed by <b>one line voltage</b> (example shown: $U_{L2,L3}$ effectively a series circuit of 2R); $P_{\text{tot}}$ falls by <b>half</b> .	

- Measure the voltages and currents as listed in table 12.5.1.3, in the faulty star circuit.

Phase voltage [V]			Line voltage [V]			Line current [mA]				Fault:
$U_{R1}$	$U_{R2}$	$U_{R3}$	$U_{L1,L2}$	$U_{L2,L3}$	$U_{L1,L3}$	$I_{R1}$	$I_{R2}$	$I_{R3}$	$I_N$	
										Break in supply line L2
										Break in L2 and L3
										Break in neutral line and L3

Table 12.5.1.3: Values measured in a faulty star circuit

## Practical Experiments

- Calculate  $P_{\text{tot}}$  for the 3 faulty star circuits and compare the values with the power consumption of the fully functional circuit in 12.3.2.1.

$P_{\text{tot}}$  of the faultless star circuit:

Break in supply line L2:

Break in supply lines L2, L3:

Break in supply line L3 and neutral line:

### 12.5.2 Measurements on Faulty Delta Circuits

If a 3-phase generator is loaded with 3 consumers in a **symmetrical delta circuit** (Fig. 12.5.2.1), then the faults listed in table 12.5.2.2 can occur:

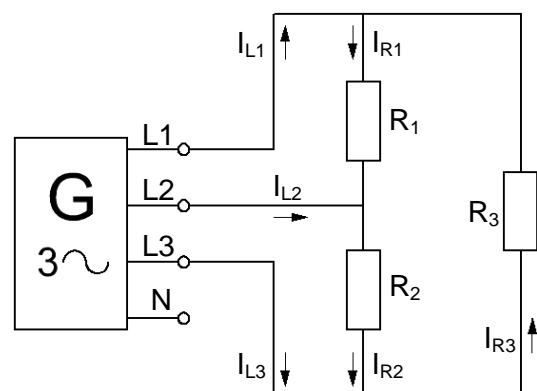


Fig. 12.5.2.1

## Practical Experiments

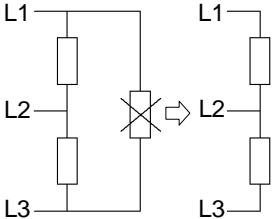
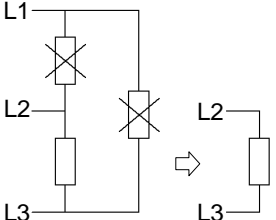
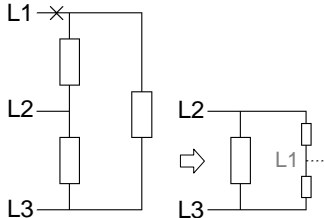
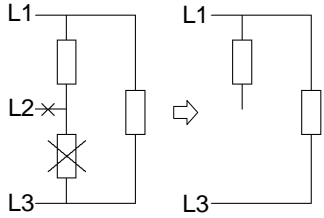
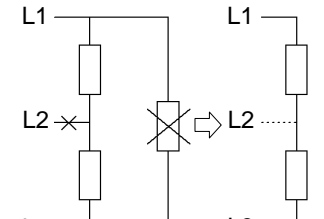
	Fault	Effect	Resulting circuit
1	Break in <b>one</b> phase or one of the consumers $R_1$ to $R_3$	Power consumption $P_{tot}$ falls by <b>one-third</b> (example shown: $I_{R3} = 0$ ) compared to the maximum possible power.	
2	Break in <b>two</b> phases or 2 of the consumers $R_1$ to $R_3$	No flow of current in two of the 3 branches (example shown: $I_{R1} = 0$ and $I_{R3} = 0$ ), Power consumption $P_{tot}$ falls by <b>two-thirds</b>	
3	Break in <b>one</b> supply line <u>or</u> failure in <b>one</b> phase voltage, L1 to L3	The resulting resistor network $R // 2R$ is supplied by <b>one line voltage</b> (example shown: $U_{L2,L3}$ effective at $R_2 // R_1 + R_3$ ; $P_{tot}$ falls by <b>half</b> )	
4	Break / failure of <b>one</b> consumer $R_1$ to $R_3$ <u>and</u> break in <b>one direct</b> supply line L1 to L3 to this phase	The <b>one</b> remaining line voltage supplies the <b>one</b> remaining consumer; Power consumption $P_{tot}$ falls by <b>two-thirds</b> (example shown: line voltage $U_{L1,L3}$ produces $I_{R3}$ )	
5	Break / failure of <b>one</b> consumer $R_1$ to $R_3$ <u>and</u> break in <b>one</b> supply line L1 to L3, that does not <b>directly</b> feed this phase	The <b>one</b> remaining line voltage supplies the <b>series circuit 2R</b> ; $P_{tot}$ falls to <b>one-sixth</b> (example shown: line voltage $U_{L1,L3}$ produces the current in $R' = R_1 + R_2$ )	

Table 12.5.2.2: Possible faults in a delta circuit

## Practical Experiments

Measure the voltages and currents as listed in table 12.5.2.3, in the faulty star circuit.

Phase voltage [V]			Line current [mA]			Phase current [mA]			Fault:
$U_{L1,L2}$	$U_{L2,L3}$	$U_{L1,L3}$	$I_{L1}$	$I_{L2}$	$I_{L3}$	$I_{R1}$	$I_{R2}$	$I_{R3}$	
									Break in phase $R_3$
									Break in phases $R_1$ and $R_3$
									Break in supply line $L1$
									(direct) supply line $L2$ and $R_2$ defect
									(indirect) supply line $L2$ and $R_3$ defect

Table 12.5.2.3: Values measured in a faulty delta circuit

- Calculate  $P_{tot}$  for the 5 faulty delta circuits and compare the values with the power consumption of the fully functional circuit in 12.4.2.1.

$P_{tot}$  of the faultless delta circuit:

$R_3$  defect:

$R_1$  and  $R_3$  defect:

Break in supply line  $L1$ :

## Practical Experiments

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(direct) supply line L2 and R<sub>2</sub> defect:

(indirect) supply line L2 and R<sub>3</sub> defect:

### 13. Capacitor in an AC Circuit

#### 13.1 Construction and Characteristics of Capacitors

In its simplest form, a capacitor consists of 2 parallel, electrically conductive plates (Fig. 13.1.1, left). An air gap between the plates, acts as an insulator. When a constant voltage  $U$  is applied to this capacitor, charge carriers flow between the plates and one plate becomes positively charged, the other negatively charged. As the level of charge increases, an electric field is created between the plates (Fig. 13.1.1, centre). When the voltage across the plates has reached the same as the applied voltage, the flow of current stops.

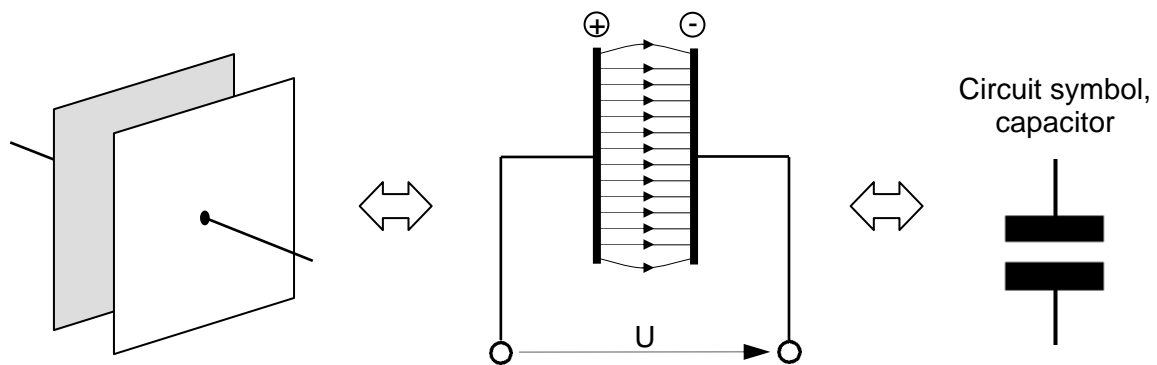


Fig. 13.1.1: Basic construction of a capacitor

The capacitor retains its charge, even when the external voltage is removed. This voltage can be measured at the external connections, on a voltmeter<sup>1</sup>. The amount of the **stored charge Q** depends on the magnitude of the applied **charging voltage U** and the **capacitance C** of the capacitor, i.e.:

$$Q = U \cdot C$$

The **capacitance, C** of the capacitor is determined by its form of construction. The larger the **area of the plates**, the more charge it can store. The smaller the **distance** between the plates, the stronger is the electric field and more charge can be drawn to the plates and stored. Also, the type of insulation between the plates is very significant. This insulation is known as the '**dielectric**'. Some materials support the formation of an electric field between the plates better than others, or than air (free space); these materials have a larger value of dielectric constant  $\epsilon_r$ .

The **capacitance, C** is given by:

$$C = \epsilon_0 \cdot \epsilon_r \cdot \frac{A}{l}$$

- C : Capacitance (Farad)
- $\epsilon_0$  : Absolute permittivity of free space  
( $8,85 \cdot 10^{-12}$  As/Vm)
- $\epsilon_r$  : Relative permittivity of the dielectric  
(dielectric constant)
- A : Area of the plates [ $m^2$ ]
- l : Distance between the plates [m]

<sup>1</sup> This measurement is quite difficult using commercial multimeters, because their internal resistance is too small. When attempting to measure the voltage, the capacitor quickly discharges through the  $R_i$  of the voltmeter.

## Practical Experiments

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When a DC voltage is applied, a charging current flows for only a short time, until the capacitance  $C$  of the capacitor is 'filled' with charge carriers. The insulation between the capacitor plates functions as a *break in the DC circuit*. However, if an AC voltage is applied to the capacitor, then the continuous reversal of the polarity of the external voltage results in a continual charge exchange between the plates. This exchange of charge follows the electric field between the plates, that rhythmically changes in strength and direction. An ammeter in the external circuit would indicate the flow of current due to the charge exchange. *For alternating voltages a capacitor does not present any break in the circuit*. However, the flow of alternating current in a capacitor is different to that through an ohmic resistor. There is no dissipation of power at a capacitor! The flow of alternating current in a capacitor is given the term 'reactive current'.

It is logical then, that the resistance offered by a capacitor to the flow of an AC is given the name **capacitive reactance**,  $X_C$ . The higher the frequency,  $f$  of an applied AC voltage and the larger the capacitance  $C$  of the capacitor, the smaller is the value of  $X_C$ . Equation:

$$X_C = \frac{1}{\omega \cdot C} = \frac{1}{2 \cdot \pi \cdot f \cdot C}$$

As shown, the capacitance of a capacitor increases with a smaller distance between the plates. In industrially manufactured capacitors the thickness of the dielectric is microscopic. From this it follows that high demands are placed in the insulation resistance  $R_p$  of the dielectric so that any residual current, and thus ohmic losses in the capacitor, is kept as small as possible. In practice, the value of  $R_p$  is greater than  $1 \text{ G}\Omega$ .

The thin dielectric also limits the *dielectric strength* of the component. In this respect, a differentiation is made between two characteristic quantities: The **nominal voltage** is the maximum permissible continuous voltage. The **peak voltage** is the maximum permissible short-term transient value of voltage that the capacitor can withstand without causing any damage to the component.

### 13.2 Types and Tasks of Capacitors

In electrical engineering and electronics, capacitors have a wide variety of uses:

- Storing energy
- Storing data
- Frequency-dependent resistance
- Introducing a phase shift between voltage and current
- Isolating DC and AC voltages
- Smoothing rectified AC
- Construction of delay elements
- Construction of oscillating circuits and filters

Depending on their use, capacitors are required with special properties or distinct characteristic quantities. Table 13.2.1 summarises common types of capacitor construction.



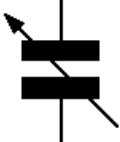
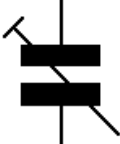
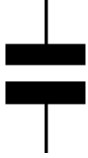
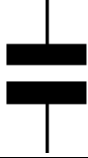

Capacitance	Description	Circuit symbol	Construction	
Variable	Variable capacitor		Capacitance is varied either by: - Plate area - Plate separation or - Dielectric	Precision engineered, intended for frequent, repeated adjustment
	Trimmer			Used seldom or only once, for alignment or tuning processes
Fixed	Ceramic capacitor		Dielectric consists of various ceramic materials (e.g. titanium dioxide, barium titanate) with high dielectric strength and sometimes a higher dielectric constant $\epsilon_r$ (up to 14000)	
	Wound capacitor		Metal and insulating foil (dielectric) are laid out on top of each other and rolled up to give more plate area and thus, a larger capacitance	
	Electrolytic capacitor		The anode (+) is made of metal coated with the insulating dielectric by way of electrolysis. The cathode (-) consists of a paste-like electrolyte. When electrolytic capacitors are used in circuits having a DC component, the correct polarity <b>must</b> be observed. <b>With incorrect connection, there is a danger of explosion!</b>	

Table 13.2.1: Types of capacitors

## Practical Experiments

### 13.3 Charge and Discharge of a Capacitor

#### 13.3.1 Principles of Charge and Discharge Processes

By charging / discharging, a capacitor attempts to reach the same value as the external voltage potential present at its terminals. This external voltage could be the output of a voltage source, the output from a voltage divider, zero volts (in which case, the capacitor discharges), or any other potential. Charge and discharge current always flow via an ohmic resistor<sup>2</sup>, that limits the charge current. In Fig. 13.3.1.1 when  $S_1$  is closed, the capacitor charges via resistor  $R$  ( $U_C = U$ ). When  $S_1$  is opened, the capacitor retains the charge ( $U_C = \text{constant}$ ). When  $S_2$  is closed, the capacitor discharges via resistor  $R$ . The capacitor now functions itself as a voltage source. Therefore, the discharge current ( $I_{\text{dis.}}$ ) flows in the opposite direction (Fig. 13.3.1.1).

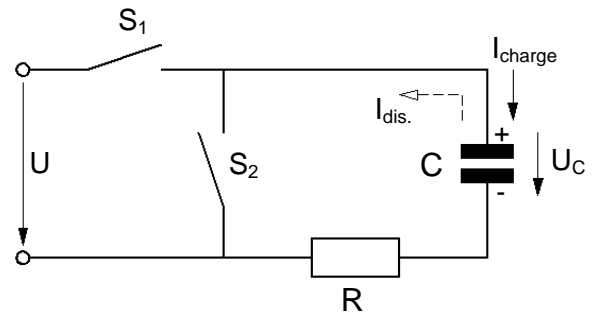


Fig. 13.3.1.1: DC circuit with capacitor  $C$

With a constant charge voltage, the current flow in the circuit and the voltage across the capacitor, follow an **exponential function** (e-function, Fig. 13.3.1.2). The effective **time constant**  $\tau$  of the curve is given by the product of resistance  $R$  in the charge circuit and capacitance  $C$ :

$$\tau = R \cdot C \quad \left| \begin{array}{l} C : \text{Capacitance [F]} \\ R : \text{Resistance [\Omega]} \\ \tau : \text{Time constant [s]} \end{array} \right.$$

At time  $1\tau$  after the start of charging, the voltage at the capacitor ( $U_C$ ) has reached 0,63 of the maximum value (Fig. 13.3.1.2). After 5-times  $\tau$  ( $5\tau$ ), the charging process is considered to be finished. The instantaneous value of capacitor voltage  $u_C$  is calculated by the equation:

$$u_C = U \cdot (1 - e^{-t/\tau}) \quad \left| \begin{array}{l} U : \text{Charge voltage [V]} \\ t : \text{Charging time [s]} \\ e : \text{Euler's constant, 2,718} \end{array} \right.$$

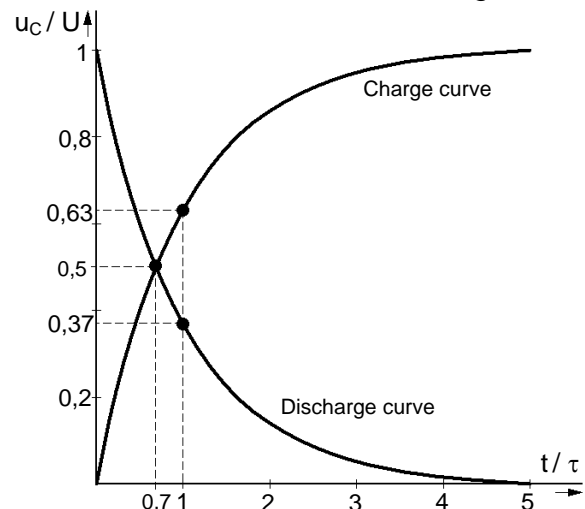


Fig. 13.3.1.2: Charge/discharge curves of a capacitor

The discharge of a capacitor follows the the same e-function (mirrored, Fig. 13.3.1.2). The same time relationships apply as for the charge process: Discharge by 50% after  $0,7\tau$ , by 63% (to  $0,37 \cdot U_C$ ) after  $1\tau$ , process end after  $5\tau$ . The instantaneous value of capacitor voltage  $u_C$  is calculated by the equation:

$$u_C = U \cdot e^{-t/\tau} \quad \left| \begin{array}{l} U : \text{Capacitor voltage [V]} \\ t : \text{Discharging time [s]} \\ e : \text{Euler's constant, 2,718} \end{array} \right.$$

<sup>2</sup> Even with a fast discharge using a short circuit bridge, there is still an effective minimum resistance – the resistance of the wire bridge.

## Practical Experiments

The flow of current in an RC-circuit, also follows an exponential function  $e^{-t/\tau}$  (Fig. 13.3.1.3). The current curves for charge and discharge, are identical. Since the flow of current changes direction during discharge, the equations for the instantaneous values of current differ in their sign, as given below:

$$\begin{array}{l} \text{Charge: } i_C = \frac{U}{R} \cdot e^{-t/\tau} \\ \text{Discharge: } i_C = -\frac{U}{R} \cdot e^{-t/\tau} \end{array} \quad \left| \begin{array}{l} U : \text{ Charge voltage [V]} \\ U : \text{ Capacitor voltage [V]} \end{array} \right.$$

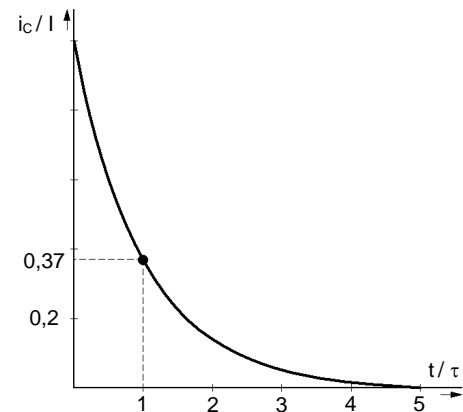


Fig. 13.3.1.3: Charge and discharge current in a capacitor

The charge and discharge response of capacitors is very significant for understanding complex circuits. Here, current, voltage and reactance  $X_C$  should be considered together. At the start of charging the flow of current is maximum, whilst at the same time, the voltage at the capacitor is minimum. Therefore, according to Ohm's law  $X_C$  is initially, very small. The current is limited by resistor  $R$  in the charging path. Towards the end of charging, at almost maximum capacitor voltage  $U_C$  and a small charging current,  $X_C$  has increased to a very high value and attempts to increase to infinity ( $\infty$ ). It can be seen already, that current and voltage are out of phase.

- The charging/discharging response of a capacitor will now be examined in an exercise. Assemble the circuit in Fig. 13.3.1.4 on the Electronic Circuits Board. If possible, use an analog voltmeter to enable the charging and discharging process at the capacitor to be followed from the deflection of the needle.

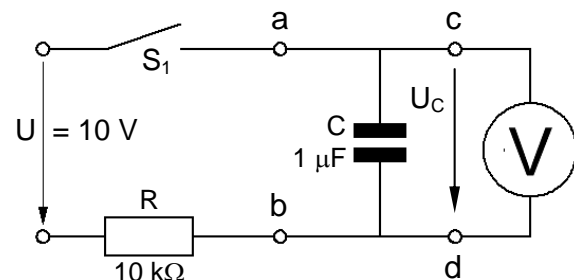


Fig. 13.3.1.4: DC circuit with R and C

- How much time is required by the capacitor  $C = 1 \mu\text{F}$ , to charge up to  $U = 10 \text{ V}$  when switch  $S_1$  is closed?
  
- Now, close the switch and observe the voltage indication. What response do you expect on the voltmeter?



## Practical Experiments

### 13.3.2 Reaction of a Capacitor to Square-wave Voltages

A square-wave voltage with a positive amplitude can be considered as a DC voltage, periodically switched on and off ( $U$  in Fig. 13.3.2.1 right). If the pulse duration and interpulse period are both at least equal to  $5 \cdot \tau$ , then the capacitor  $C$  can fully charge and discharge, via resistor  $R$  (Fig. 13.3.2.1 left). This results in the typical voltage response across the capacitor  $C$ , of a sequence of e-functions ( $U_C$  in Fig. 13.3.2.1 right).

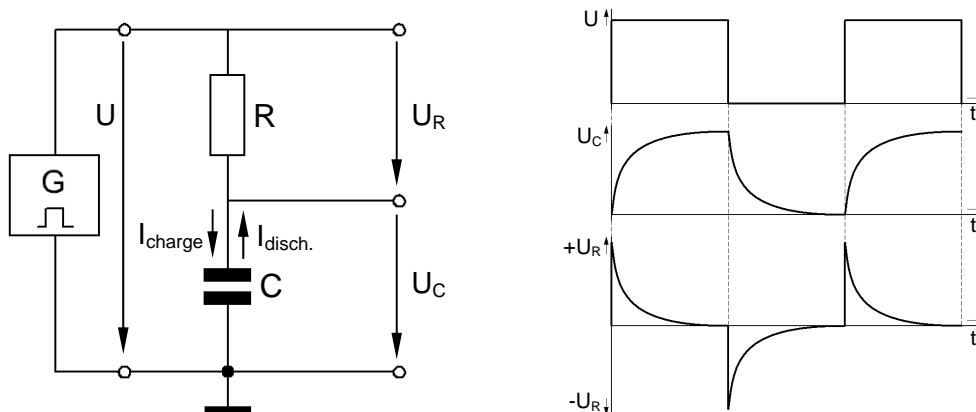


Fig. 13.3.2.1: Reaction of a capacitor to a square-wave voltage

Whilst the capacitor is charging, the voltage difference  $U_R = U - U_C$  is dropped across the ohmic resistance. The reason for  $U_R$  is the initial maximum, then quickly reducing charging current  $I_{\text{charge}}$ . For the time of charging, a typical needle pulse (e-function) across  $R$ , can be displayed on an oscilloscope. The shorter the time constant  $\tau = R \cdot C$ , the narrower is the needle pulse.

During the interpulse period, the capacitor  $C$  functions as a voltage source, discharging via  $R$  with a current flow in the opposite direction ( $I_{\text{dis.}}$ ). The discharge occurs with the same time constant  $\tau$ , so that the second needle pulse produced has the same shape as the first pulse. Due to the current reversal, this needle pulse is negative.

The needle pulses produce heat losses at resistor  $R$ . Here, actual ohmic power is dissipated, so-called 'active power'. In contrast, at the capacitor there is only reactive power that does not produce any warming effects.

The response of a capacitor will now be examined using the components shown, together with the input voltage given in Fig. 13.3.2.2.

- Assemble the circuit in Fig. 13.3.2.2 on the Electronic Circuits Board.
- Set the square-wave generator to a peak voltage of  $U_p = 4 \text{ V}$  at a frequency of  $f = 500 \text{ Hz}$ .

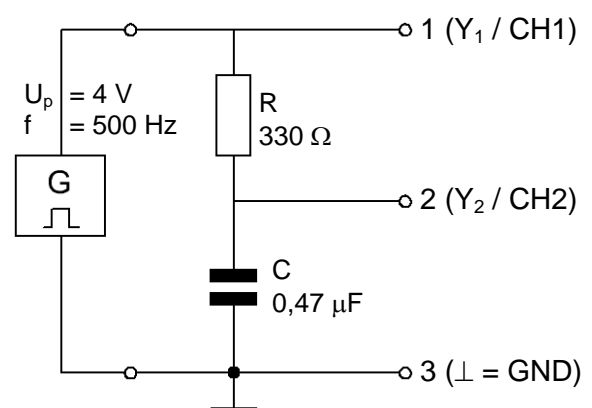


Fig. 13.3.2.2: Square-wave voltage in an RC-circuit

## Practical Experiments

- Connect the oscilloscope as shown. Select the settings on the oscilloscope so that both signals are displayed (one below the other) and a timebase to display at least one complete signal period.
- Draw the signals displayed  $U$  and  $U_C$  in the chart in Fig. 13.3.2.3.

Fig. 13.3.2.3: Display,  $U$  and  $U_C$

<p><b>Oscilloscope settings:</b>  <math>X</math> : 0,2 ms/ div.  <math>Y_1</math> : 2 V/ div., DC  <math>Y_2</math> : 2 V/ div., DC</p>
---

- Change the connections of the oscilloscope in Fig. 13.3.2.2, to display the signal across resistor  $R$ .
- Draw the signals displayed  $U$  and  $U_R$  in the chart in Fig. 13.3.2.4.

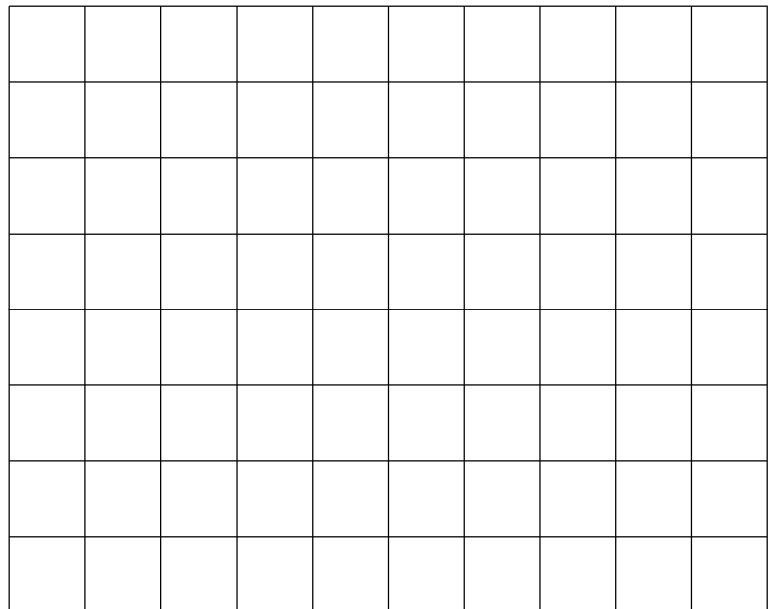
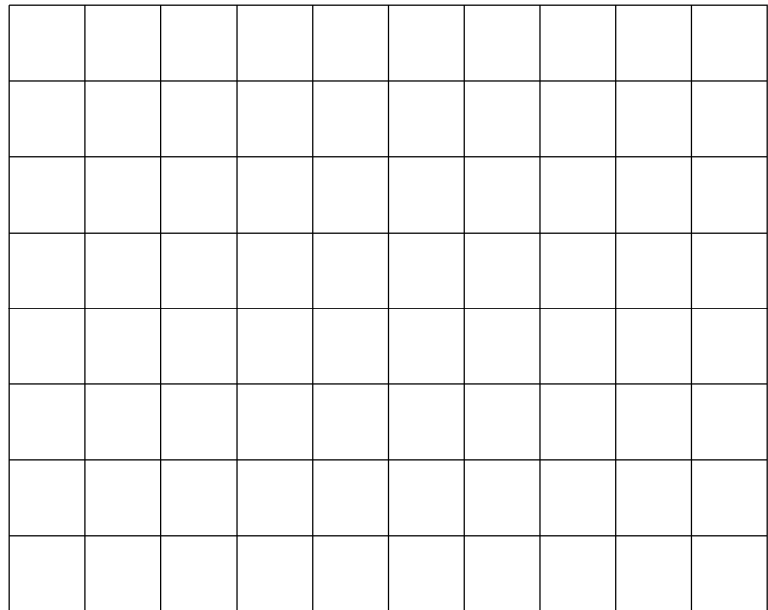
<p><b>Oscilloscope settings:</b>  <math>X</math> : 0,2 ms/ div.  <math>Y_1</math> : 2 V/ div., DC  <math>Y_2</math> : 2 V/ div., DC</p>
---

Fig. 13.3.2.4: Display,  $U$  and  $U_R$

- From the waveforms drawn, determine the time constant  $\tau$  as accurately as possible. Check your result by calculation.

$\tau$  From waveforms:

$\tau$  By calculation:



## Practical Experiments

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- What is the voltage at the capacitor ( $u_C$ ) 0,4 ms after the start of charging? Measure the value from the waveforms or on the oscilloscope screen. Check your measurement by calculation.

$u_C$  Measured after 0,4 ms :

$u_C$  Calculated:

- What current is flowing 0,2 ms after the capacitor starts discharging? Determine the current from the waveforms drawn in Fig. 13.3.2.4 or directly from the oscilloscope screen. Check your measurements by calculation.

$i_{dis}$ . After 0,2 ms:

$i_{dis}$ . Calculated:

- At what time does the capacitor store its maximum charge and how large is this maximum charge?

- In the circuit of Fig. 13.3.2.2 the capacitor C is replaced with one of  $C = 1 \mu\text{F}$ . What effect has this change in the circuit?

- Check your statement by measurement. Display the voltage across the capacitor  $C = 1 \mu\text{F}$  (R unchanged).

## Practical Experiments

### 13.4 Capacitor with a Sine-wave Voltage

#### 13.4.1 Phase Shift between Current and Voltage

It has already been seen that with a square-wave voltage applied to a capacitor, current and voltage at the capacitor, are out of phase. The current immediately reaches a fairly high value, whilst in comparison, the voltage gradually increases as the capacitor is charged. In other words, the current leads the voltage.

With a sine-wave voltage applied, the capacitor charges in rhythm with the periodic time  $T$  from a positive to a negative peak value ( $U_C$  in Fig. 13.4.1.1). The current leads this process by a quarter-period ( $I_C$  in Fig. 13.4.1.1). The current is at a maximum when the voltage has just cut the zero axis. The phase shift between current and voltage is  $90^\circ$ .

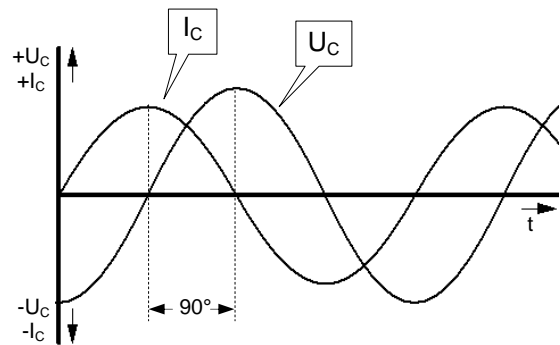


Fig. 13.4.1.1: Phase shift between current and voltage at a capacitor

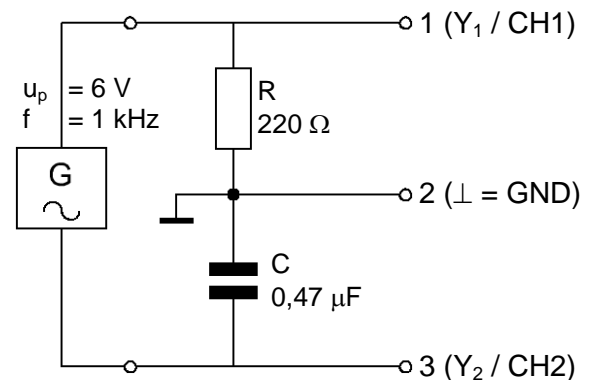
The phase shift between current and voltage will now be proved in a circuit as shown in Fig. 13.4.1.2.

- Assemble the circuit in Fig. 13.4.1.2 on the Electronic Circuits Board.

Fig. 13.4.1.2: Exercise circuit to show the phase shift between  $I$  and  $U$

Since the changes of current and voltage at an ohmic resistor are always proportional to each other,  $U_R$  ( $Y_1 / CH1$ ) can be used for showing the phase of the current  $I_C$  in the circuit.

- Set the signal generator to a sine-wave voltage  $u_{pp} = 12 \text{ V}$  at a frequency of  $f = 1 \text{ kHz}$ .
- Connect the 2-channel oscilloscope as shown in Fig. 13.4.1.2.



By adjusting the 0-axis (GND) between  $R$  and  $C$ , the voltages  $U_R$  and  $U_C$  can both be displayed on the 2-channel oscilloscope. However, the negative voltage  $U_C$  ( $Y_2 / CH2$ ) has a  $180^\circ$  phase shift. For measuring the correct phase relationship, one channel of the oscilloscope must be operated in the 'inverted' mode.

- Display the voltage waveforms  $U_R$  and  $U_C$  on the oscilloscope. Adjust the oscilloscope for a display of at least 2 periods of the sine-wave.
- Draw the signal waveforms displayed in the chart, Fig. 13.4.1.3.



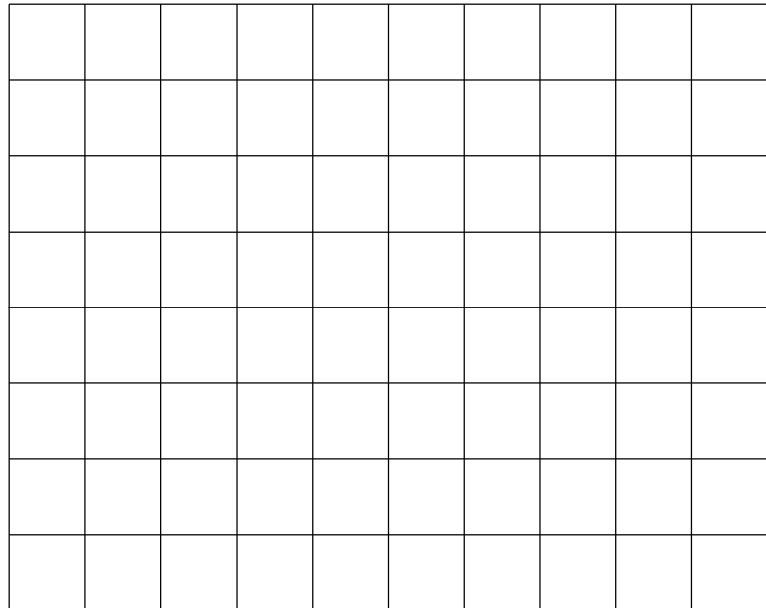
## Practical Experiments

**Oscilloscope settings:**

X : 0,1 ms/ div.  
 Y<sub>1</sub> : 1 V/ div., AC  
 Y<sub>2</sub> : 2 V/ div., AC, inverted

Fig. 13.4.1.3: Phase relationship between current voltage at the capacitor

- From the signal waveforms, measure the periodic time T, the frequency f and the angle of phase shift φ between current and voltage.



### 13.4.2 Capacitive Reactance, X<sub>C</sub>

When an sine-wave voltage is applied to a capacitor, the capacitor is continually charged and discharged. This corresponds to a periodic build-up and decay then a build-up with the opposite polarity, of the electric field between the plates of the capacitor. The current flowing at this time, leads the voltage by 90° and determines the physical properties of the capacitor as a resistance, that limits the flow of current. Since at this resistor, there is no thermal power dissipated, it is known as '**capacitive reactance, X<sub>C</sub>**'.

The magnitude of the capacitive reactance X<sub>C</sub> is inversely proportional to the capacitance C of the capacitor and the frequency f of the applied sine-wave voltage.  
 Equation:

$$X_C = \frac{1}{2 \cdot \pi \cdot f \cdot C} \quad \left| \begin{array}{l} C : [F] \\ f : [1/s] \\ X_C : [\Omega] \end{array} \right.$$

With a given capacitor current I<sub>C</sub> and a known capacitor voltage U<sub>C</sub>, Ohm's law can be used for calculation.  
 Equation:

$$X_C = \frac{U_C}{I_C} \quad \left| \begin{array}{l} U_C : [V] \\ I_C : [A] \\ X_C : [\Omega] \end{array} \right.$$

The response of the capacitive reactance X<sub>C</sub> will now be examined using the circuit shown in Fig. 13.4.2.1. The current flowing in the capacitor can be calculated from the voltage drop U<sub>R</sub> across the resistor R = 1 kΩ (U<sub>R</sub> and I<sub>C</sub> in phase).

## Practical Experiments

By adjusting the 0-axis (GND) between R and C, the voltages  $U_R$  and  $U_C$  can both be displayed on the 2-channel oscilloscope.

- Assemble the circuit in Fig. 13.4.2.1 on the Electronic Circuits Board.
- Set the signal generator to a sine-wave voltage  $u_{pp} = 12\text{ V}$  at an initial frequency of  $f = 1\text{ kHz}$ .
- Connect the 2-channel oscilloscope as shown in Fig. 13.4.2.1.
- Measure the peak-to-peak values of the voltages  $U_C$  and  $U_R$  for the 3 capacitors listed in table 13.4.2.2, at the given frequencies. Enter the measured values in table 13.4.2.2.

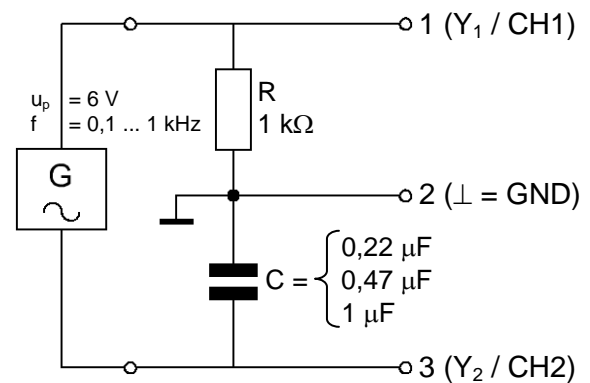


Fig. 13.4.2.1: Exercise circuit to examine the relationship between  $X_C$ ,  $f$  and  $C$

Table 13.4.2.2: Capacitive reactance  $X_C$  for different capacitors at various frequencies

f [kHz]		0,1	0,2	0,3	0,4	0,6	1
$U_C$ [V <sub>pp</sub> ]	0,22 μF						
	0,47 μF						
	1 μF						
$U_R$ [V <sub>pp</sub> ]	0,22 μF						
	0,47 μF						
	1 μF						
$I_C$ [mA <sub>pp</sub> ]	0,22 μF						
	0,47 μF						
	1 μF						
$X_C$ [kΩ]	0,22 μF						
	0,47 μF						
	1 μF						

- Calculate the peak-to-peak currents  $I_C$  and enter the values in table 13.4.2.2.
- Calculate the values of  $X_C$  and enter the values in table 13.4.2.2.
- Plot the calculated values of capacitive reactance  $X_C$  in the chart (Fig. 13.4.2.3). Join the points plotted and draw the characteristics  $X_{Cn} = f(f)$  for the 3 capacitors.


Fig. 13.4.2.3:  
Characteristics  $X_C = f(f)$

- Check the values measured for  $X_C = f$  (100Hz) for the capacitor  $C = 0,47 \mu\text{F}$  by calculation.
  
- How do you explain the deviation between measured and calculated values for  $X_C = f(100 \text{ Hz} ; 0,47 \mu\text{F})$ ?
  
- What tendency is shown by the capacitive reactance  $X_C$  of a capacitor  $C = 0,01 \mu\text{F}$  (= 10 nF) at very high (> 1 MHz) and very low (< 100 Hz) frequencies?
  
- What value must a capacitor have, to present a capacitive reactance of  $X_C = 50 \Omega$  at a frequency of  $f = 14,5 \text{ kHz}$ ? Check your calculated result by measurements, using the circuit in Fig. 13.4.2.1.

## Practical Experiments

### 13.4.3 Active and Reactive Power at a Capacitor

In an *ideal capacitor*, there is no **active power** in the form of dissipated heat. But, there is a flow of energy between the capacitor plates in the form of charge carriers that the capacitor stores as a voltage which can be measured, or as an electric field between the plates (Fig. 13.1.1). With a later discharge or a reversal of charge, this energy in the capacitor, is again available. The electric field decays and drives the discharge current. Thus, current and voltage at a capacitor, produce only a **reactive power**.

In real capacitors however, there are *ohmic losses* that must be taken into account. On the one hand, there is the frequency-dependent **leakage current** through the dielectric, which like all insulators, does not have an infinitely large resistance. Leakage currents are responsible for a slow discharge of the energy stored in the capacitor. In practice, these losses are more significant in electrolytic capacitors that have a measurable insulation resistance due to their form of construction. This is more apparent on old electrolytic capacitors, where the leakage current is higher. In applications where a capacitor is used for storing information, the very minute leakage currents must also be taken into account, because they limit the length of time that the data can be stored. For all other circuits, the second form of ohmic loss, the frequency-dependent **displacement current**, is significant. The dielectric supports the build-up of the electric field and in this way, increases the capacitance of the capacitor (see section 13.1). This is achieved whereby the polarity of the molecules in the dielectric material is reversed in time with the frequency. The higher the frequency, the more often are the polarity changes in the dielectric and the higher the flow of displacement current, and the greater is the power consumed by the electric field. Thus, at high frequencies, the warming of a capacitor can be physically felt.

The active power losses are combined and represented by the **power loss resistance  $R_p$**  imagined to be connected in parallel to the capacitor (Fig. 13.4.3.1), through which the sum of all leakage currents flow  $I_{Rp}$ . Since the capacitor current  $I_C$  leads the leakage current  $I_{Rp}$  by  $90^\circ$ , the relevant vectors show a loss angle,  $\delta$  (Fig. 13.4.3.1).

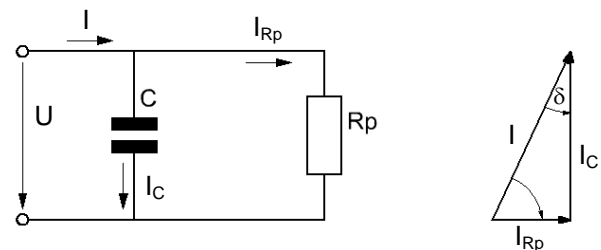


Fig. 13.4.3.1: Losses at a capacitor

The active power losses give the **loss factor  $d$** , that should be as small as possible ( $< 1$ ):

$$d = \tan \delta = \frac{I_{Rp}}{I_C} = \frac{X_C}{R_p}$$

$d$  : Loss factor, [no dimensions]

$\delta$  : Loss angle [  $^\circ$  ]

$I_{Rp}$  : Leakage current [A]

$I_C$  : Reactive current [A]

$X_C$  : Reactance [ $\Omega$ ]

$R_p$  : Loss resistance [ $\Omega$ ]

The active power consumed by a capacitor is the result of unwanted but unavoidable losses. They must be accepted within reason, due to the physical limits in the manufacture of capacitors.

## Practical Experiments

The **reactive power  $Q$**  at a capacitor is given by the reactive current and the capacitor voltage. It can be represented as a multiplication of the instantaneous values of  $i_C$  and  $u_C$  in a line chart, with the phase relationships (Fig. 13.4.3.2).

The reactive power  $Q$  is calculated from:

$$Q_C = U_C \cdot I_C \quad \text{or}$$

$$Q_C = \frac{U_C^2}{X_C} \quad \text{or}$$

$$Q_C = I_C^2 \cdot X_C$$

$Q_C$ : Reactive power, [W]

$U_C$ : [V]

$I_C$ : [A]

$X_C$ : [ $\Omega$ ]

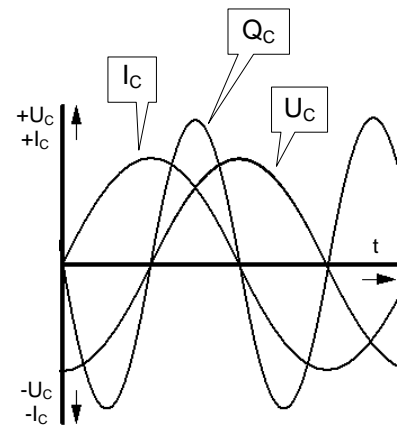


Fig. 13.4.3.2: Reactive power

In an example circuit, the response of current and voltage will be displayed on an oscilloscope, for one complete period of a sinusoidal voltage. The waveforms displayed will then be drawn in a chart. Finally, the waveform of the reactive power curve will be plotted from the values measured and the curve drawn in the chart.

Assemble the circuit in Fig. 13.4.3.3 on the Electronic Circuits Board.

The current  $I_C$  is determined from the voltage  $U_R$  measured on  $Y_1 / CH1$  of the oscilloscope. For measuring the correct phase relationship, one channel of the oscilloscope must be operated in the 'inverted' mode.

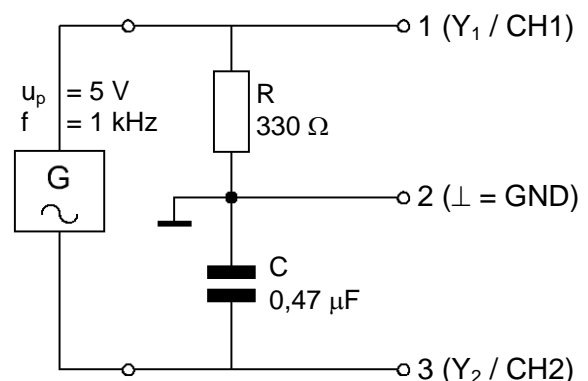


Fig. 13.4.3.3: Exercise circuit for measuring the capacitive reactance,  $Q_C$

- Set the signal generator to a sine-wave voltage  $u_{pp} = 10 \text{ V}$  at a frequency of  $f = 1 \text{ kHz}$ .
- Connect the 2-channel oscilloscope as shown in Fig. 13.4.3.3.
- Display the voltage waveforms  $U_R$  and  $U_C$  on the oscilloscope.
- Measure the instantaneous values of the voltages  $u_R$  and  $u_C$  at the times given in table 13.4.3.4. Enter the values in the table.
- Calculate the instantaneous values of capacitor current  $i_C$  from  $u_R$  and enter the values in the table.
- Calculate the reactive power  $q_C$  from  $u_C$  and  $i_C$ , at the times given in table. Complete the table with your results of calculation.

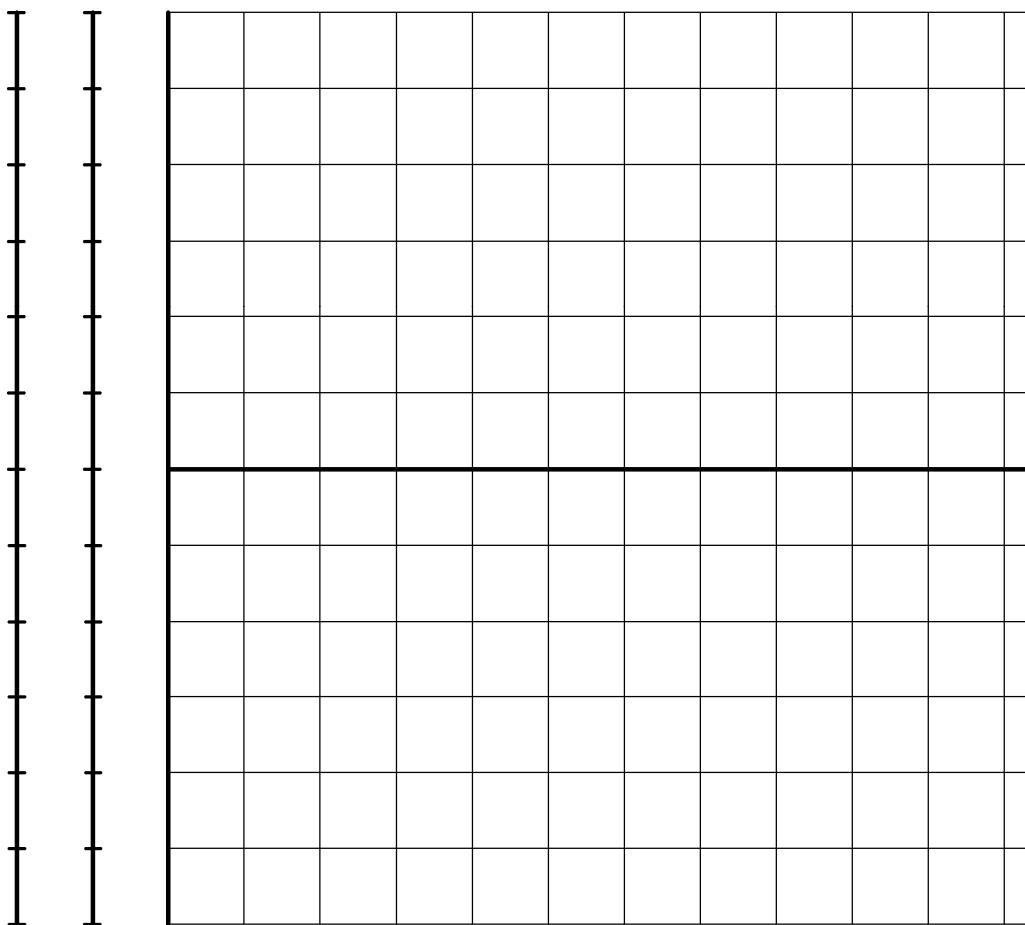
## Practical Experiments

Table 13.4.3.4: Instantaneous values, exercise circuit in Fig. 13.4.3.3

t [ms]	0	0,1	0,2	0,25	0,4	0,5	0,6	0,75	0,8	0,9	1
$u_R$ [V]											
$u_C$ [V]											
$i_C$ [mA]											
$q_C$ [mW]											

- Sketch the current curve  $I_C = f(t)$ , the voltage curve  $U_C = f(t)$  and the power curve  $Q_C = f(t)$ , as accurately as possible, in the chart given in Fig. 13.4.3.5).

Fig. 13.4.3.5: Voltage  $U_C$ , reactive current  $I_C$  and reactive power  $Q_C$  waveforms at the capacitor



## Practical Experiments

### 13.5 Capacitors Connected in Series

#### 13.5.1 Response of Capacitors Connected in Series

In a **series connection** of capacitors, the *plate separation*  $l$  (Fig. 13.5.1.1) is effectively increased. The total capacitance is therefore, less than the smallest single capacitor (Fig. 13.5.1.2). Equation:

$$C_{tot} = \frac{1}{\frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3} + \dots + \frac{1}{C_n}}$$

With only 2 capacitors connected in series, the equation simplifies to:

$$C_{tot} = \frac{C_1 \cdot C_2}{C_1 + C_2}$$

The same current flows through all capacitors and the individual voltages across the capacitors, add to give the total voltage  $U$ . In some applications, this is referred to as a **capacitive voltage divider** (Fig. 13.5.1.2).

$$U = U_{tot} = U_{C1} + U_{C2} + U_{C3} + \dots + U_{Cn}$$

Similarly, at a given frequency  $f$ , the total reactance  $X_{Ctot}$  is given by:

$$X_{Ctot} = X_{C1} + X_{C2} + X_{C3} + \dots + X_{Cn}$$

#### 13.5.2 Practical Proof of the Capacitor Response in a Series Circuit

The statement, 'the total capacitance of a series circuit is always less than the smallest single capacitor', will now be proved by voltage and indirect current measurements on a multimeter.

- Assemble the circuit in Fig. 13.5.2.1 on the Electronic Circuits Board.
- Set the function generator to  $U_{rms} = 4\text{ V}$ ,  $f_{Sine} = 1\text{ kHz}$ .
- Measure the values listed in table 13.5.2.2 with a voltmeter and enter the values in the table.

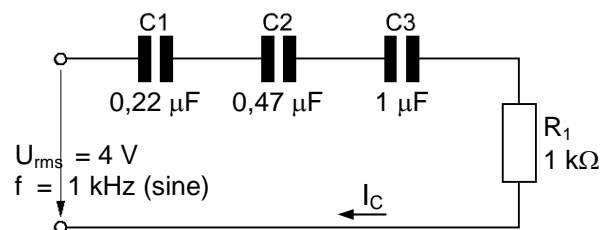


Fig. 13.5.2.1: Measurements on a series circuit of capacitors

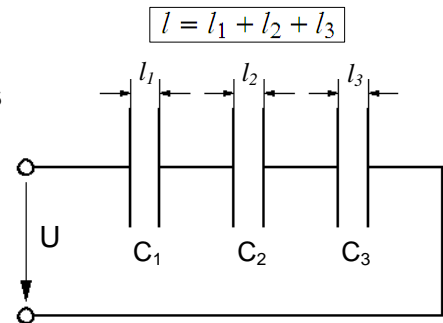
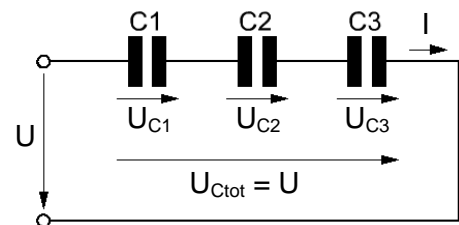


Fig. 13.5.1.1: Series connection of capacitors

Fig. 13.5.1.2: Series connection of capacitors



## Practical Experiments

Table 13.5.2.2: Measurements on a series circuit of capacitors

All voltages in [V]					
$U_{rms}$	$U_{C1}$	$U_{C2}$	$U_{C3}$	$U_{Ctot}$	$U_{R1}$

- From the measured values and using Ohm's law, calculate first the capacitor current  $I_C$ , and then the reactances  $X_{Cn}$  and  $X_{Ctot}$ .

- Calculate the individual capacitances  $C_n$  and the total capacitance  $C_{tot}$ . Use the calculated values of reactance.

- Check the flow of alternating current  $I_C$  on an ammeter. Compare the measured and calculated values.

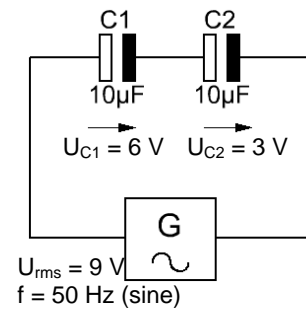
- Calculate  $C_{tot}$  as a check, using the nominal values of the 3 capacitors.



## Practical Experiments

In the circuit of Fig. 13.5.2.3, a fault has occurred in the voltage distribution between the capacitors. What could have been the cause?

Fig. 13.5.2.3: Series circuit, 2 equal value electrolytic capacitors



- What is the value of  $C_{tot}$  in a faulty circuit as in Fig. 13.5.2.3?

### 13.5.3 Exercise Assembly of a Capacitor Series Circuit on the Electronic Circuits Board

An output voltage is set on the function generator of the Electronic Circuits Board of  $U_{rms} = 4\text{ V}$  at a frequency of  $f = 1\text{ kHz}$  (Fig. 13.5.3.1). The voltage divider of  $R_1$  and capacitors  $C_1$ ,  $C_2$ ,  $C_3$  is arranged so that the voltmeter can measure each individual voltage, without any hinderance. The voltage  $U_{Ctot} = 3,07\text{ V}$  is measured across the 3 capacitors (Fig. 13.5.3.1). For a check measurement of the current, the ammeter can be inserted in the circuit in place of one of the bridges to the generator connections.

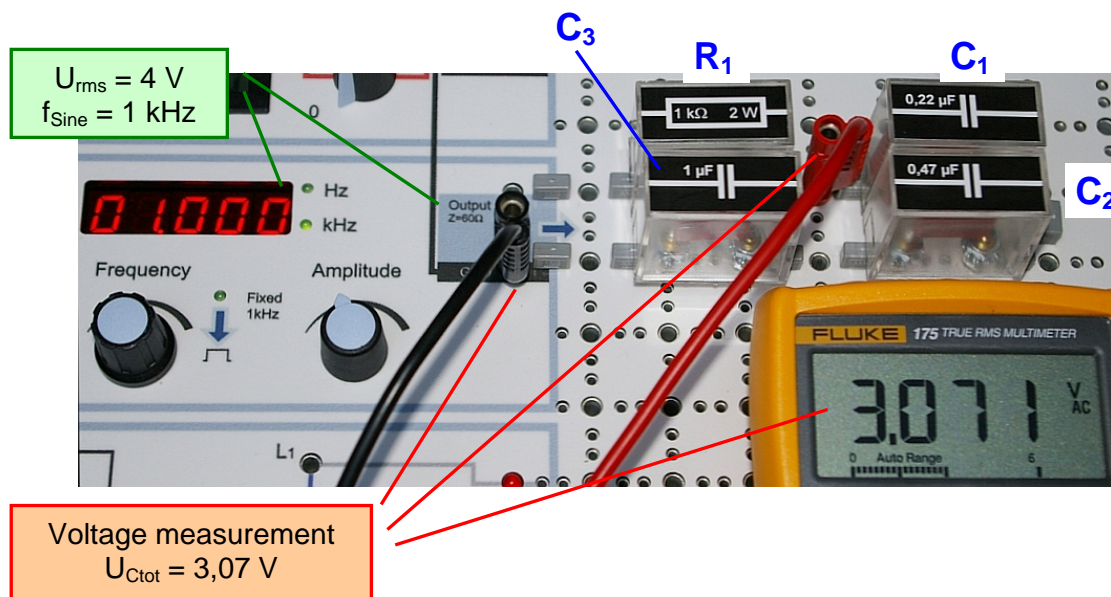


Fig. 13.5.3.1: Exercise assembly for the series connection of capacitors

## Practical Experiments

### 13.6 Capacitors Connected in Parallel

#### 13.6.1 Response of Capacitors Connected in Parallel

In a **parallel circuit** of capacitors, the *plate area A* becomes larger. Therefore, the capacitance  $C$  is given by the sum of all single capacitors (Fig. 15.6.1.1). Equation:

$$C_{tot} = C_1 + C_2 + C_3 + \dots + C_n$$

The total current  $I_{Ctot}$  is divided between the individual capacitor branches, according to the values of the individual capacitors.

The capacitor voltage  $U_C$  across all parallel connected capacitors, is the same. The capacitive reactance of the whole circuit,  $X_{Ctot}$  is less than the smallest single reactance,  $X_{Cn}$ .

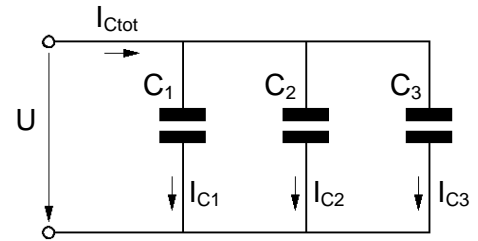


Fig. 13.6.1.1: Parallel circuit of capacitors

$$X_{Ctot} = \frac{1}{\frac{1}{X_{C1}} + \frac{1}{X_{C2}} + \frac{1}{X_{C3}} + \dots + \frac{1}{X_{Cn}}}$$

#### 13.6.2 Practical Proof of the Capacitor Response in a Parallel Circuit

The statement, 'the total capacitance of a parallel circuit of capacitors is equal to the sum of the single capacitances' will now be proved by voltage and current measurements on a multimeter.

- Assemble the circuit in Fig. 13.6.2.1 on the Electronic Circuits Board.
- Set the function generator to  $U_{rms} = 4\text{ V}$ ,  $f_{Sine} = 1\text{ kHz}$ .
- Measure the voltage  $U$  and the total current  $I_{Ctot}$ .

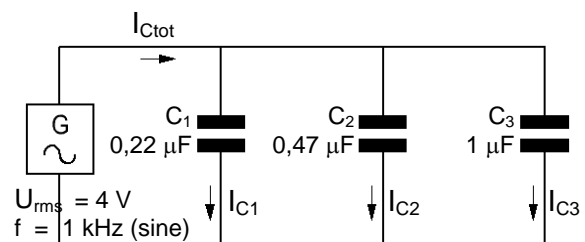


Fig. 13.6.2.1: Measurements on a parallel circuit of capacitors

$U = \dots\dots\dots$  ;  $I_{Ctot} = \dots\dots\dots$

- Calculate the total capacitance of the parallel circuit using the measured values.

- As a check, calculate the capacitor values from their nominal value and compare the result with the value of  $C_{tot}$  calculated from the measured values.

## 14. Coil in an AC Circuit

### 14.1 Construction and Characteristics of Coils

Current flowing through a conducting material (e.g. copper wire), generates a *magnetic field*, the *lines of force* of which can be considered as concentric circles about the centre of the wire (Fig. 14.1.1). The term 'magnetic field' is often used (and is also used in this handbook), but strictly speaking, the real term is **magnetic flux density B** or **magnetic induction**. The direction of the magnetic flux ('lines of force') around the wire is given by the *right hand rule*: If the thumb of the right hand points in the direction of the current flow, then the fingers bent around the wire, point in the direction of the magnetic flux.

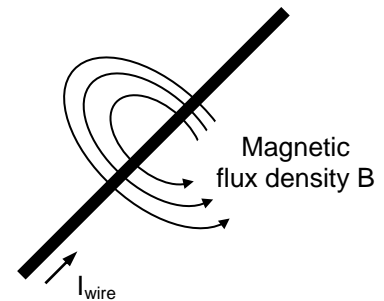


Fig. 14.1.1:  
Magnetic flux density B

A coil is created when a conductor is wound to form a spring-like body. The shape of the coil causes a concentration of the magnetic flux B. Fig. 14.1.2 shows the orientation of the magnetic flux in and around, a cylindrical coil of wire. In electronic circuits, either of the circuit symbols shown in Fig. 14.1.2 right, can be used. The top symbol is used mainly for high-energy, low frequency applications (e.g. electric motors or transformers); the symbol below this, is used in applications for higher frequencies with a lower power (e.g. oscillatory circuits or small coupling transformers). Coils react to a change in current flow that causes a build-up or decay of their magnetic field. The reaction is always opposite to the cause, thus:

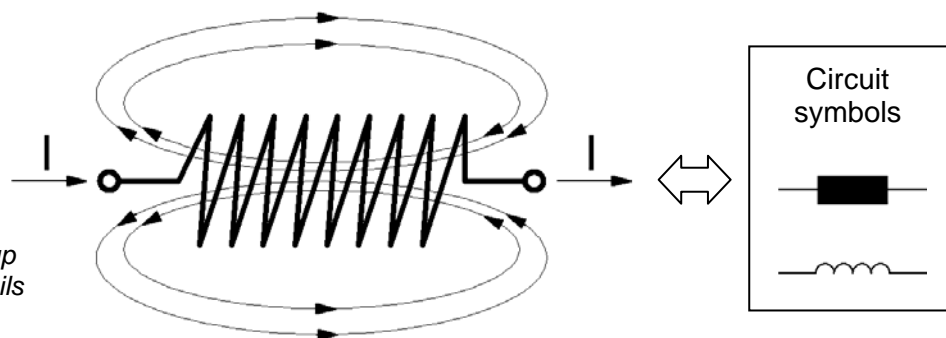


Fig. 14.1.2: Field build-up and circuit symbols of coils

- An increase in current produces a **mutual induction  $U_L$**  in the coils that opposes the external voltage. This voltage cannot be measured, but it has the effect on the current, of producing a decay of the magnetic field. The coil consumes energy from the circuit to build up the magnetic field, that the coil stores as magnetic flux.
- If the current in a circuit decreases, then the coil generates a voltage by mutual induction that attempts to maintain the current flow. In other words, it 'pushes' current into the circuit. The energy for this process originates from the magnetic field, that in turn, decays by the same amount.

The reaction of a coil to changes in the current, depends on its **inductance L**. The larger the inductance, the greater is the effect of the mutual induction of the coil in the circuit. The inductance L is given by the properties of the coil, *number of turns, cross sectional area and length of the coil, and material of the conductor*.

## Practical Experiments

A decisive factor is also whether the coil is air-spaced or has a *core* in the centre, the material of which supports the magnetic flux. An example is shown in Fig. 14.1.3, a small so-called cross-wound coil for high frequency applications in the region of 300 to 3000 kHz. It is wound on a plastic former with an iron-dust core in the centre. By screwing the core in or out, the inductance of the coil can be altered for the purposes of tuning.



Fig. 14.1.3:  
Example of a cross-wound coil

In the calculation of inductance, the number of windings is taken as a square of the number. The other terms or factors, in the equation can only be approximately estimated. Therefore, these factors are combined to give the **coil constant  $A_L$** .

Inductance:

$$L = N^2 \cdot A_L$$

Coil constant:  
(cylindrical coil)

$$A_L = \frac{\mu_0 \cdot \mu_r \cdot A}{l}$$

$L$  : Inductance, Henry [H]  
 $N$  : Number of windings [no dimensions]  
 $A_L$  : Coil constant [H]  
 $A$  : Cross-sectional area [m<sup>2</sup>]  
 $l$  : Length [m]  
 $\mu_0$  : Magnetic field constant  $1,257 \cdot 10^{-6}$  [Vs/Am]  
 $\mu_r$  : Permeability [no dimensions]

For a *cylindrical* coil, the coil constant  $A_L$  is valid with the above equation. Determining the magnitude of  $A$  (cross-sectional area) and  $l$  (length), depends on whether the coil has a core or not:

- *Without a core*, the area and length refer to the actual coil. Also, the permeability number  $\mu_r$  is omitted from the equation.
- *With a core*, the area and length of the core as well as the permeability number  $\mu_r$  for the material, must be inserted in the equation.

The permeability number  $\mu_r$  in a vacuum is unity ('1'), with air, almost unity and increases when special core materials are used, up to a 6-figure value.

Due to the effects of mutual induction in the coil, *alternating currents* produce an **inductive reactance  $X_L$** , where no active power is dissipated. The coil does consume energy however, from the circuit for the build-up of the magnetic field, but with the later decay of the field, feeds this energy back into the circuit.

The magnitude of the inductive reactance depends on the frequency and the inductance; equation:

$$X_L = \omega \cdot L = 2\pi \cdot f \cdot L$$

$X_L$  : Inductive reactance [ $\Omega$ ]  
 $\omega$  : Angular frequency [1/s]  
 $f$  : Frequency [1/s]  
 $L$  : Inductance [H]

## 14.2 Types and Tasks of Coils

In electrical engineering and electronics, coils are required in a multitude of very different applications:

- Energy storage
- Electric drives (electromotors)
- Converting other forms of energy to electrical energy (generators)
- Transformation of AC voltages and current (transformers)
- Isolating electrical circuits (coupling transformers)
- Switching large currents by way of a smaller current (relays, contactors)
- Selection of frequency ranges (filters)
- Generating oscillations (oscillatory circuits)

Table 14.2.1 Summary of basic types of coils and applications.




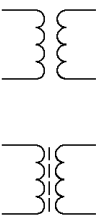
Inductance	Description	Circuit symbol	Construction
Variable	Adjustable inductance		For single or seldom alignment processes (high frequency techniques)
Fixed	Fixed inductance		Coil without core, air-spaced, wound on a former or encapsulated; $\mu_r \sim 1$
	Coil with core		Coil with core for improving the magnetic flux by increasing the inductance; $\mu_r \neq 1$
	Transformer		Two coils (primary & secondary windings), coupled via a common magnetic field; the transformation of energy is determined by the ratio of the coil windings. For low-frequency uses; for energy transfer, always with core, for high-frequency uses, also without core.

Table 14.2.1: Types of coils

## Practical Experiments

### 14.3 Reaction of a Coil to Voltage Changes

#### 14.3.1 On and Off Switching Processes at a Coil

The current in a coil changes only when the current is switched on and off. The change produced in the magnetic flux generates a *self-induced e.m.f. (or voltage)*. Its direction is such that it maintains the existing state of the magnetic field. When the current is switched on, the self-induction effect then opposes the build-up of the magnetic flux. At the instant of switch-on, the mutually induced voltage opposes the input voltage, thus there is no flow of current. With the initial rapid increase in current flow, the magnetic field in the coil increases and the effects of mutual induction are reduced. Finally, the current in the circuit is limited by the ohmic resistance of the coil, or any other resistor in the circuit. (Fig. 14.3.1.1).

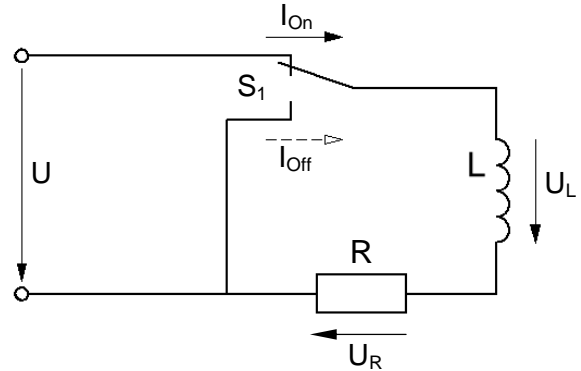


Fig. 14.3.1.1: DC circuit with coil, L

Current and voltage at the coil, both follow an *e-function* (Fig. 14.3.1.2 shows the current curve). The same applies to the switch-off process. At the instant of switching off, an opposing self-induced voltage delays the decay of current. The field energy in the coil, drives the current in the same direction, through the circuit. The decay of current follows a similar e-function as before (Fig. 14.3.1.2). Finally, both coil and resistor are without voltage and there is no flow of current; the field energy in the coil is converted at the resistor, to heat.

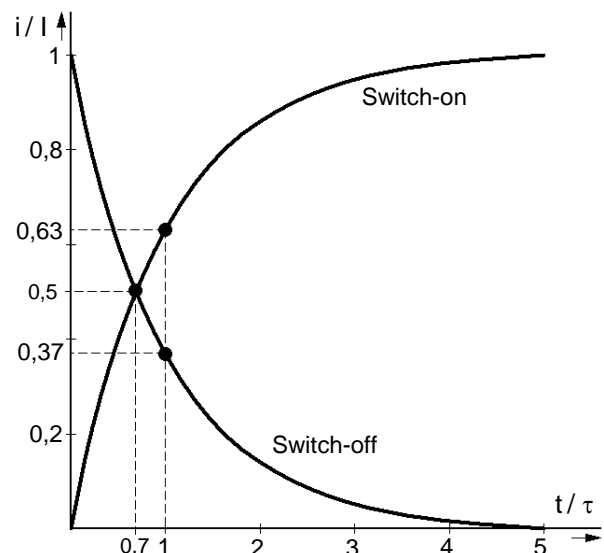


Fig. 14.3.1.2: On and Off switching curves at the coil

The time response of a coil, corresponds to that of a capacitor. The time constant  $\tau$  is given by the ratio of inductance L to resistance R:

$$\tau = \frac{L}{R} \quad \left| \begin{array}{l} L: \text{Inductance [H]} \\ R: \text{Resistance } [\Omega] \\ \tau: \text{Time constant [s]} \end{array} \right.$$

At  $1 \cdot \tau$  after switch-on, the current in the coil has reached 0,63-times its maximum value (Fig. 14.3.1.2). After  $5 \cdot \tau$ , the field build-up is complete and the current flow is at maximum.

The instantaneous value of current  $i_L$  in the coil, is given by:

$$i_L = I_{\max} \cdot (1 - e^{-t/\tau}) \quad \left| \begin{array}{l} I_{\max}: U/R \text{ [A]} \\ t: \text{Switch on time [s]} \\ e: \text{Euler's number: 2,718} \end{array} \right.$$



## Practical Experiments

The decay of coil voltage  $U_L$  after switch-on, is given by:

$$u_L = U \cdot e^{-t/\tau} \quad \left| \begin{array}{l} U : \text{Maximum coil voltage [V]} \end{array} \right.$$

The decay of current after switch-off, follows a mirrored e-function (Fig. 14.3.1.2). The same time relationships apply as for the switch-on process: Current decays by 50% after  $0,7 \cdot \tau$ ; by 63% (to  $0,37 \cdot I_{\max}$ ) after  $1 \cdot \tau$ ; process end after  $5 \cdot \tau$ .

The instantaneous value of current  $i_L$  in the coil, is given by:

$$i_L = I_{\max} \cdot e^{-t/\tau} \quad \left| \begin{array}{l} I_{\max} : U/R \text{ [A]} \\ t : \text{Switch off time [s]} \\ e : \text{Euler's number: 2,718} \end{array} \right.$$

The negative sign should be remembered for the decay of the coil voltage  $U_L$  after switch-off:

$$u_L = -U \cdot e^{-t/\tau} \quad \left| \begin{array}{l} U : \text{Maximum coil voltage [V]} \end{array} \right.$$

Familiarity with the reponse of the coil to sudden changes in voltage, is important for understanding more complex circuits. The following relationships exist between current, voltage and reactance  $X_L$  of the coil : Immediately after switching on a voltage, there is only a minimum flow of current whilst the voltage across the coil reaches its maximum value. Thus, according to Ohm's law,  $X_L$  is very large. The coil blocks the flow of current. Towards the end of the build-up of the field, at almost maximum coil current  $I_L$  and a small residual voltage  $U_L$ ,  $X_L$  has fallen to a very small value and is still reducing towards zero. From this description, it can be recognised the current and voltage at the coil (as seen previously for a capacitor), are out of phase.

### 14.3.2 Reaction of a Coil to Square-wave Voltages

A square-wave voltage can be considered as a DC voltage, periodically switched on and off. If the pulse duration  $t_i$  is at least equal to  $5 \cdot \tau$ , then the current through the coil and thus the voltage at the resistor, can increase to their maximum values, following an e-function. In the interpulse period (if  $t_p \geq 5 \cdot \tau$ ), the current in the coil  $I_L$  and voltage  $U_R$  again, fall to zero ( $I_L/U_R$  in Fig. 14.3.2.1 right).

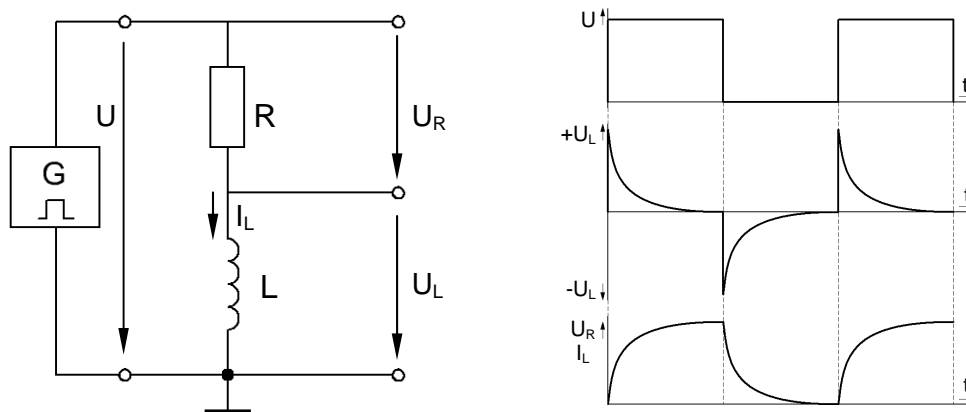


Fig. 14.3.2.1: Reaction of a coil to a square-wave voltage

## Practical Experiments

The voltage drop across a coil, is given by  $U_L = U - U_R$  in the form of needle pulses. The shorter the time constant  $\tau = L / R$ , the narrower are the needle pulses. The negative needle pulses in the interpulse period, are the result of the opposing self-induced voltage that attempts to maintain the flow of current in the coil.

The response of a coil will now be examined using the components shown, together with the input voltage given in Fig. 14.3.2.2.

- Assemble the circuit in Fig. 14.3.2.2 on the Electronic Circuits Board.
- Set the square-wave generator to a peak voltage of  $U_p = 5 \text{ V}$  at a frequency of  $f = 800 \text{ Hz}$ .

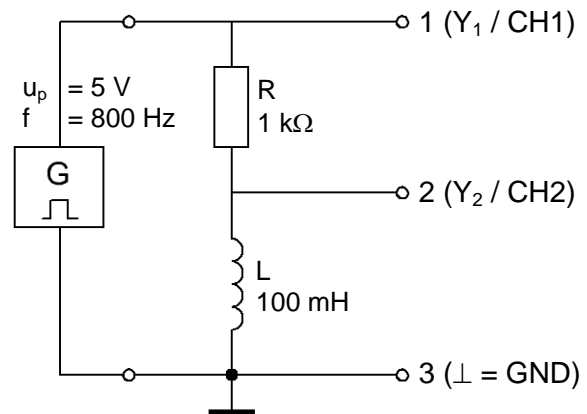


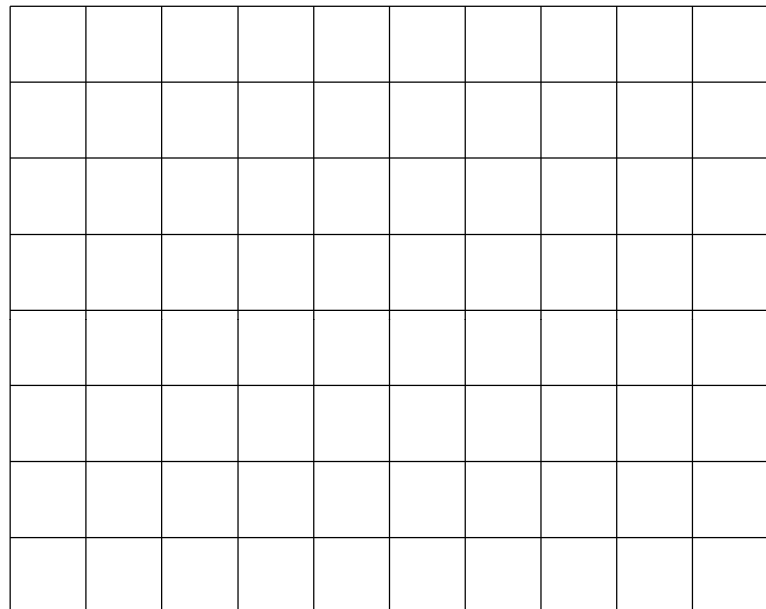
Fig. 14.3.2.2: Square-wave voltage in an LC-circuit

- Connect the oscilloscope as shown in Fig. 14.3.2.2. Adjust the oscilloscope so that both signals are displayed, one above the other with at least one complete period of the signal.

- Draw the signals displayed of  $U$  and  $U_L$  in the chart in Fig. 14.3.2.3.

Fig. 14.3.2.3: Display,  $U$  and  $U_L$

**Oscilloscope settings:**  
 $X : 0,2 \text{ ms/ div.}$   
 $Y_1 : 5 \text{ V/ div., DC}$   
 $Y_2 : 2 \text{ V/ div., DC}$

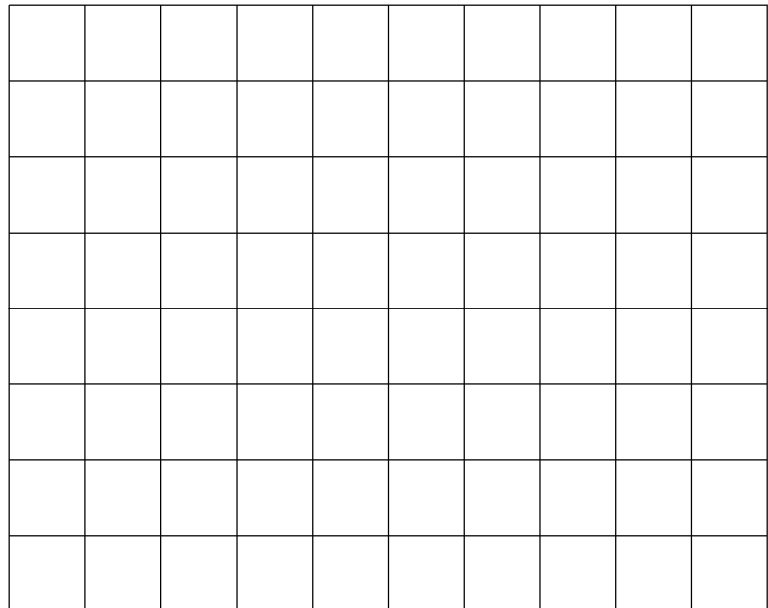


- Exchange  $R$  and  $L$  in the circuit, to display the signal across resistor  $R$ .
- Draw the signals displayed of  $U$  and  $U_R$  ( $\rightarrow I_L$ ) in the chart in Fig. 14.3.2.4.



Fig. 14.3.2.4:  
Display,  $U$  and  $U_R (\rightarrow I_L)$

**Oscilloscope settings:**  
 $X$  : 0,2 ms/ div.  
 $Y_1$  : 2 V/ div., DC  
 $Y_2$  : 2 V/ div., DC



- From the waveforms drawn, determine the time constant  $\tau$  as accurately as possible. Check your result by calculation.

$\tau$  From waveforms:

$\tau$  By calculation:

- What is the value of current in the coil ( $I_L$ ), 0,2 ms after the start of the pulse  $t_i$ ? Determine the value of  $U_R$ , by Ohm's law, using the values drawn or read from the oscilloscope ascreen. Check your measurement by calculation (use the equation from section 14.3.1).

$u_R$  Measured after 0,2 ms / read from screen:

$i_L$  by calculation:

- Explain the deviation between your calculated value and the measured value of  $u_R$ ?

## Practical Experiments

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- Calculate the inductance  $L$  from the value measured for  $\tau$ .

- What voltage can be measured across the coil, 0,2 ms after the start of the interpulse period  $t_p$ ? Read the value as accurately as possible, from the oscilloscope screen. Optimise the oscilloscope settings for reading the value accurately.

$$U_L = \dots\dots\dots$$

- Check the value read, by calculation.

- At what time has the magnetic field of the coil, reached its full strength?

- In the circuit of Fig. 14.3.2.2, the resistor is replaced by one of  $R = 220 \Omega$ . What effect has this change to the circuit have, on the time constant and the build-up of the field?

- Check your statement by measurement. Replace the resistor in the circuit of Fig. 14.3.2.2 with one of  $R = 220 \Omega$ . Display the voltages across the components on the oscilloscope. Compare the voltage waveforms with the results of the measurements in Figs. 14.3.2.3/4).

## Practical Experiments

### 14.4 Inductance with a Sine-wave Voltage

#### 14.4.1 Phase Shift between Current and Voltage

It has already been seen that with a square-wave voltage, voltage and current at a coil were out of phase. Due to the self-induction, the voltage immediately increases to a maximum, whilst the current increases only after the self-induced voltage has decayed: the current lags the voltage.

With a sine-wave voltage applied, the polarity of the magnetic field reverses, in rhythm with the frequency of the current through the coil ( $I_L$  in Fig. 14.4.1.1). The voltage across the coil leads on this process by a quarter-period ( $U_L$  in Fig. 14.4.1.1): The voltage is at a maximum when the current cuts the zero axis. Thus, between voltage and current, there is a phase shift of  $90^\circ$ .

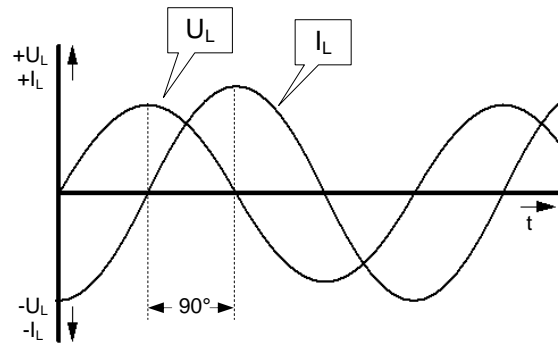


Fig. 14.4.1.1: Phase shift between voltage and current at a coil

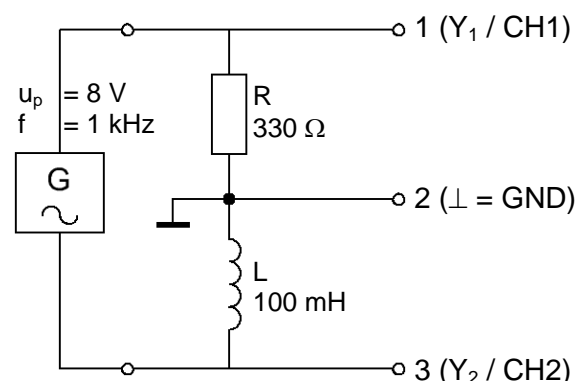
The phase shift between current and voltage will now be proved in a circuit as shown in Fig. 14.4.1.2.

- Assemble the circuit in Fig. 14.4.1.2 on the Electronic Circuits Board.

Since the changes of current and voltage at an ohmic resistor are always proportional to each other,  $U_R$  ( $Y_1 / CH1$ ) can be used for showing the phase of the current  $I_L$  in the circuit.

- Set the signal generator to a sine-wave voltage  $u_{pp} = 16 \text{ V}$  at a frequency of  $f = 1 \text{ kHz}$ .
- Connect the 2-channel oscilloscope as shown in Fig. 14.4.1.2.

Fig. 14.4.1.2: Exercise circuit to show the phase shift between  $U$  and  $I$



By adjusting the 0-axis (GND) between R and L, the voltages  $U_R$  and  $U_L$  can both be displayed on the 2-channel oscilloscope. However, the negative voltage  $U_L$  ( $Y_2 / CH2$ ) has a  $180^\circ$  phase shift. For measuring the correct phase relationship, one channel of the oscilloscope must be operated in the 'inverted' mode.

- Display the voltage waveforms  $U_R$  and  $U_L$  on the oscilloscope. Adjust the oscilloscope for a display of least 2 periods of the sine-wave.
- Draw the signal waveforms displayed in the chart, Fig 14.4.1.3.

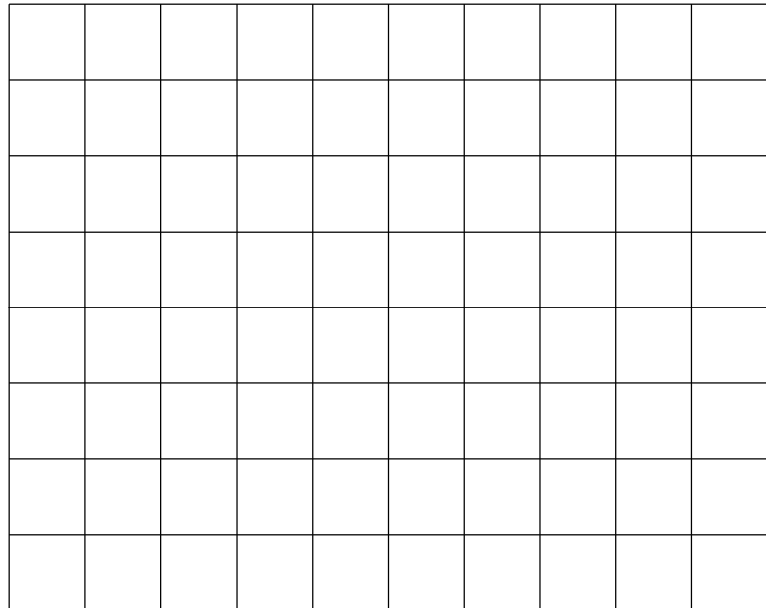
## Practical Experiments

**Oscilloscope settings:**

X : 0,2 ms/ div.  
 Y<sub>1</sub> : 2 V/ div., AC  
 Y<sub>2</sub> : 2 V/ div., AC, inverted

Fig. 14.4.1.3: Phase shift between voltage and current at the coil

- From the waveforms, determine the periodic time T, the frequency f and the angle of phase shift φ between voltage and current.



- In the circuit of Fig. 14.4.1.2, the resistance of 330 Ω is increased to 1 kΩ. What effects do you expect to see on the signals displayed on the oscilloscope? What is the tendency of events and check your considerations by measurement.

### 14.4.2 Inductive Reactance, X<sub>L</sub>

On an inductance, a sinusoidal voltage generates a magnetic field that periodically reverses in polarity. The coil presents a limiting resistance to the current produced that lags on the voltage by 90°. At this resistance, there is no thermal (active) power dissipated, therefore the resistance is known as '**inductive reactance, X<sub>L</sub>**'.

The magnitude of the inductive reactance X<sub>L</sub> is proportional to the inductance L of the coil and the frequency f of the applied sinusoidal voltage :

$$X_L = 2 \cdot \pi \cdot f \cdot L \quad \left| \begin{array}{l} L : [\text{H}] \\ f : [1/\text{s}] \\ X_L : [\Omega] \end{array} \right.$$

With a given coil current I<sub>L</sub> and a known coil voltage U<sub>L</sub>, Ohm's law can be used for calculating the value of X<sub>L</sub> :

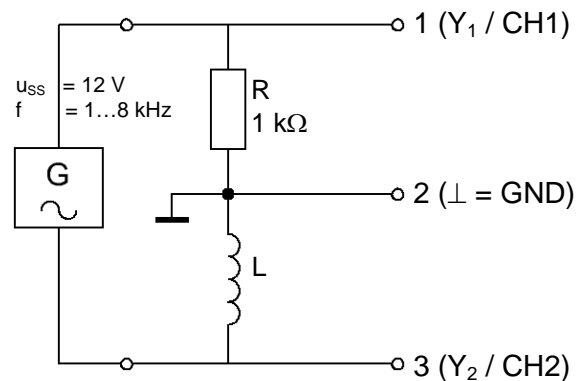
$$X_L = \frac{U_L}{I_L} \quad \left| \begin{array}{l} U_L : [\text{V}] \\ I_L : [\text{A}] \\ X_L : [\Omega] \end{array} \right.$$

## Practical Experiments

The response of inductive reactance  $X_L$  will now be examined using the circuit in Fig. 14.4.2.1, assembled on the Electronic Circuits Board. The current flow through the inductance will be calculated from the voltage drop  $U_R$  across the resistor  $R = 1\text{ k}\Omega$  ( $U_R$  and  $I_L$  in-phase).

By adjusting the 0-axis (GND) between R and L, the voltages  $U_R$  and  $U_L$  can both be displayed on the 2-channel oscilloscope.

Fig. 14.4.2.1: Exercise circuit to examine the relationship between  $X_L$ ,  $f$  and  $L$



- Assemble the circuit in Fig. 14.4.2.1 with  $L = 100\text{ mH}$  on the Electronic Circuits Board (assembly layout notes and the measurement details, are given at the end of this section).

- Set the signal generator to a sine-wave voltage  $u_{pp} = 12\text{ V}$  at an initial frequency of  $f = 1\text{ kHz}$ .

- Connect the 2-channel oscilloscope as shown in Fig. 14.4.2.1.

- Measure the peak-to-peak values of the voltages  $U_L$  and  $U_R$  at the frequencies given in the table 14.4.2.2. Complete these measurements with 2 different coils:

Coil 1:  $L = 100\text{ mH}$  (component in plastic housing)

Coil 2: Transformer coil  $N = 900$ ; upper half of the iron core, inserted.

- Enter the values measured in the table.

Table 14.4.2.2: Reactance  $X_L$ , inductance  $L$  and frequency  $f$

f [kHz]		1	2	3	4	6	8
$U_L$ [V <sub>pp</sub> ]	N = 900						
	100 mH						
$U_R$ [V <sub>pp</sub> ]	N = 900						
	100 mH						
$I_L$ [mA <sub>pp</sub> ]	N = 900						
	100 mH						
$X_L$ [kΩ]	N = 900						
	100 mH						

- Calculate the peak-to-peak values of current  $I_L$  and enter the values in the table.

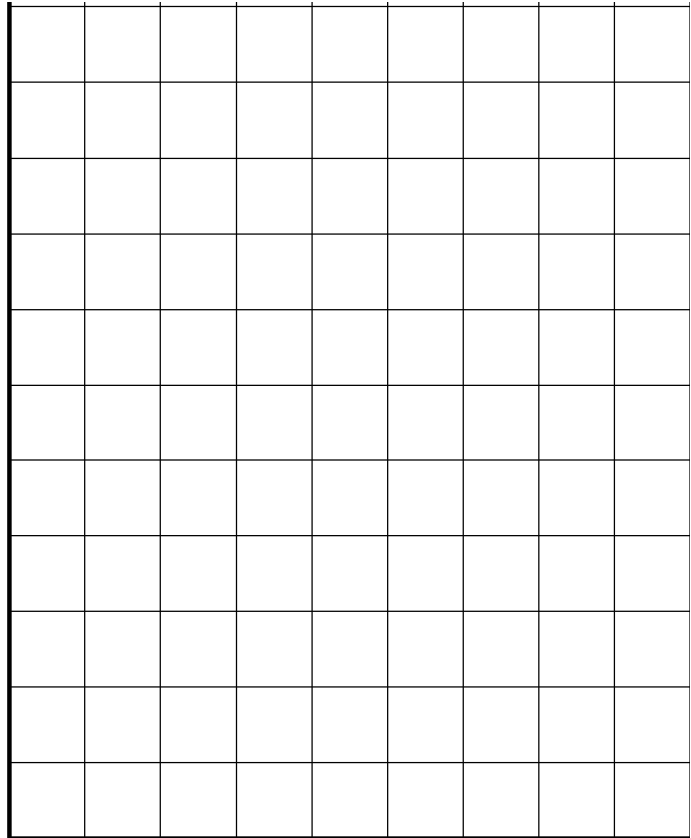
- Calculate the values for  $X_L$  and complete the table with your results.

- Plot the calculated values for the reactance  $X_L$  in the chart (Fig. 14.4.2.3).

## Practical Experiments

- Draw the characteristic  $X_L = f(f)$  for both coils.

Fig. 14.4.2.3:  
Characteristic  $X_L = f(f)$



- Check the measured values by calculation at  $X_L = f(6 \text{ kHz})$  for the coil  $L = 100 \text{ mH}$ .

- Check the nominal value of the coil  $L = 100 \text{ mH}$  by calculation. Use the values measured at  $4 \text{ kHz}$ .

- Explain the deviation between the two check calculations?

- Calculate the unknown inductance  $L$  of the transformer coil ( $N = 900$ ) from the value measure at  $X_L = f(3 \text{ kHz})$ .

- What rules or relationships can be deduced from the shape of the characteristics?

- What tendency does the reactance  $X_L$  of a coil  $L = 0,01 \text{ H}$  ( $= 10 \text{ mH}$ ), show at very high ( $> 10 \text{ MHz}$ ) and very low ( $< 100 \text{ Hz}$ ) frequencies?

## Practical Experiments

- What is the inductance  $L$  of the transformer coil ( $N = 900$ ) without a core? Measure the value in a circuit corresponding to Fig. 14.4.2.1. Use a frequency of  $f = 8$  kHz when completing the measurement.

**Exercise assembly for examining the relationships between reactance  $X_L$ , inductance and frequency.**

Fig. 14.4.2.4 shows one possible layout of the components on the Electronic Circuits Board. In the layout, the coil  $L = 100$  mH, after completing the measurements, has been removed from its original position and inserted somewhere else without connections. The transformer coil is then inserted in the circuit by completing its connections.

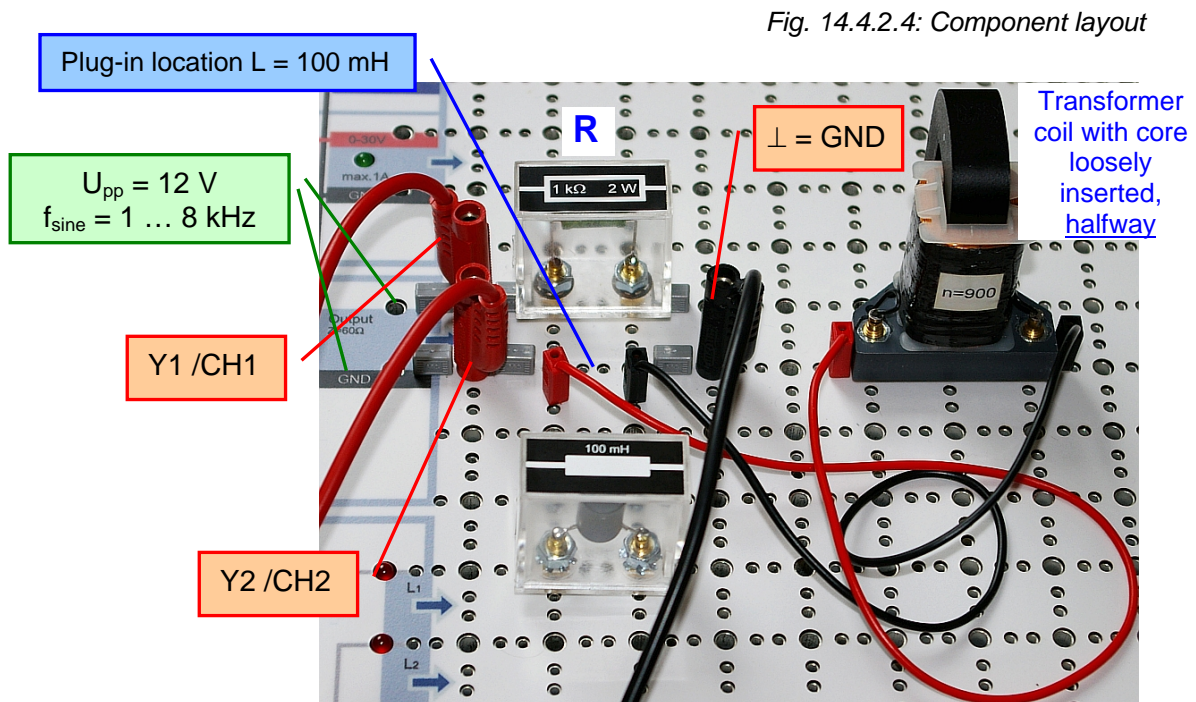


Fig. 14.4.2.4: Component layout

## Practical Experiments

### 14.4.3 Active and Reactive Power in a Coil

An *ideal coil* does not dissipate any **active power**. Although the build-up of the magnetic field requires energy, the coil stores the field energy and later when the field decays, the stored energy is again available. So in this respect, voltage and current in an inductance produce only **reactive power**.

In *real coils* however, *ohmic losses* are present, such as:

- Losses in the windings
- Current displacement losses in the windings
- Eddy current losses in the core of the coil
- Losses due to magnetic reversal in the core of the coil
- Eddy current losses in the windings
- Scattering (or leakage) losses.

**Losses in the windings** are independent of frequency and are caused by the ohmic resistance of the wire used for the windings. The losses can be in the region of a few hundred ohms when the coil consists of many turns of thin wire (the inductance  $L$ , increases with the square of the number of windings  $N$ ).

**Current displacement losses** increase with the frequency of the AC current, that is forced from inside the wire to the surface area, or skin of the wire. This reduces the effective cross sectional area of the wire, causing the wire resistance to increase. This effect is called the **skin-effect**.

**Eddy current losses** are produced in the core of the coil and in the windings, by induced voltages. They cause irregular current patterns that produce warmth in the material. These losses increase with the square of the frequency.

**Losses due to magnetic reversal** in the core of the coil are frequency-dependent and correspond to the power that must be used to align the molecular magnetic particles in the core material.

**Scattering (or leakage) losses** increase with frequency. They occur when part of the magnetic field of the coil induce eddy currents in metal objects in the vicinity of the coil.

The active power losses are combined and represented by the **power loss resistance**  $R_v$  imagined to be connected in series with the inductance (Fig. 14.4.3.1). The loss current produces the voltage drop  $U_{Rv}$  across  $R_v$ . Since the voltage at the coil ( $U_L$ ) leads the loss current and thus, the voltage  $U_{Rv}$  by  $90^\circ$ , the relevant vectors show a loss angle,  $\delta$  (Fig. 14.4.3.1).

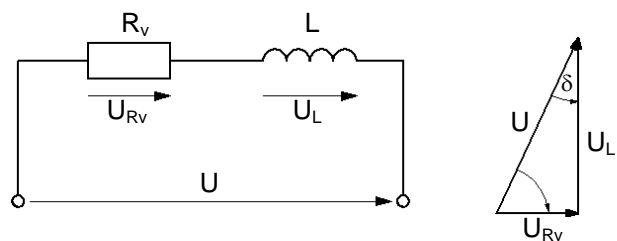


Fig. 14.4.3.1: Losses at a real coil

The active power losses give the **loss factor, d** :

$$d = \tan \delta = \frac{R_v}{X_L} = \frac{U_{Rv}}{U_L}$$

$d$  : Loss factor, [no dimensions]  
 $\delta$  : Loss angle [°]  
 $X_L$  : Reactance [ $\Omega$ ]  
 $R_v$  : Loss resistance [ $\Omega$ ]



## Practical Experiments

The **active power (P)** consumed by a coil is the result of unwanted but unavoidable losses. They must be accepted within reason, due to the physical limits in the manufacture of coils.

The **reactive power Q** at a coil is given by the product of coil voltage and reactive current. It can be represented as a multiplication of the instantaneous values of  $u_L$  and  $i_L$  in a line chart with the phase relationships (Fig. 14.4.3.2).

The reactive power  $Q_L$  is calculated from:

$$Q_L = U_L \cdot I_L \quad \text{or}$$

$$Q_L = \frac{U_L^2}{X_L} \quad \text{or}$$

$$Q_L = I_L^2 \cdot X_L$$

$Q_L$  : Reactive power, [W]  
 $U_L$  : [V]  
 $I_L$  : [A]  
 $X_L$  : [ $\Omega$ ]

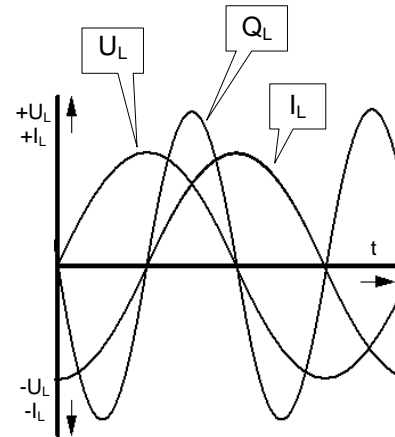


Fig. 14.4.3.2: Reactive power,  $Q_L$

In an example circuit, the response of current and voltage will be displayed on an oscilloscope, for one complete period of a sinusoidal voltage. The waveforms displayed will then be drawn in a chart. Finally, the waveform of the reactive power curve will be plotted from the values measured and the curve drawn in the chart..

- Assemble the circuit in Fig. 14.4.3.3 on the Electronic Circuits Board.

The current  $I_L$  is determined indirectly from the voltage  $U_R$  measured on  $Y_1 / CH1$  of the oscilloscope. Because the earth point (GND) is taken between R and L in the circuit, one channel of the oscilloscope must be operated in the 'inverted' mode to display the correct phase relationship.

- Set the signal generator to a sine-wave voltage  $u_p = 6 \text{ V}$  at a frequency of  $f = 1 \text{ kHz}$ .

- Connect the 2-channel oscilloscope as shown in Fig. 14.4.3.3.

- Display the voltage waveforms  $U_R$  and  $U_L$  on the oscilloscope.

- Measure the instantaneous values of the voltages  $u_R$  and  $u_L$  at the times given in table 14.4.3.4. Enter the values in the table.

- Calculate the instantaneous values of current in the coil  $i_L$  from  $u_R$  and enter the values in the table.

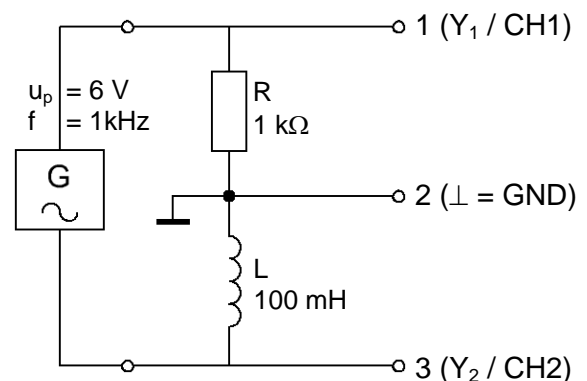


Fig. 14.4.3.3: Exercise circuit for measuring the inductive reactance,  $Q_L$

## Practical Experiments

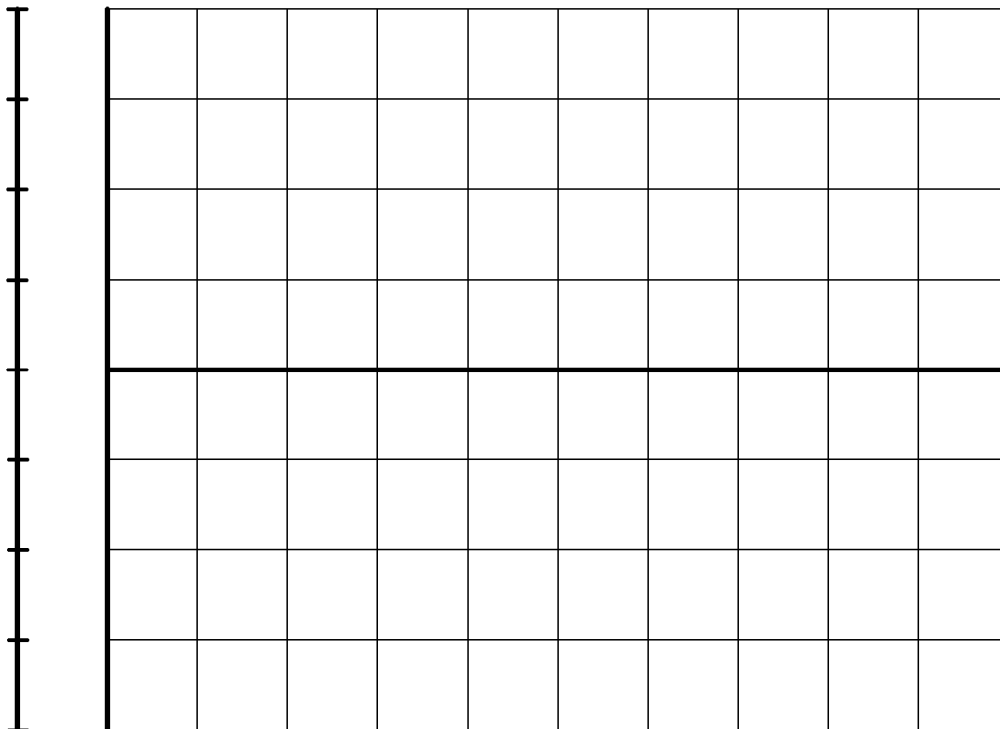
- Calculate the reactive power  $q_L$  from  $u_L$  and  $i_L$  at the times given in table. Complete the table with your results of calculation.

Table 14.4.3.4: Instantaneous values, exercise circuit in Fig. 14.4.3.3

t [ms]	0	0,1	0,2	0,25	0,4	0,5	0,6	0,75	0,8	0,9	1
$u_R$ [V]											
$u_L$ [V]											
$i_L$ [mA]											
$q_L$ [mW]											

- Sketch the voltage curve  $U_L = f(t)$ , the current curve  $I_L = f(t)$  and the power curve  $Q_L = f(t)$  as accurately as possible, in the chart given in Fig. 14.4.3.5.

Fig. 14.4.3.5: Waveforms of voltage  $U_L$ , reactive current  $I_L$  and reactive power  $Q_L$  at the coil



## Practical Experiments

### 14.5 Coils Connected in Series

#### 14.5.1 Response of Coils Connected in Series

In a **series connection** of coils (Fig. 14.5.1.1), the change of current  $\Delta I/\Delta t$  acts in all individual coils at the same time. Thus, at each coil a self-induced voltage is produced of the same polarity, that acts in opposition to the current change. The self-induced voltages in the series connected coils, add to give the total voltage.

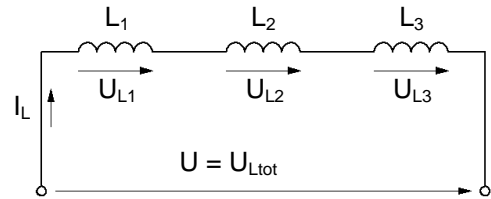


Fig. 14.5.1.1:  
Coils connected in series

$$U = U_{tot} = U_{L1} + U_{L2} + U_{L3} + \dots + U_{Ln}$$

The total inductance  $L_{tot}$  is given by the sum of the individual inductances :

$$L_{tot} = L_1 + L_2 + L_3 + \dots + L_n$$

Also, the total inductive reactance  $X_{Ltot}$  is given by the sum of the individual inductances :

$$X_{Ltot} = X_{L1} + X_{L2} + X_{L3} + \dots + X_{Ln}$$

#### 14.5.2 Practical Proof of the Coil Response in a Series Circuit

The statement, 'the total inductance of a series circuit is given by the sum of all individual inductances', will now be proved by voltage and current measurements on a multimeter.

- Assemble the circuit in Fig. 14.5.2.1 on the Electronic Circuits Board. Use the following coils:

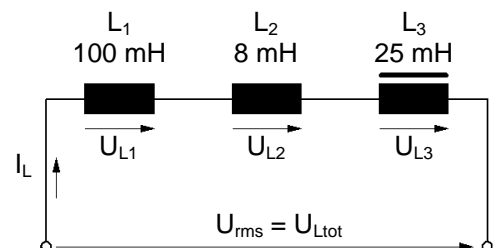
$L_1$  : Component in plastic housing;  $L = 100\text{mH}$

$L_2$  : Transformer coil;  $N = 900$ ; without core;  $L = 8\text{ mH}$

$L_3$  : Transformer coil;  $N = 900$ , half-core;  $L = 25\text{ mH}$

- To avoid any influence of mutual magnetic coupling, the coils should be located on the Board with as much clearance as possible. Notes on the layout and measurements, will be found in section 14.5.3).

Fig. 14.5.2.1: Measurements on a series circuit of coils



- Set the function generator to  $U_{rms} = 6\text{ V}$ ,  $f_{sine} = 1\text{ kHz}$ .

- Measure the values of voltage named in table 14.5.2.2 with a multimeter and enter the values in the table.

Table 14.5.2.2: Measurements on a series circuit of coils

Voltage [V]				Current [mA]
$U_{rms} = U_{Ltot}$	$U_{L1}$	$U_{L2}$	$U_{L3}$	$I_L$
6				



## Practical Experiments

- Assume that at coil  $L_1$  in the circuit of Fig. 14.5.2.3, due to a manufacturing fault, a break occurred in the core in the coil. This has had an effect on the build-up and decay of the magnetic field. In such a case, how do the values change of the variables given below? Indicate the tendency in the form of up and down arrows.

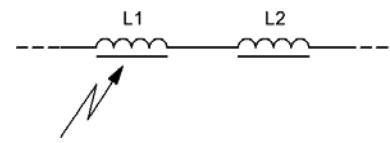


Bild 14.5.2.3: Break in the core

$L_1$ : ;  $X_{L1}$ : ;  $I_L$ : ;  $U_{L1}$ : ;  $U_{L2}$ :

Check your assumptions for  $I_L$  and  $U_{L_n}$  by measurement in the circuit shown in Fig. 14.5.2.1. Simulate the break in the core by removing half of the core in  $L_3$ .

### 14.5.3 Exercise Assembly of a Series Circuit of Coils on the Electronic Circuits Board

To avoid any influence of mutual magnetic coupling between the coils,  $L_1$ ,  $L_2$  and  $L_3$  should be located on the Electronic Circuits Board with as much clearance as possible (Fig. 14.5.3.1). The actual spacing is limited only by the connection leads (preferably, with 2 mm plugs). The ammeter is in the circuit and forms the connection between  $L_3$  and GND of the sine-wave generator.

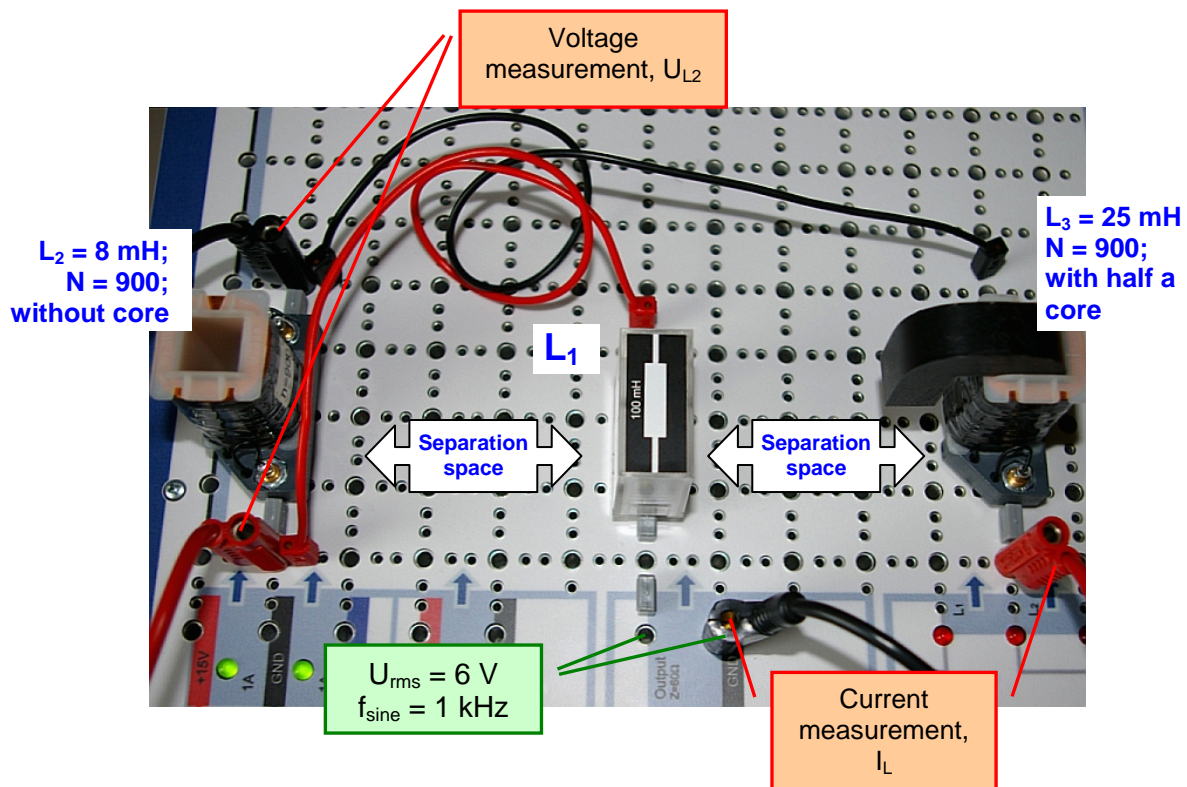


Fig. 14.5.3.1: Component layout for the series circuit of coils

## Practical Experiments

### 14.6 Coils Connected in Parallel

#### 14.6.1 Response of Coils Connected in Parallel

In a **parallel connection** of coils (Fig. 14.6.1.1) the total inductance  $L_{tot}$  is always less than the smallest single inductance :

$$L_{tot} = \frac{1}{\frac{1}{L_1} + \frac{1}{L_2} + \frac{1}{L_3} + \dots + \frac{1}{L_n}} \quad \text{or :}$$

$$\frac{1}{L_{tot}} = \frac{1}{L_1} + \frac{1}{L_2} + \frac{1}{L_3} + \dots + \frac{1}{L_n}$$

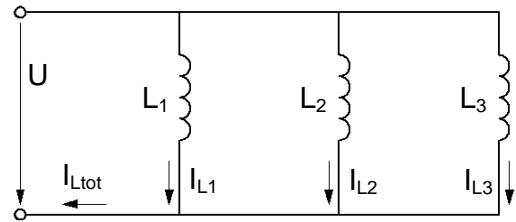


Fig. 14.6.1.1: Parallel connection of coils

The equation can be simplified for a parallel connection of only 2 coils :

$$L_{tot} = \frac{L_1 \cdot L_2}{L_1 + L_2}$$

The total current  $I_{tot}$  is divided in the individual branches of coils, inversely proportional to the corresponding inductance in each branch. The inductive reactance of the circuit  $X_{L_{tot}}$  is less than the smallest single reactance  $X_{L_n}$ :

$$X_{L_{tot}} = \frac{1}{\frac{1}{X_{L1}} + \frac{1}{X_{L2}} + \frac{1}{X_{L3}} + \dots + \frac{1}{X_{Ln}}} \quad \text{or :} \quad \frac{1}{X_{L_{ges}}} = \frac{1}{X_{L1}} + \frac{1}{X_{L2}} + \frac{1}{X_{L3}} + \dots + \frac{1}{X_{Ln}}$$

#### 14.6.2 Practical Proof of the Coil Response in a Parallel Circuit

The statement, 'the total inductance of a parallel connection of coils is less than the smallest single inductance', will now be proved by voltage and current measurements on a multimeter.

- Assemble the circuit in Fig. 14.6.2.1 on the Electronic Circuits Board. Remember the spacing between individual coils (layout notes, see section 14.5.3).

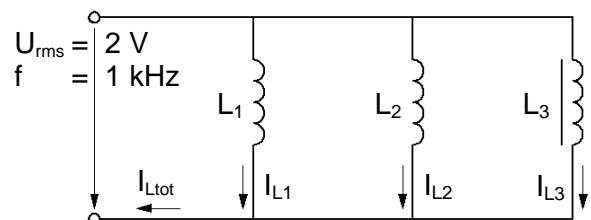


Fig. 14.6.2.1: Measurements on a parallel circuit of coils

- Use the following coils:

$L_1$  : Component in plastic housing;  $L = 100\text{mH}$

$L_2$  : Transformer coil;  $N = 900$ ; without core;  $L = 8\text{ mH}$

$L_3$  : Transformer coil;  $N = 900$ , with half-core;  $L = 25\text{ mH}$

- Set the function generator to  $U_{rms} = 2\text{ V}$ ;  $f_{sine} = 1\text{ kHz}$ .

- Measure the values of current in table 14.6.2.2 with a multimeter and enter the values in the table.

## Practical Experiments

Table 14.6.2.2: Measurements on a parallel circuit of coils

Current [mA]				Voltage [V]
$I_{L_{tot}}$	$I_{L_1}$	$I_{L_2}$	$I_{L_3}$	$U = U_{rms}$
				2

- From the values measured and using Ohm's law, determine the reactances  $X_{L_n}$  and  $X_{L_{tot}}$ .

- Use your results from calculating the reactance, to determine the inductances,  $L_n$  and  $L_{tot}$ . Calculate the total reactance  $L_{tot}$ , using 2 different methods.

- How do the values change of the variables given below, when half of the core in  $L_3$  is removed? Indicate the tendency in the form of up and down arrows.

$L_3$ :        ;     $X_{L3}$ :        ;     $I_{L3}$ :        ;     $I_L$ :        ;     $L_{tot}$ :

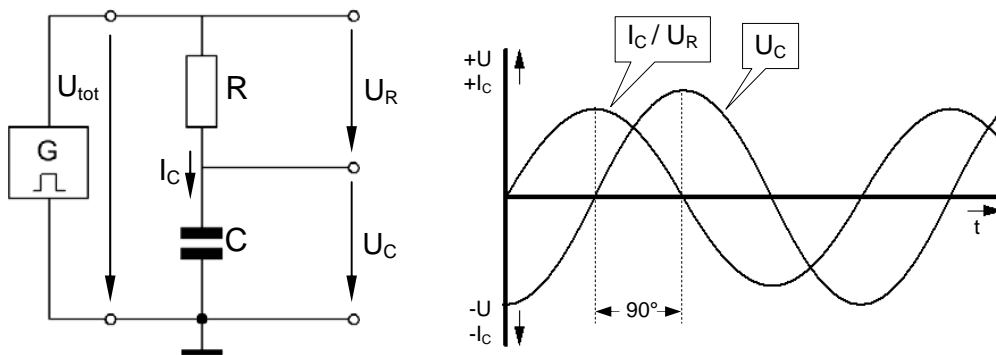
- Check your conclusions for the current changes, by measurement in the circuit of Fig. 14.6.2.1.

## 15. Combination of Reactive and Active Resistance

### 15.1 Working with Vector Diagrams

Passive components such as resistors, capacitors and coils, are often used in a combined circuit. In such a circuit, measured alternating voltages, currents and resistances (reactances), cannot simply be added or subtracted because they exhibit a **phase shift** to one another. This fact was seen for the first time, in the study of the responses of capacitors (Fig. 15.1.1). Current and voltage are  $90^\circ$  out-of-phase. The voltage drop across the resistor  $R$ , produced by the current through the capacitor, must lead the capacitor voltage by  $90^\circ$  (Fig. 15.1.1, right).

Fig. 15.1.1: Phase shift between  $U_C$  and  $U_R$



The **vector diagram** has proved to be very useful (Fig. 15.1.2), for simplifying the task of understanding the relationships between the variables and as an aid in forming a picture of the resultant values. A vector diagram enables quantities to be represented as straight lines to show both magnitude and direction of the quantity. In the case here, the angle from the  $360^\circ$  full circle, indicates the phase relationship and the length of the line, represents the magnitude. Fig. 15.1.2 (top) shows a vector diagram for an RC combination: the vector for the voltage at resistor  $U_R$  is horizontal at  $0^\circ$ . The capacitor voltage  $U_C$  is drawn with  $-90^\circ$  phase shift because it lags. The length of the vectors (= voltage values) form 2 sides of a rectangle, the diagonal of which represent the total voltage,  $U_{tot}$ . This resultant voltage has a phase shift of  $\varphi$  to the  $0^\circ$ -axis (Fig. 15.1.2, top). The final vector diagram is shown in the middle diagram of Fig. 15.1.2.

The phase relationship of the resultant voltage also depends on the magnitude of the voltages (vector length). Due to the reactance  $X_C$ , the voltages are frequency-dependent. For example, if the frequency of the applied voltage  $U_{tot}$  in Fig. 15.1.1 is increased, the reactance  $X_C$  decreases, which is why  $U_C$  falls.  $U_R$  increases and the phase angle  $\varphi$  becomes smaller (Fig. 15.1.2, bottom).

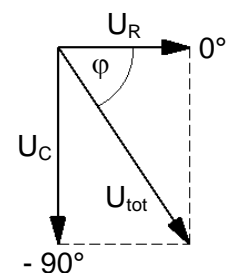
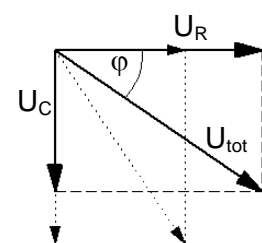
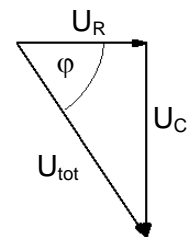


Fig. 15.1.2: Vector diagrams





## Practical Experiments

Since the 2 components R and C in the circuit of Fig. 15.1.1 are *in series*, the same current I, flows through both. A vector diagram of currents, only really makes sense, when used for *parallel circuits*. In parallel circuits, the same voltage is present across all components, which is why a voltage vector diagram is not used.

Irrespective of whether it is series or parallel, all circuits have resistance. The phase angle corresponds to the relevant voltage that is dropped across the resistance. Fig. 15.1.3 shows the resistance vectors for the R-C circuit of Fig. 15.1.1. The active resistance R is on the 0°-axis. The reactance  $X_C$ , as the associated capacitor voltage  $U_C$ , lags by 90°. Both quantities add vectorially to give the **impedance Z**, the phase angle ( $\varphi$ ) of which corresponds to that of the voltage  $U_{tot}$ .

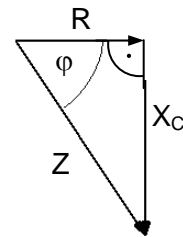


Fig. 15.1.3: Vector diagram, R,  $X_C$ , Z

Since vector diagrams form a right-angled triangle (Fig. 15.1.3), the quantities can be calculated by way of the trigonometrical functions  $\sin \varphi$  and  $\cos \varphi$  as well as from the theorem of Pythagoras. For example, there are several possible methods of calculating the impedance Z in Fig. 15.1.3:

$$\sin \varphi = \frac{X_C}{Z} \Rightarrow Z = \frac{X_C}{\sin \varphi} \quad \text{or} \quad \cos \varphi = \frac{R}{Z} \Rightarrow Z = \frac{R}{\cos \varphi} \quad \text{or}$$

$$Z = \sqrt{R^2 + X_C^2}$$

As shown in Fig. 15.1.4, an example of an RLC series circuit, any combination can exist of passive components such as capacitors, inductances and resistors. Since inductive and capacitive components exhibit a phase shift of 180° to each other, the vectors subtract (diagram, Fig. 15.1.4 centre). The remaining vector, together with the ohmic component, forms the resultant quantity ( $U_{tot}$  in Fig. 15.1.4, right).

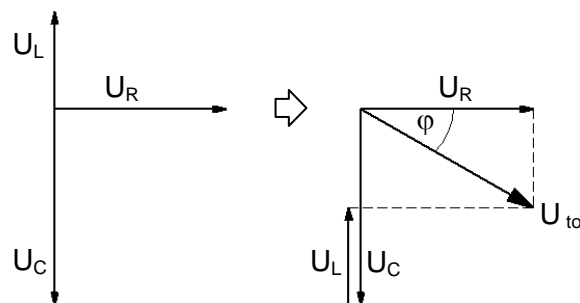
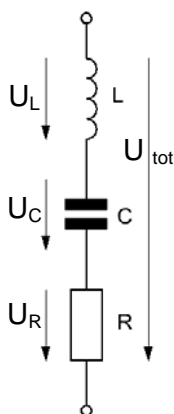


Fig. 15.1.4: Vector diagram, RLC circuit

## Practical Experiments

In the consideration of parallel circuits, complicated resistance equations using calculations with the conductivity value, can be avoided. The **conductance G** is calculated with the **susceptance values**  $B_C$  (capacitive) and  $B_L$  (inductive) to give the **admittance value Y**. Fig. 15.1.5 clearly shows this, in an RL-parallel circuit:

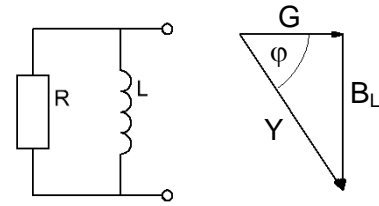


Fig. 15.1.5: Calculating with conductivity values

$$Y = \sqrt{G^2 + B_L^2} \Leftrightarrow \left( Z = \frac{1}{Y} \ ; \ R = \frac{1}{G} \ ; \ X_L = \frac{1}{B_L} \right)$$

If necessary, the resistance values  $Z$ ,  $R$ ,  $X_L$  and  $X_C$  can be calculated at any time, by forming the reciprocal of the relevant conductivity value.

Powers show the same phase shift as that of voltages or currents, from which the power is calculated. The **active power P** and the capacitive or inductive **reactive power** ( $Q_C$ ,  $Q_L$ ) are shown by the vector for **apparent power S**. Fig. 15.1.6 shows the relationships in an RL parallel circuit. Apparent power  $S$  and active power  $P$  are linked by the phase shift angle  $\varphi$ .

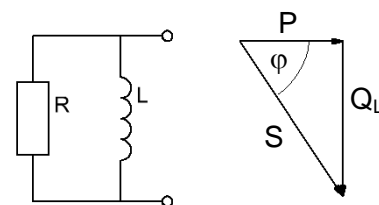


Fig. 15.1.6: Power in RLC circuits

Thus, for calculating the power, the trigonometrical functions  $\sin \varphi$  and  $\cos \varphi$ , explained previously, can be used as well as the theorem of Pythagoras.

## Practical Experiments

### 15.2 Series Circuits of Resistor, Capacitor and Coil

The use of vector diagrams and the calculation of characteristic quantities will now be practised with examples on an RLC series circuit.

**Note: A layout example for RLC circuits, will be found in section 15.4.**

#### Exercise 1: RL Series Circuit

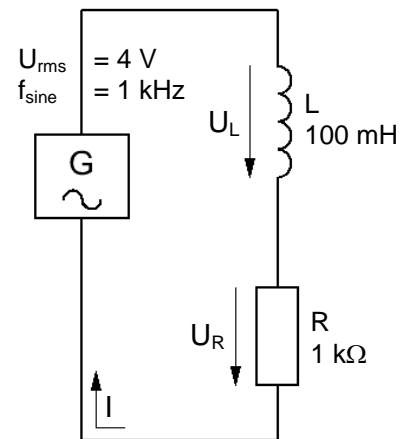
- Assemble the circuit in Fig. 15.2.1 on the Electronic Circuits Board.
- Set the function generator to an output voltage of  $U_{rms} = 4\text{ V}$ ,  $f_{sine} = 1\text{ kHz}$ .
- Measure the voltages and current in the circuit.

$$U_{rms} = U_{tot} = \quad ; U_L =$$

$$U_R = \quad ; I =$$

- Calculate the inductive reactance  $X_L$  and the resistance  $R$ , from the values measured.

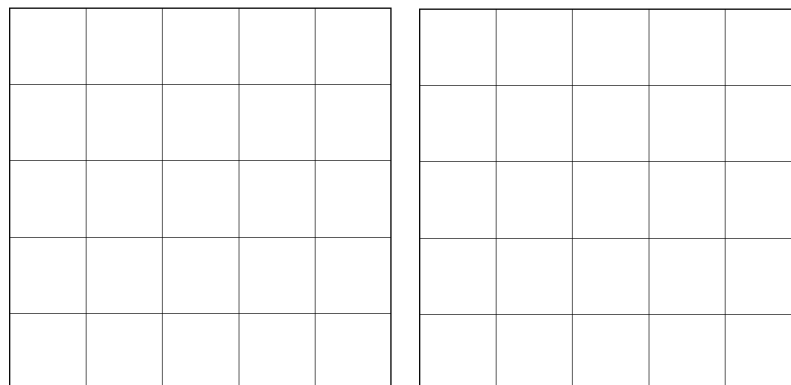
Fig. 15.2.1: RL series circuit



- Draw the vector diagram for the voltages ( $U_R$ ,  $U_L$ ,  $U_{tot}$ ) and the resistances ( $R$ ,  $X_L$ ,  $Z$ ) in the chart, Fig. 15.2.2.

Fig. 15.2.2:  
Vector diagrams

Scale:  
1 cm = 1 V



Scale:  
1 cm = 200 Ω

- Determine the impedance  $Z$  from the diagram and check the value by calculation, using the values measured.

From the diagram:  $Z =$

Calculation:

## Practical Experiments

- Draw the phase angle  $\varphi$  in the diagrams. Calculate the phase angle from your measured values.

- Connect the inputs of the oscilloscope : Y1:  $U_{tot}$  ; Y2:  $U_R$  (GND = GND function generator).

- Display the voltages  $U_{rms} = U_{tot}$  and  $U_R$ . Calculate the expected peak values. Check your measurements with the calculated values.

Measurement:  $U_{tot} = \dots\dots\dots$  ;  $U_R = \dots\dots\dots$

- Adjust the oscilloscope so that to ease measurements, the phase shift between the voltages is clearly seen. Draw one period of the voltage waveform in the chart below (Fig. 15.2.3).

**Oscilloscope settings:**  
 X : 0,1 ms/ div.  
 Y<sub>1</sub> : 2 V/ div., AC  
 Y<sub>2</sub> : 2 V/ div., AC

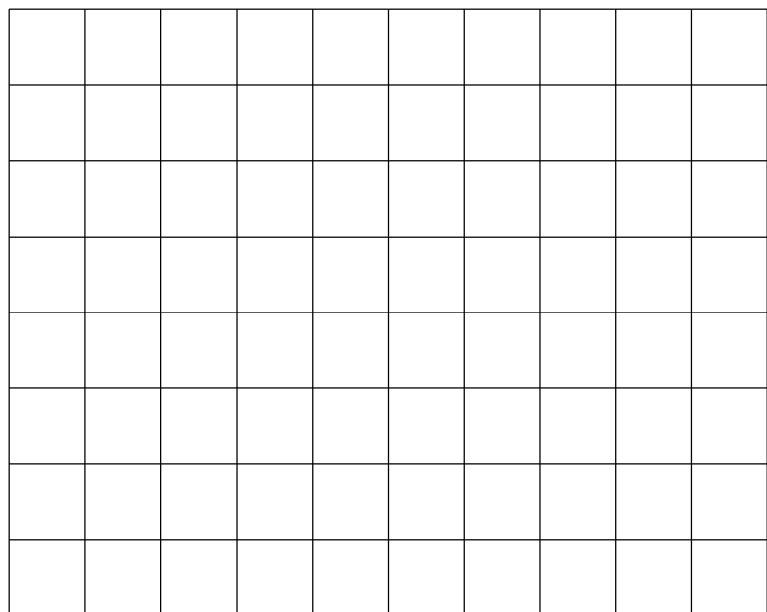


Fig. 15.2.3: Phase shift,  $U_{tot}$  to  $U_R$

- Determine the phase shift in degrees, between the generator voltage and the voltage at the resistor from your drawing, or read the value from the oscilloscope screen.

Phase shift  $U_{tot}$  to  $U_R$ :

What angle corresponds to the measured phase shift?

## Practical Experiments

### Exercise 2: RC Series Circuit

- The relationships in an RC series circuit Fig. 15.2.4 are to be measured. The phase angle  $\varphi$  between generator voltage and the voltage across the resistor ( $U_R$ ), is  $46^\circ$ .
- Calculate the values of  $U_R$  and  $U_C$  using the phase angle  $\varphi$ .

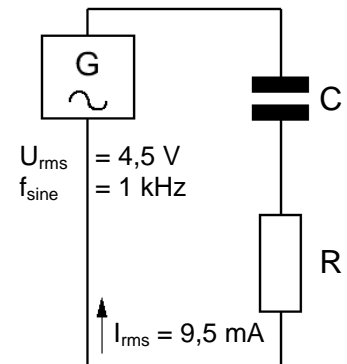


Fig. 15.2.4: RC series circuit

- Draw the vector diagram for the voltages  $U$ ,  $U_R$ ,  $U_C$  in Fig. 15.2.5.

Scale:  
1 cm = 1 V

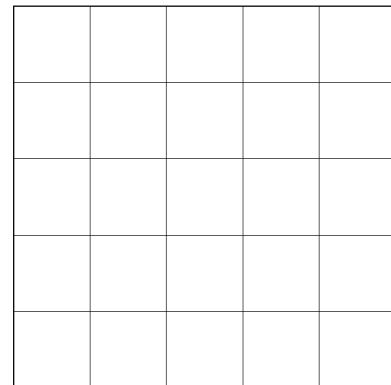


Fig. 15.2.5:  
U-Vector diagram

- Calculate the values of  $R$ ,  $X_C$ ,  $Z$  and  $C$ .
- The results from calculations will now be checked in a practical exercise. Assemble the RC series circuit in Fig. 15.2.4 on the Electronic Circuits Board. Use the following components:  $R = 330 \Omega$ ,  $C = 0,47 \mu\text{F}$ . Set the function generator to:  $U_{\text{rms}} = 4,5 \text{ V}$  ( $f_{\text{sine}} = 1 \text{ kHz}$ ).
- Measure the voltages and current in the circuit with a multimeter. Check the measured values against the results of calculation.

$U_R =$

$U_C =$

$I =$

## Practical Experiments

- Measure the phase angle  $\varphi$  on the oscilloscope. Display the voltages  $U$  and  $U_R$ . Draw the voltage waveform in the chart (Fig. 15.2.6).

**Oscilloscope settings:**  
 $X : 0,1 \text{ ms/div.}$   
 $Y_1 : 2 \text{ V/div., AC}$   
 $Y_2 : 2 \text{ V/div., AC}$

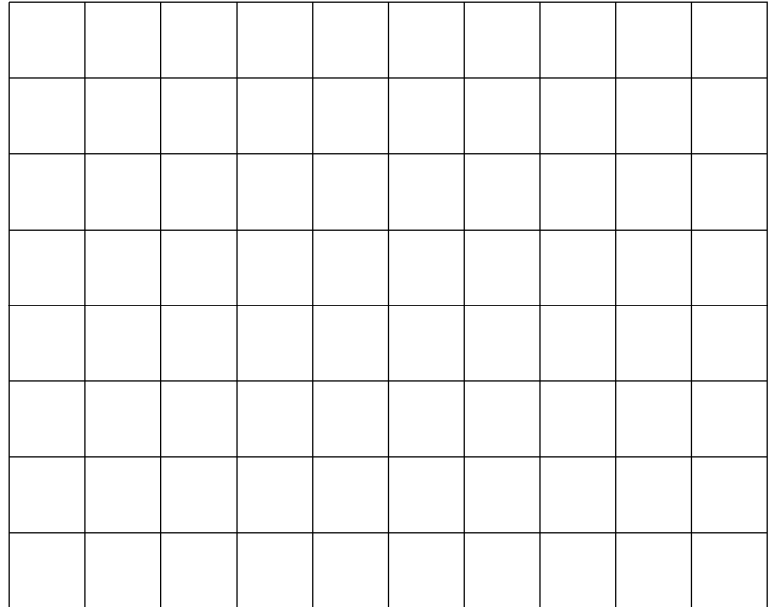


Fig. 15.2.6: Determining the phase angle

### Exercise 3: RLC Series Circuit

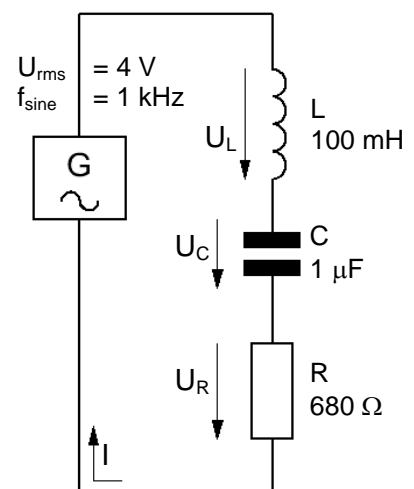
- Assemble the circuit in Fig. 15.2.7 on the Electronic Circuits Board.
- Set the function generator to an output voltage of  $U_{\text{rms}} = 4 \text{ V}$ ,  $f_{\text{sine}} = 1 \text{ kHz}$ .
- Measure the voltages across the components on a voltmeter.

$$U_{\text{rms}} = U_{\text{tot}} = 4 \text{ V} \quad ; \quad U_L =$$

$$U_C = \quad ; \quad U_R =$$

- Calculate the current flowing in the circuit. Check the calculation by measurement.

Fig. 15.2.7: RLC-Serienschaltung

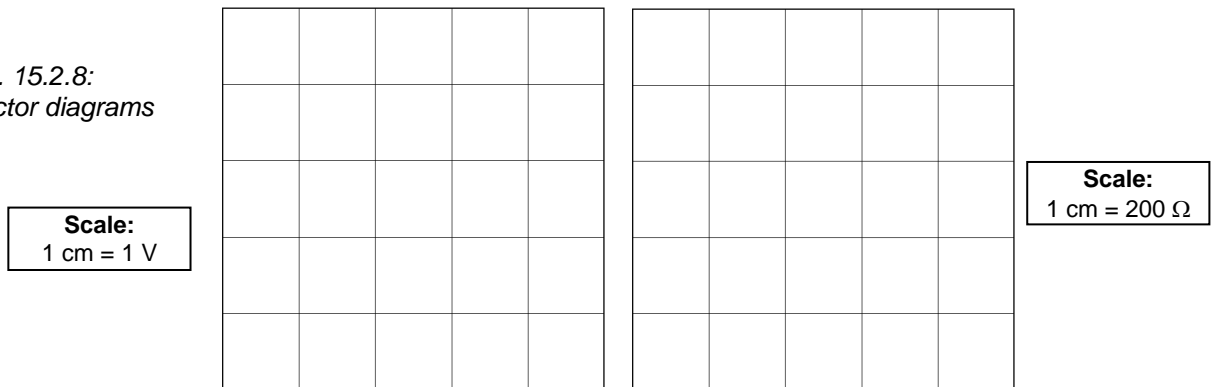


Measurement:  $I =$

## Practical Experiments

- From the measured values, calculate the reactances  $X_C$  and  $X_L$  and the resistance  $R$ .
- Draw the vector diagrams for the voltages ( $U_R$ ,  $U_C$ ,  $U_L$ ,  $U_{tot}$ ) and the resistances ( $R$ ,  $X_C$ ,  $X_L$ ,  $Z$ ) in Fig. 15.2.8.

Fig. 15.2.8:  
Vector diagrams



- Determine the impedance  $Z$  from the diagram and check the value by calculation using your measured values.

From the diagram:  $Z =$

Calculation:

- Mark the phase angle in the diagram. Calculate the phase angle from your measured values.

## Practical Experiments

- What changes are seen in the variables listed in table 15.2.9, when the frequency in the circuit of Fig. 15.2.7 is reduced from 1 kHz to 800 Hz ( $U_{\text{tot}} = \text{constant}$ )?

Indicate the tendency of each variable with arrows (except  $U_R$  and  $I$ ). Then, check your considerations by measurements and calculations. Enter the values in the table.

f ↓	$U_L$	$U_C$	$U_R$	$U_{\text{tot}} \leftrightarrow$	$I$	$X_L$	$X_C$	$R$	$Z$	$\phi$
800				4						
[Hz]	[V]				[mA]	[Ω]				[°]

Table 15.2.9: Characteristic quantities: tendencies, measurements and calculations

### 15.3 Parallel Circuits of Resistor, Capacitor and Coil

The use of vector diagrams and the calculation of characteristic quantities will now be practised with examples on an RLC parallel circuit.

**Note: A layout example for RLC circuits, will be found at the end of this section.**

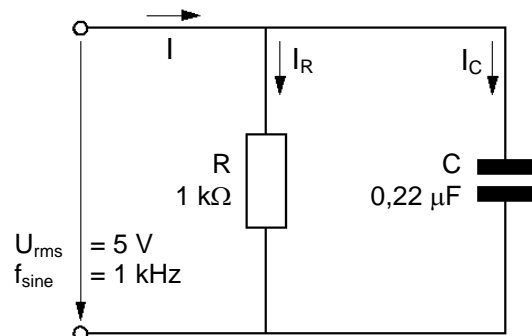
#### Exercise 1: RC Parallel Circuit

- Assemble the circuit in Fig. 15.3.1 on the Electronic Circuits Board.
- Set the function generator to an output voltage of  $U_{\text{rms}} = 5 \text{ V}$ ,  $f_{\text{sine}} = 1 \text{ kHz}$ .
- Using an ammeter measure the apparent current  $I$ , the reactive current  $I_C$  and the active current  $I_R$  in the circuit.

$$I = \quad ; \quad I_C =$$

$$I_R =$$

Fig. 15.3.1:  
RC parallel circuit

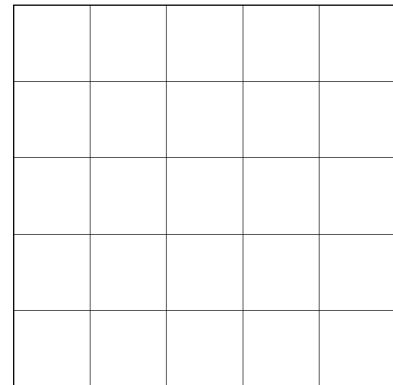




## Practical Experiments

- Draw the vector diagram for the currents in Fig. 15.3.2.
- Calculate the phase angle  $\varphi$  from your values measured.

**Scale:**  
 1 cm = 2 mA



- Calculate the susceptance  $B_C$ , the conductance  $G$  and the admittance value  $Y$  from the currents measured.

Fig. 15.3.2:  
I-vector diagram

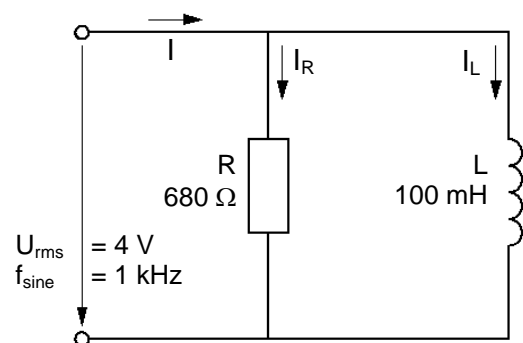
### Exercise 2: RL Parallel Circuit

- Assemble the RL circuit in Fig. 15.3.3 on the Electronic Circuits Board.
- Set the function generator to an output voltage of  $U_{\text{rms}} = 4 \text{ V}$ ,  $f_{\text{sine}} = 1 \text{ kHz}$ .
- Using an ammeter measure the currents in the parallel branches.

$I_R = \dots\dots\dots$  ;  $I_L = \dots\dots\dots$

- Calculate the total current  $I$  (apparent current) from the measured values of active current  $I_R$  and reactive current  $I_L$ .

Fig. 15.3.3: RL parallel circuit



## Practical Experiments

- Check your calculated values for the apparent current  $I$  by measurement.

$$I_{\text{meas.}} =$$

- From your measured values, calculate the susceptance  $B_L$  and the conductance  $G$ .

- From the susceptance and frequency, calculate the inductance of the coil.

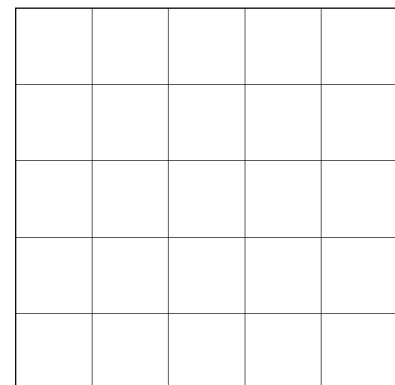
- Draw the vector diagram of susceptance and conductance values, in Fig. 15.3.4.

- Determine the value of admittance  $Y$  from the diagram.

$$Y =$$

- Calculate the phase angle  $\varphi$ .

**Scale:**  
 1 cm = 0,5 mS



- How much power is consumed by the circuit?

*Fig. 15.3.4: Conductance vector diagram*

Active power  $P$  :

Reactive power  $Q_L$  :

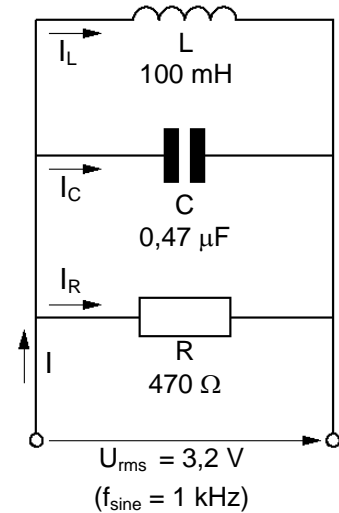
Apparent power  $S$  :

## Practical Experiments

### Exercise 3: RLC Parallel Circuit

- Calculate the currents  $I_R$ ,  $I_C$  and  $I_L$  in the circuit shown in Fig. 15.3.5. Use the given components.

Fig. 15.3.5:  
RLC parallel circuit



- Assemble the RLC parallel circuit in Fig. 15.3.5 on the Electronic Circuits Board. Set the function generator to an output voltage of  $U_{rms} = 3,2 \text{ V}$ ,  $f_{sine} = 1 \text{ kHz}$ .
- Check your calculations by measurement on an ammeter.

$$I_R = \dots\dots\dots ; \quad I_L = \dots\dots\dots ; \quad I_C = \dots\dots\dots$$

- Draw the vector diagram of currents in Fig. 15.3.6. From your drawing, determine the apparent current (total current)  $I$ .

Result:  $I =$

- Check the value of  $I$  from the drawing by a calculation using the measured values of current.

**Scale:**  
1 cm = 2 mA

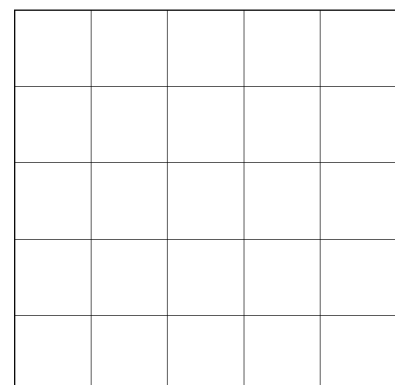


Fig. 15.3.6: Current  
vector diagram

- Calculate the phase shift between apparent current  $I$  and reactive current  $I_C$ .

How much active power  $P$ , is dissipated in the RLC circuit?

- Calculate the value of apparent power  $S$ , using  $P$  and the phase angle  $\varphi$ .
- How does the RLC circuit in Fig. 15.3.5 load the AC voltage source, capacitive or inductive? Give reasons for your answer.

### 15.4 Exercise Assembly – Example for an RLC Parallel Circuit

Fig. 15.4.1 shows one possible time-saving layout of the components for the exercises on the combination of active and reactive resistances. Components and the arrangement of plugs, provide an easy access for connecting the test instruments. Fig. 15.4.1 shows a current measurement in the parallel branch of a coil  $L = 100$  mH and the voltage measurement at the output of the AC voltage source.

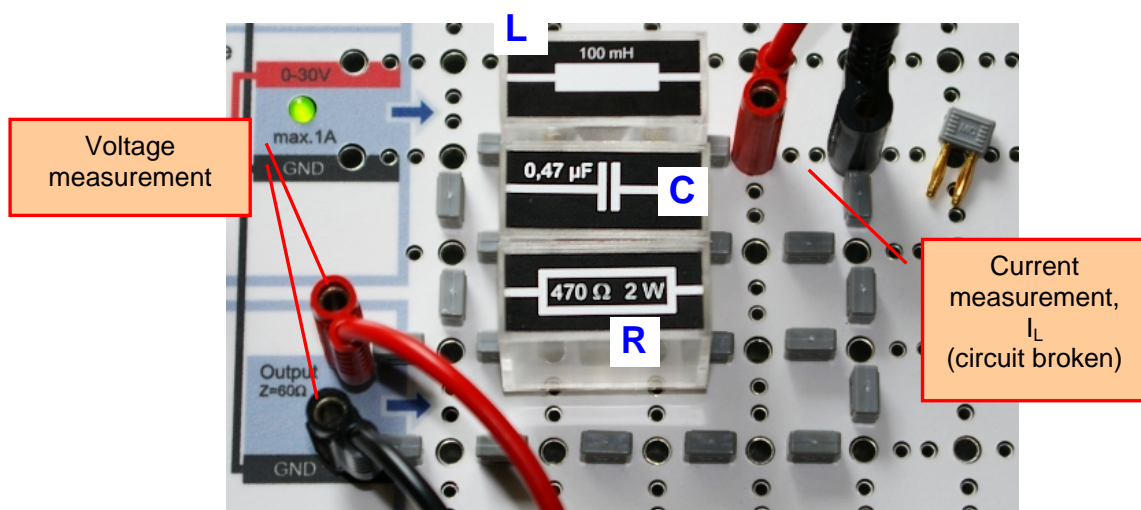


Fig. 15.4.1: Example of an exercise layout

## 16. Oscillating Circuit

### 16.1 Generation of a Sinusoidal Oscillation and Resonance

If a charged capacitor C is bridged by an active resistor, current flows for a specific time. The same applies to a coil L, in which a magnetic field has built up. Both phenomena are due to the energy that has been stored, i.e. the electrical field of the capacitor and the magnetic field in the coil. If now, both components are connected together, the capacitor is able to pass its stored energy to the coil L, and vice versa (Fig. 16.1.1). The discharge current from the capacitor generates a magnetic field in the coil. When the capacitor has fully discharged, the current flow stops and the collapse of the magnetic field in the coil, produces a current that charges the capacitor with the opposite polarity. When the magnetic field in the coil has completely decayed, the capacitor can again discharge and the process is repeated (Fig. 16.1.1). Thus at both components, a self-generated periodic oscillation is produced. Capacitor C and coil L form an **oscillating circuit**.

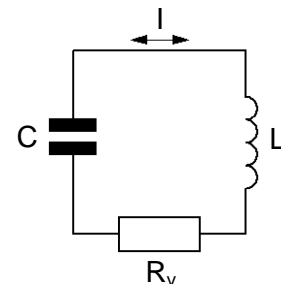


Fig. 16.1.1: L and C form an oscillating circuit

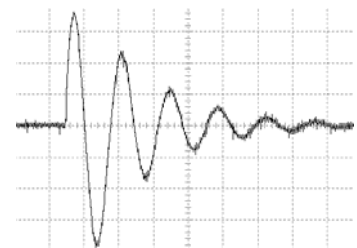


Fig. 16.1.2: Oscilloscope display of damped sinusoidal oscillation

The current controlling this alternating exchange of energy – i.e. the oscillation – is sinusoidal. However, active power losses do occur in the capacitor, the coil and also with less effect, in the connecting cables (symbolised in Fig. 16.1.1 by the equivalent resistor,  $R_v$ ). Therefore, power in the form of heat, is dissipated in the air surrounding the components. This causes a continual loss of energy and the amplitude of the oscillations become smaller. This is known as a **damped oscillation** (Fig. 16.1.2).

If suitable energy is applied to the oscillating circuit, sufficient to compensation for the losses, the circuit then continues to oscillate at a constant amplitude and frequency. The circuit is then said to be at **resonance**. The **resonant frequency  $f_o$**  of the oscillating circuit depends on the capacitance of the capacitor C and the inductance of the coil L. When the circuit oscillates at its resonant frequency, both coil and capacitor must exchange the same magnitude of energy. The frequency adjusts itself, so that the two reactances  $X_L$  and  $X_C$  have the same value. At resonance, the following equation applies:

$$X_L = X_C \Rightarrow 2\pi \cdot f_o \cdot L = \frac{1}{2\pi \cdot f_o \cdot C} \Rightarrow \boxed{f_o = \frac{1}{2\pi \sqrt{L \cdot C}}}$$

## Practical Experiments

### 16.2 Series and Parallel Oscillating Circuits

Depending on how it is connected in a circuit, the LC group in Fig. 16.1.1 can be used as a **series** or **parallel oscillating circuit**.

**Series resonance:** Fig. 16.2.1 shows a **series oscillating circuit**, where the coil and capacitor are connected in series. Capacitor and coil 'share' the generator voltage. The series loss resistance  $R_v$  is very small and consists mainly of the ohmic resistance of the coil windings (Fig. 16.2.1).

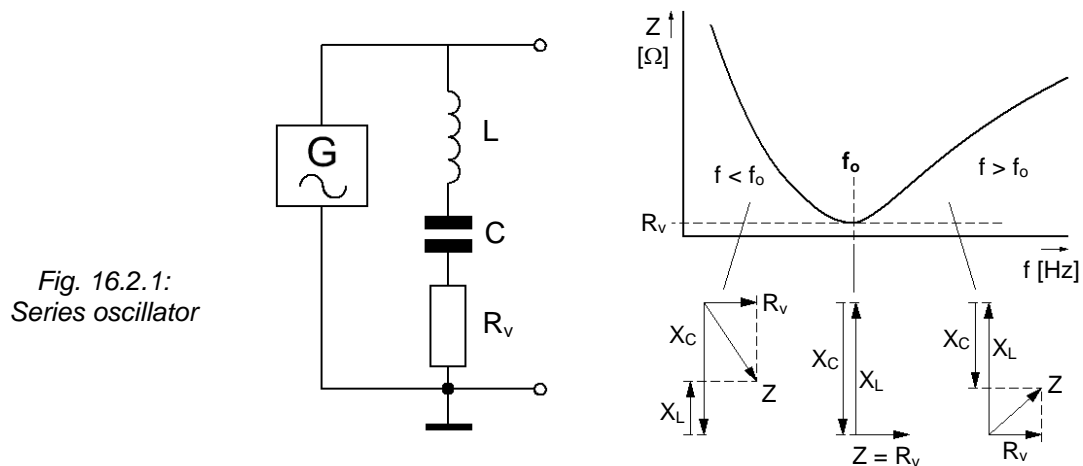


Fig. 16.2.1:  
Series oscillator

If the AC voltage generator supplies a sine-wave voltage below the resonant frequency ( $f < f_0$ ), then the reactance  $X_C$  of the capacitor is the dominant factor. A series oscillating circuit is thus capacitive. The higher the frequency, the more  $X_L$  increases, whilst the impedance  $Z$  becomes smaller (Fig. 16.2.1, vector diagram, left).

At the resonant frequency  $f_0$ , the reactances cancel each other. The small, pure ohmic loss resistance  $R_v$  ( $Z = R_v$ ) determines the flow of current in the circuit (Fig. 16.2.1, right). In the case of resonance in a series circuit, current and voltage are in phase (Fig. 16.2.1, vector diagram, centre).

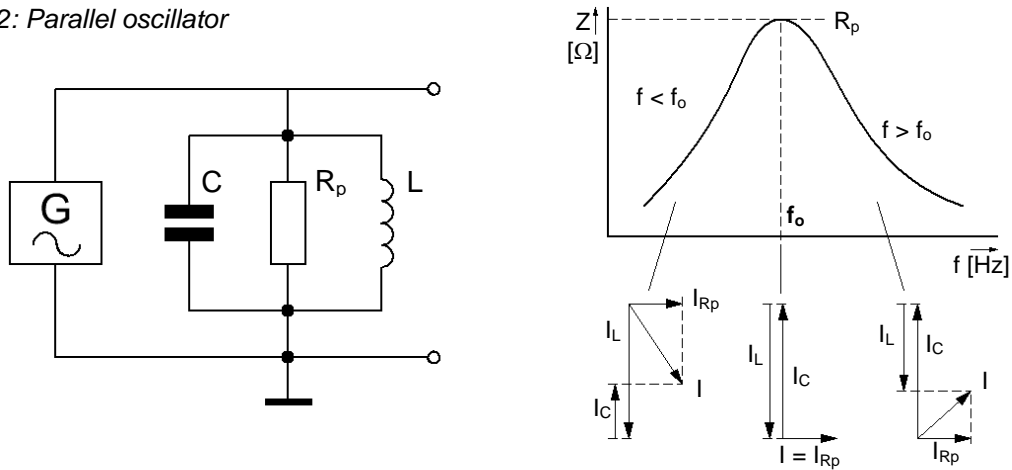
If the frequency is increased above resonance ( $f > f_0$ ), then the series oscillating circuit is inductive, because the reactance of the coil ( $X_L$ ) dominates over the reactance of the capacitor ( $X_C$ ) (Fig. 16.2.1, vector diagram, right).

The curve shown in Fig. 16.2.1,  $Z = f(f)$  is known as the **resonance curve** of the oscillating circuit.

**Parallel resonance:** In a parallel oscillating circuit, there are other electrical relationships as in a series circuit because the generator voltage supplies all components, equally. The ohmic losses at the coil and capacitor are combined in the equivalent resistance  $R_p$  that is assumed to be in parallel with the coil and capacitor (Fig. 16.2.2, left).

If the AC voltage generator supplies a sine-wave voltage below the resonant frequency ( $f < f_0$ ), then the current  $I_L$  in the coil is greater than  $I_C$  in the capacitor. A parallel oscillating circuit in this frequency range, is inductive. If the frequency is increased, then  $I_L$  reduces and  $I_C$  increases (Fig. 16.2.2, vector diagram, left).

Fig. 16.2.2: Parallel oscillator



At the resonant frequency  $f_o$ , the reactances and reactive currents cancel each other. The high, pure ohmic loss resistance  $R_p$  ( $Z = R_p$ ) determines the flow of current in the circuit (Fig. 16.2.2, vector diagram, centre). In the case of resonance in a parallel oscillating circuit, current and voltage are also in phase. A parallel circuit oscillating at its resonant frequency exhibits its maximum resistance.

If the frequency is increased above resonance ( $f > f_o$ ), then a parallel oscillating circuit is inductive because the reactive current in the capacitor ( $I_C$ ) dominates over the current in the coil ( $I_L$ ) (Fig. 16.2.2, vector diagram, right).

The resonance curves show clearly the significant difference between series and parallel resonance: If the circuit is excited at a frequency close to the resonant frequency, then the impedance  $Z$  of a series circuit falls to a minimum. On the other hand, in a parallel oscillating circuit, the impedance reaches its maximum value in the region of the resonant frequency.

The response of the resonance curve for an oscillating circuit, is determined mainly by the active power losses occurring in the circuit. Fig. 16.2.3 shows the tendency, when  $R_p$  in a parallel oscillating circuit increase as a result of increased ohmic losses.

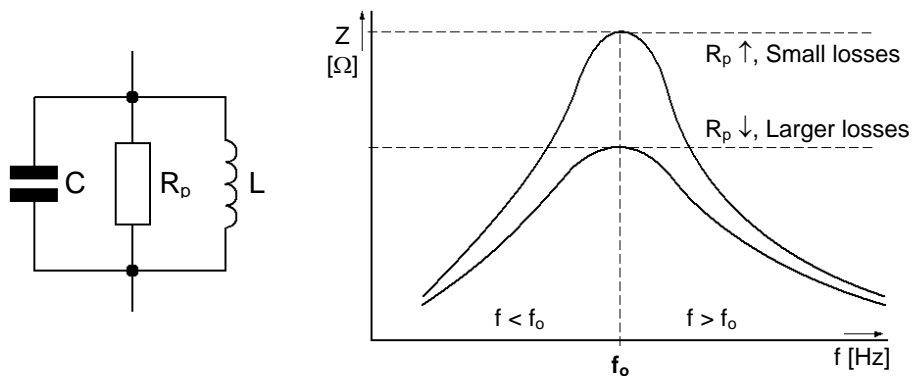


Fig. 16.2.3: Effect of active power losses on the resonance curve

## Practical Experiments

### 16.3 Practical Proof of Resonance Curves

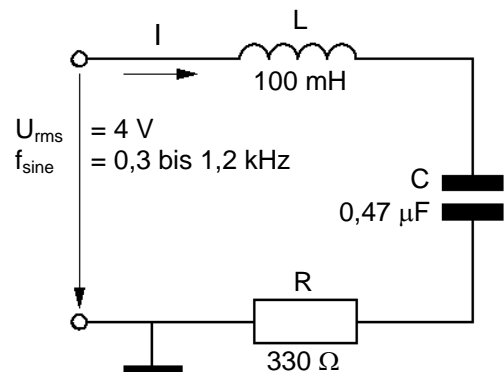
The resonance response of oscillating circuits will now be proved with practical exercises.

**Note:** Layout examples on the Electronic Circuits Board for the measurements in oscillating circuits, will be found after exercise 2.

#### Exercise 1: Series Oscillating Circuit

- Assemble the oscillating circuit in Fig. 16.3.1 on the Electronic Circuits Board.
- Calculate the resonant frequency of the series oscillating circuit.

Fig. 16.3.1:  
Series oscillating circuit



- Enter the calculated value of resonant frequency  $f_0$  in the empty square of frequency values in table 16.3.2.
- Set the function generator to an output voltage of  $U_{\text{rms}} = 4 \text{ V}$ , at a starting frequency of  $f_{\text{sine}} = 300 \text{ Hz}$ . Measure the voltage on a voltmeter.
- At the given frequencies, measure the current flow on an ammeter. Enter the values in the table.

Table 16.3.2: Measured values, series oscillating circuit

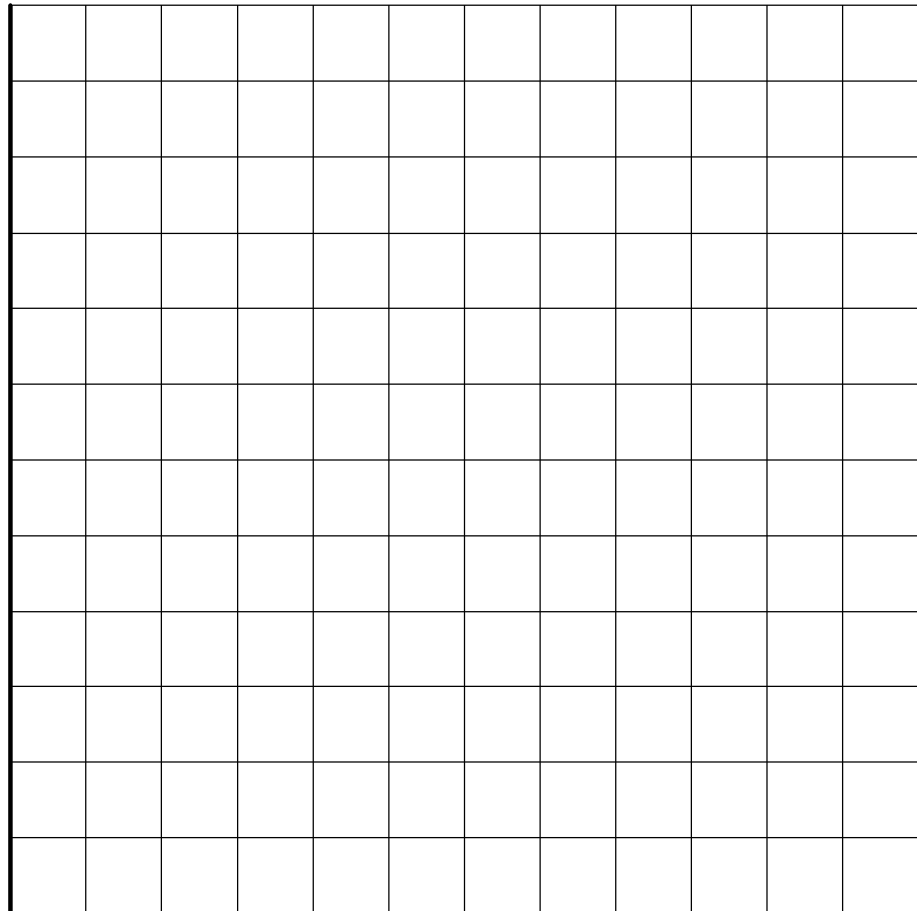
	f [kHz]	0,3	0,4	0,6		0,8	0,9	1	1,2
330 Ω	I [mA]								
	Z [kΩ]								
220 Ω	I [mA]								
	Z [kΩ]								

- Calculate the values of impedance Z and enter the results in the table.
- Draw the resonance curve  $Z_{330 \Omega} = f(f)$  in the chart (Fig. 16.3.3) for this series oscillating circuit.
- Exchange the resistor R in the circuit of Fig. 16.3.1 with one of  $R = 220 \Omega$ .
- Repeat the series of measurements for table 16.3.1 and enter the new values in the table.
-



## Practical Experiments

- Draw the resonance curve  $Z_{220\ \Omega} = f(f)$  in the chart (Fig. 16.3.3) for the modified series oscillating circuit.



*Fig. 16.3.3:  
Resonance curves,  
series oscillating  
circuit*

- What properties has the impedance  $Z$  at the resonant frequency  $f_0$ ?
- The series oscillating circuit of Fig. 16.3.1 includes a resistor (330 or 220  $\Omega$ ) for limiting the current flow. What is the actual value of loss resistance  $R_v$  in the circuit?
- Indicate on the curves you have drawn, the areas where the oscillating circuit acts as a capacitance and as an inductance.

## Practical Experiments

### Exercise 2: Parallel Oscillating Circuit

- Assemble the circuit in Fig. 16.3.4 on the Electronic Circuits Board.

**Note: Resistor R = 330 Ω is used only for current limiting and is not part of the parallel oscillating circuit.**

- Set the function generator to an output voltage of  $U_{rms} = 4\text{ V}$ , at a starting frequency of  $f_{sine} = 300\text{ Hz}$ . Measure the voltage on a voltmeter.

- At the given frequencies, measure the current flow on an ammeter. Enter the values in table 16.3.5.

Fig. 16.3.4: Parallel oscillating circuit

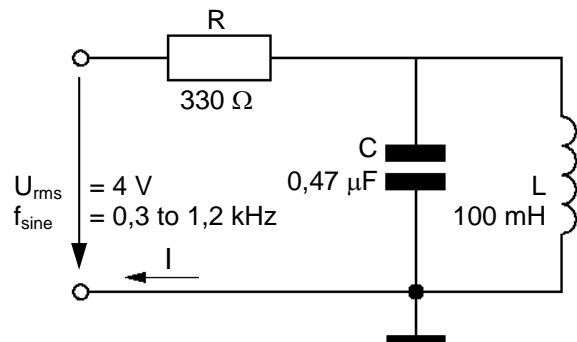


Table 16.3.5: Measured values, parallel oscillating circuit

f [kHz]	0,3	0,4	0,5	0,6	0,734	0,8	0,9	1	1,2
I [mA]									
Z [kΩ]									

- Calculate the values of impedance Z and enter the results in the table.

- Draw the resonance curve  $Z = f(f)$  in the chart (Fig. 16.3.6) for this parallel oscillating circuit.

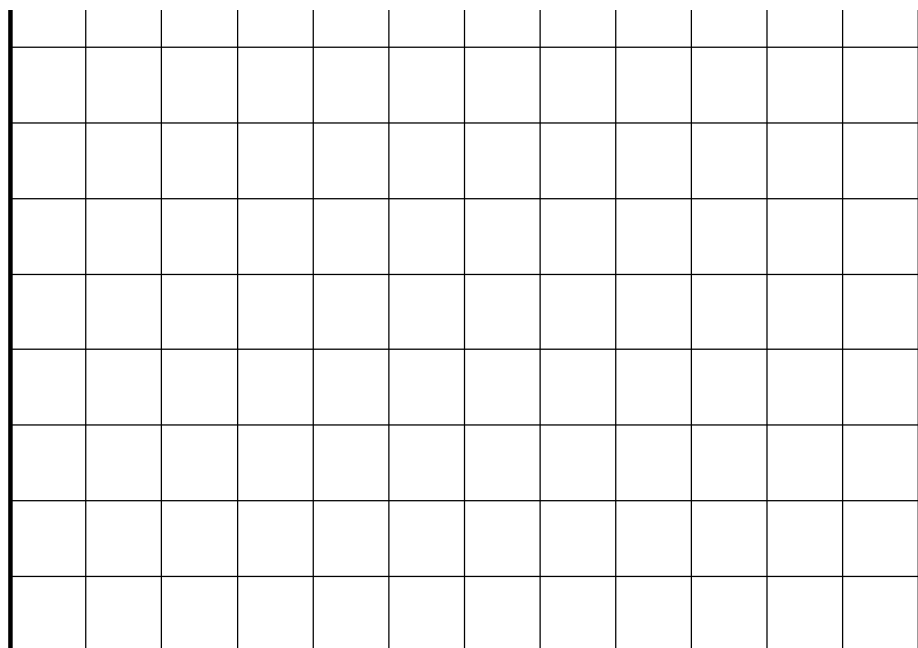


Fig. 16.3.6: Resonance curve, parallel oscillating circuit

- How do the currents  $I_L$  and  $I_C$  respond at resonance of the parallel oscillating circuit?

- Measure the currents  $I_L$  and  $I_C$  at resonance.

$I_{L \text{ Resonance}} = \dots\dots\dots$  ;  $I_{C \text{ Resonance}} = \dots\dots\dots$

**Exercise Layout, Series Oscillating Circuit**

Fig. 16.3.7 shows the exercise layout for the series resonant circuit. The illustration shows measurement of the current  $I$  at resonance. For this, the circuit is broken.

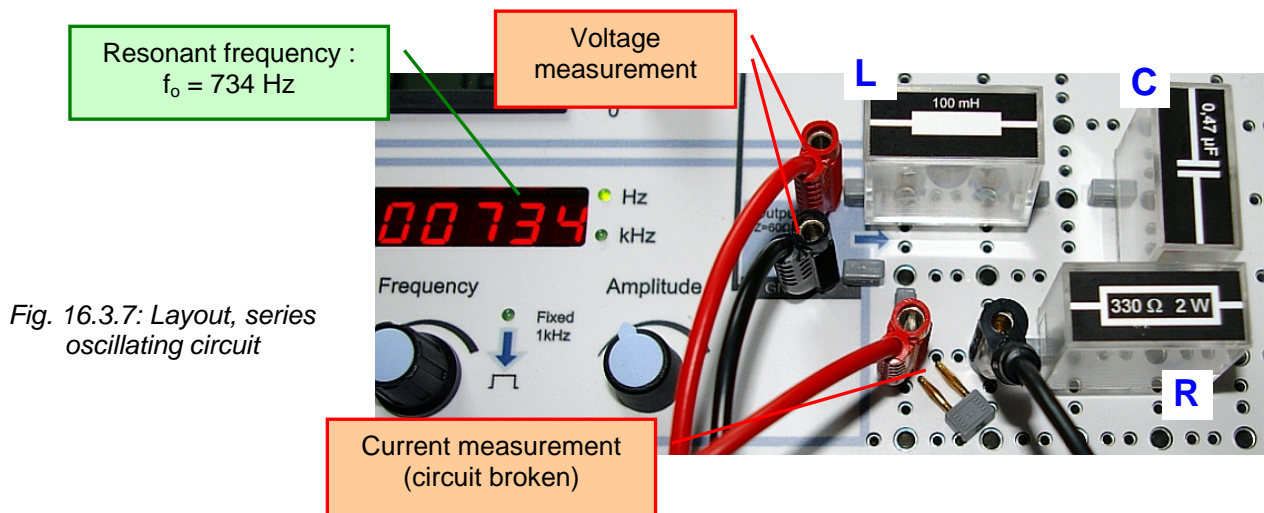


Fig. 16.3.7: Layout, series oscillating circuit

**Exercise Layout, Parallel Oscillating Circuit**

Fig. 16.3.8 shows a suggested layout for the exercise on a parallel resonant circuit. The capacitor and coil branches can be isolated for the current measurements at resonance.

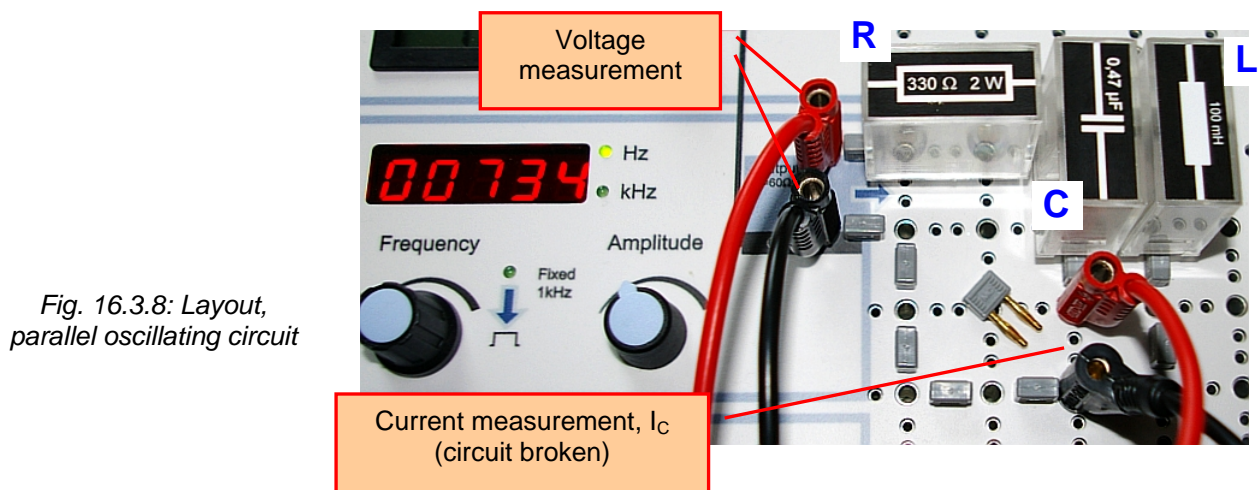


Fig. 16.3.8: Layout, parallel oscillating circuit

### Exercise 3: Generating Damped Oscillations

**Circuit description:** The circuit shown in Fig. 16.3.9 for generating an oscillation, consist of 3 parts:

The capacitors  $C_2 = C_3 = 10 \text{ nF}$  together with the coil  $L = 100 \text{ mH}$ , form a parallel oscillating circuit, where the damped sinusoidal oscillation can be measured. To initiate oscillation, the resonant circuit must periodically be 'excited' by feeding energy to the circuit.

This excitation is the task of the RC-element  $C_1/R_1$ . It converts the positive square-wave pulse ( $U_S = 6 \text{ V}$ ,  $f = 250 \text{ Hz}$ ) applied to the input of the circuit, to needle pulses that can be measured as  $U_{R1}$  (c.f. section 13.3.2).

Only part of the low-energy needle pulses ( $U_{R1}$ ) is effective at the oscillating circuit due to the relatively high-value coupling resistor  $R_2 = 22 \text{ k}\Omega$  ( $R_2$  and the oscillating circuit form a voltage divider for  $U_{R1}$ ).

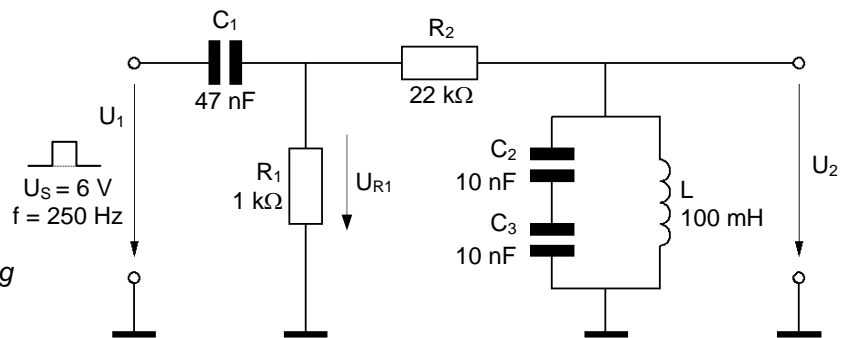


Fig. 16.3.9: Circuit for generating damped oscillations

- Assemble the circuit in Fig. 16.3.9 on the Electronic Circuits Board. Break the connection between the RC-element and oscillating circuit by removing the coupling resistor  $R_2$ .

**Note: A suggested layout of the components on the Electronic Circuits Board will be found at the end of this section.**

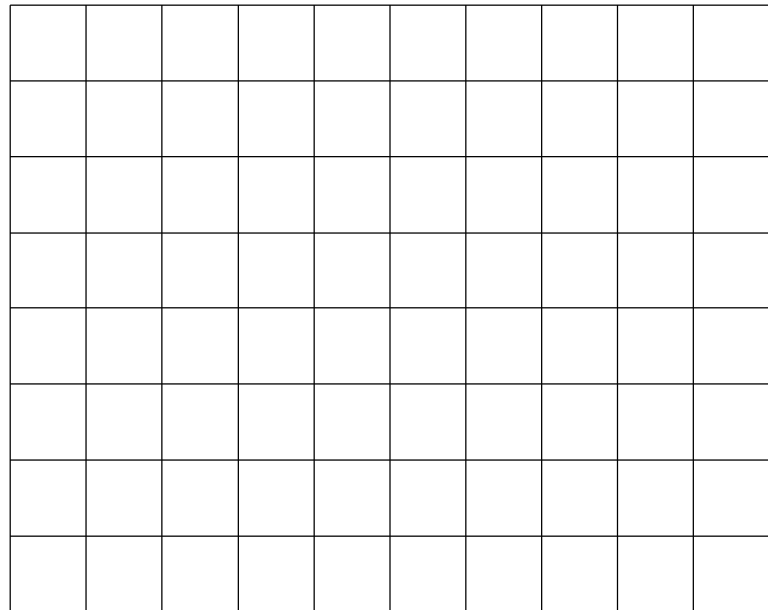
- Set the input voltage  $U_1$  at the function generator to  $U_p = 6 \text{ V}$ ,  $f = 250 \text{ Hz}$ .

First, a check must be made to ensure that needle pulses are formed at  $R_1$  as required.

- Display  $U_1$  and  $U_{R1}$  on the oscilloscope. Adjust the controls on the oscilloscope so that at least one period of the square-wave voltage is displayed.

- Draw the signal waveform in the chart (Fig. 16.3.10).

**Oscilloscope settings:**  
 X : 0,4 ms/ div.  
 Y<sub>1</sub> : 5 V/ div., DC  
 Y<sub>2</sub> : 2 V/ div., DC



*Fig. 16.3.10: Generation of needle pulses*

- Switch off the function generator and complete the circuit with the coupling resistor  $R_2 = 22 \text{ k}\Omega$ .
- Calculate the resonant frequency  $f_o$  of the oscillating circuit.

- Display  $U_{R1}$  and  $U_2$  on the oscilloscope. Adjust the controls on the oscilloscope so that at least one complete period of  $U_{R1}$  (needle pulses) is displayed.

**Note: It should now be possible to display damped oscillations on the oscilloscope, at the output of the circuit ( $U_2$ ).**

- Draw the signal waveform in the chart (Fig. 16.3.11).
- Measure the periodic time of the damped oscillation and from this, calculate the actual resonant frequency  $f_o$ . Optimise the display of the oscillation on the oscilloscope. Compare the measured resonant frequency with that calculated.

T measured:

**Oscilloscope settings:**  
X : 0,4 ms/ div.  
Y<sub>1</sub> : 5 V/ div.  
Y<sub>2</sub> : 0,5 V/ div.

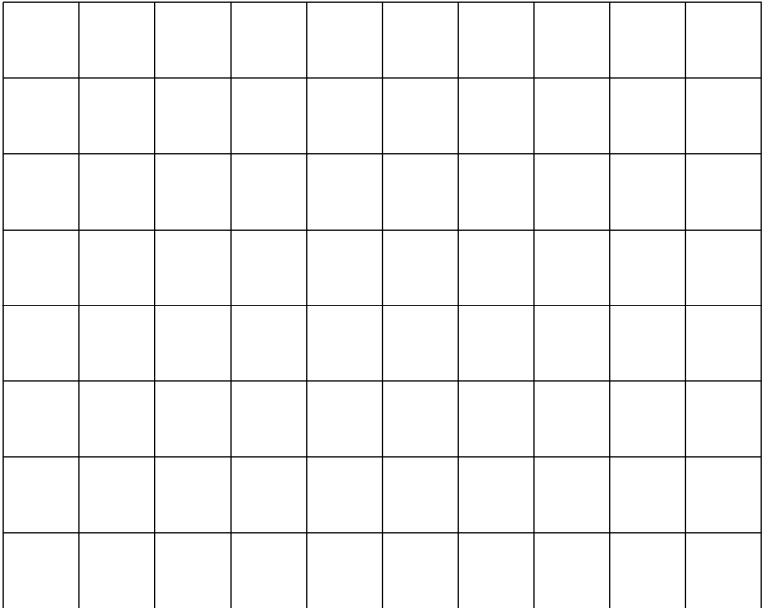


Fig. 16.3.11: Generation of damped oscillations

- What change do you expect when one of the capacitors C<sub>2</sub>/C<sub>3</sub> is removed and replaced by a bridge? Check your answer by measurements.

- What effect do you expect from a larger coupling resistor R<sub>2</sub> = 100 kΩ? Check your answer by measurement.

**Exercise Layout, Damped Oscillation**

Fig. 16.3.12 shows the exercise layout corresponding to the circuit of Fig. 16.3.9 for generating damped oscillations. The illustration shows the second measurement required on the oscilloscope. To reduce the amount of re-connection, a 2 mm connection lead is used.

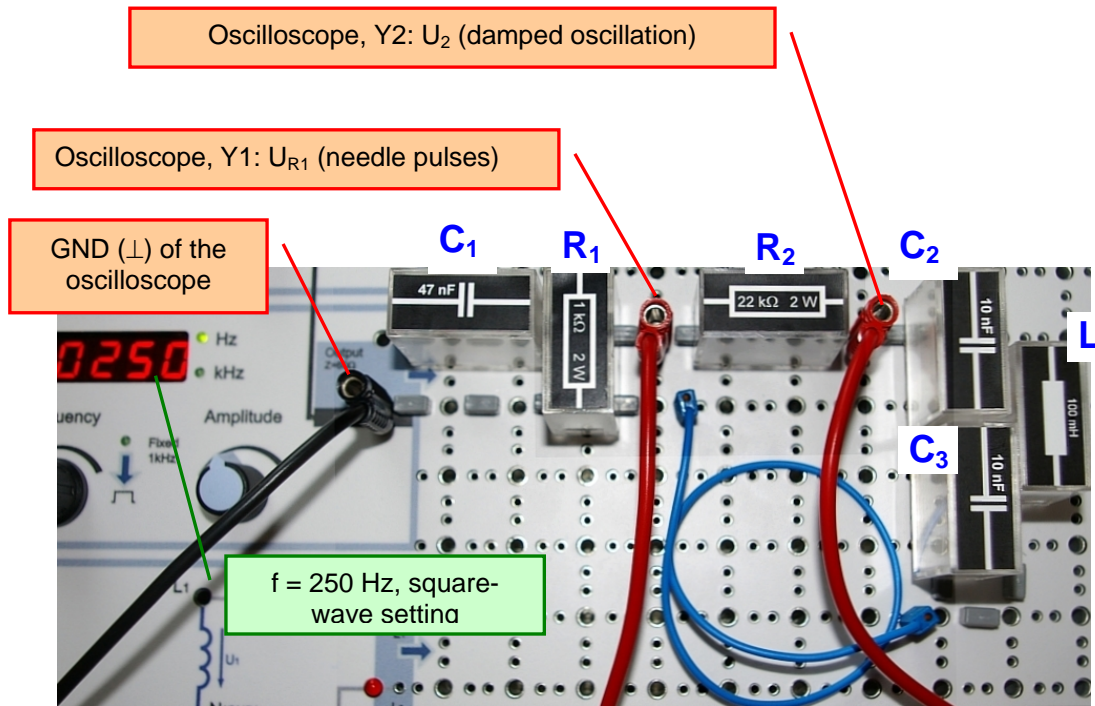


Fig. 16.3.12: Layout, Damped oscillation“

## 17. RLC Filter Circuit

A circuit with a frequency-dependent transfer response, is known as a **Filter**. The amplitude of a sinusoidal input voltage ( $U_1$ ) is more, or less, reduced depending on the frequency of the input and is available at the output ( $U_2$ ). This type of circuit is used to suppress unwanted components of a complex mixture of frequencies (frequency spectrum, signal voltages with different frequencies).

Fig. 17.1: Frequency response of a filter

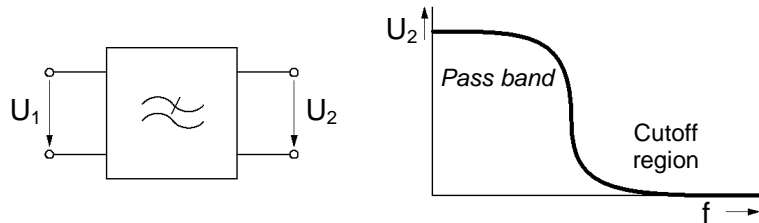


Fig. 17.1 shows the filtering principle of the frequency response of a so-called low-pass. Alternating voltages in the low-frequency range, are allowed to pass through the circuit with little or no, attenuation to the output of the circuit ( $U_2$ ). This range of frequencies is known as the **pass band** of the filter. In contrast, the **cutoff region** specifies the range (in this case), of higher frequencies that are blocked (or heavily attenuated) and no signal (or very little) reaches the output.

### 17.1 Transfer Characteristics of Filters

In order to describe the frequency response of filters, the junction of pass band and cutoff region must be clearly defined. For this reason, the **cutoff frequency**  $f_{cut}$  of the filter (Fig. 17.1.1) is defined as the point at which the output voltage of the filter is 0,707-times the input voltage.

$$U_2 = \frac{1}{\sqrt{2}} \cdot U_1 = 0,707 \cdot U_1$$

In many cases, a filter has the task of allowing a range of frequencies to pass through the filter (**bandpass**) or to suppress a range of frequencies (**bandstop**, Fig. 17.1.2). In the frequency response of such circuits, there are 2 limit frequencies, the upper ( $f_{hi}$ ) and the lower cutoff frequency ( $f_{lo}$ ). The range of frequencies between these 2 cutoff frequencies is known as the **bandwidth**  $b$  of the filter. **Bandpass** and **bandstop** filters are realised with oscillating circuits. This make use of the properties of

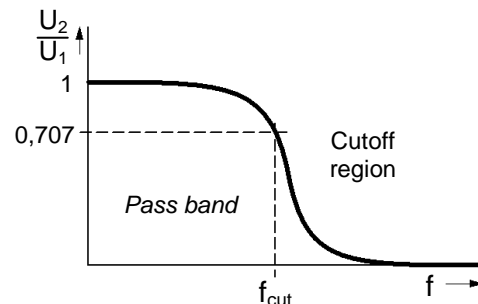


Fig. 17.1.1: Definition of the cutoff frequency  $f_{cut}$

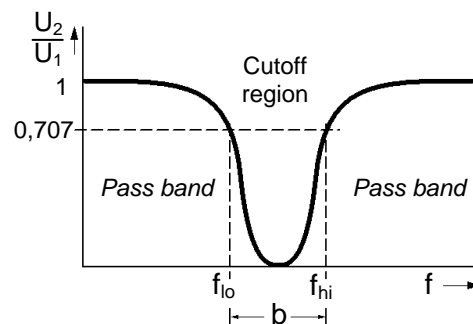


Fig. 17.1.2: Definition of upper and lower cutoff frequencies and bandwidth



## Practical Experiments

the low and high impedances in the vicinity of the resonant frequency  $f_0$ .

There are 4 types of frequency filter, summarised in Table 17.1.3 together with their DIN-symbol, transfer characteristics and RLC example circuits.

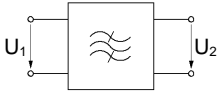
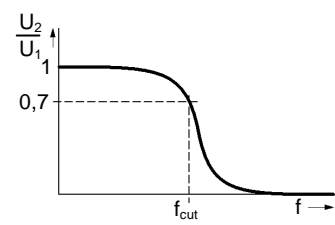
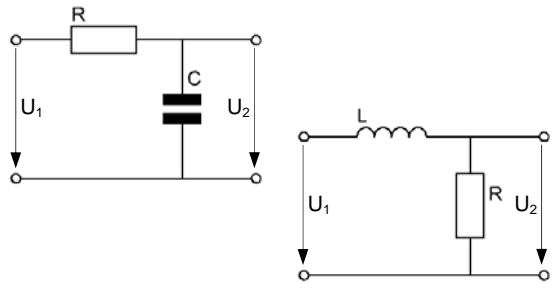
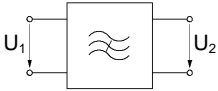
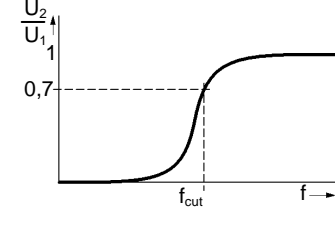
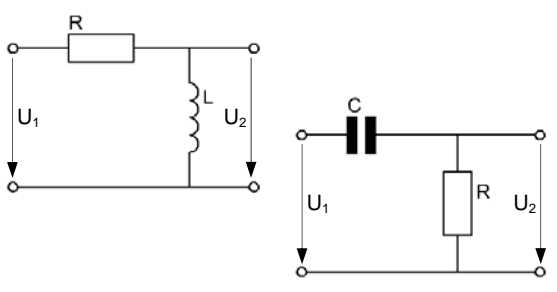
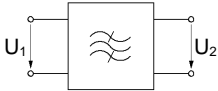
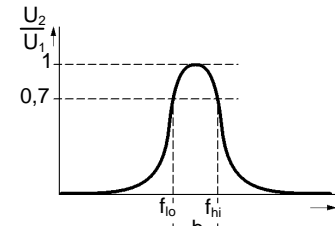
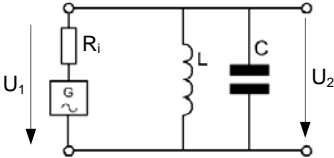
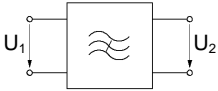
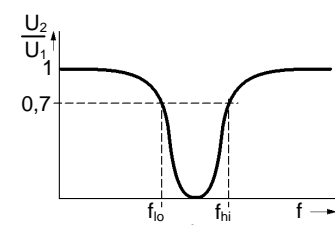

Filter type	Frequency response	RLC circuit example
<b>Low-pass</b> 		
<b>High-pass</b> 		
<b>Bandpass</b> 		
<b>Bandstop</b> 		

Table 17.1.3: Types of filter

For high- and low-pass filters, that use the RC or RL circuits shown in table 17.1.3, the following applies at the cutoff frequency,  $f_{cut}$ :

## Practical Experiments

$$\text{Reactance} = \text{Active resistance} \Rightarrow X = R \Rightarrow U_X = U_R$$

Therefore at the cutoff frequency, the phase shift  $\varphi$  between input and output voltage is  $45^\circ$ . The vector diagrams in Fig. 17.1.4 show that this applies, irrespective of which component is used for measuring the output voltage.

The ratio of output voltage to input voltage is confirmed because  $\sin \varphi = \cos \varphi = 0,707$ :

$$U_2 = \frac{1}{\sqrt{2}} \cdot U_1 = 0,707 \cdot U_1$$

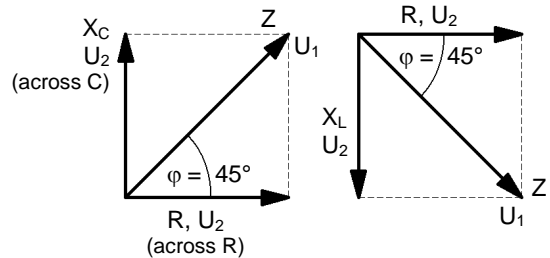


Fig. 17.1.4: Vector diagrams  $R$ ,  $X_C$  and  $R$ ,  $X_L$  at  $f_{cut}$

For low- and high-pass filters, the cutoff frequency  $f_{cut}$  is given by:

$$\text{RC-elements: } f_{cut} = \frac{1}{2\pi \cdot R \cdot C} \quad ; \quad \text{RL-elements: } f_{cut} = \frac{R}{2\pi \cdot L}$$

To improve the selectivity of filters, the edges of the pass band curve must be steeper. This is achieved in practice by modifying the basic circuits shown in table 17.1.3. More often, a completely different type of filter is used, for example quartz filters, ceramic filters or mechanical filters, to name a few.

### 17.2 Practical Proof of the Frequency Response of Filters

The transfer characteristics of filters will now be examined, using practical examples.

#### Exercise 1: High-pass Filter with RC-element

- Assemble the circuit in Fig. 17.2.1 on the Electronic Circuits Board.
- Calculate the cutoff frequency  $f_{cut}$  of the circuit, using nominal values. Round-up the result to a whole number.

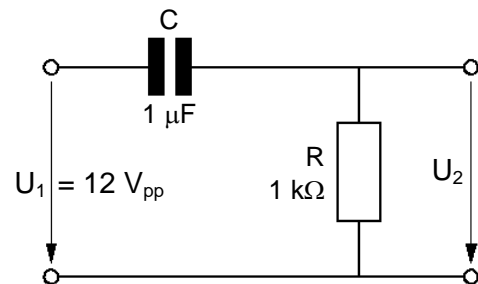


Fig. 17.2.1: RC-element as high-pass filter

**Note:** To be able to record the transfer characteristics for a frequency spectrum as wide as possible, values are measured in steps, at 10% of the cutoff frequency  $f_{cut}$ . In order to obtain a meaningful curve, it is necessary to plot the frequencies in the form  $f/f_{cut}$  referred to the cutoff frequency (Fig. 17.2.2).

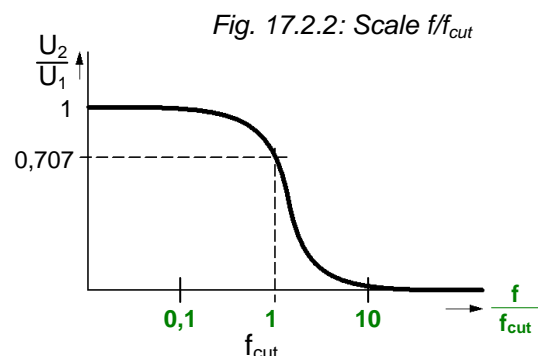


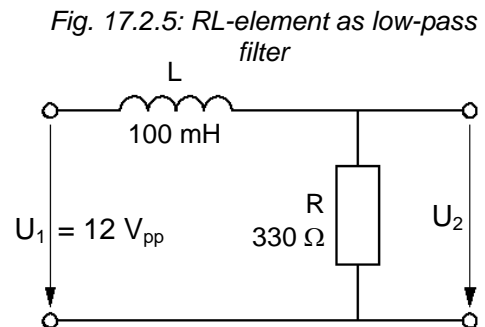
Fig. 17.2.2: Scale  $f/f_{cut}$



## Practical Experiments

### Exercise 2: Low-pass Filter with RL-element

- Assemble the circuit in Fig. 17.2.5 on the Electronic Circuits Board.
- Set the function generator for  $U_1$  to a sine-wave voltage of  $U_{pp} = 12\text{ V}$ .
- Calculate the cutoff frequency  $f_{cut}$ , using nominal values.



- How can the actual cutoff frequency  $f_{cut}$  be determined, using a voltmeter?
- Complete the measurements for determining the cutoff frequency  $f_{cut}$ .
- How can you explain the distinct difference between the calculated and measured values of  $f_{cut}$ ?
- The frequency response of the low-pass filter will now be recorded. Complete the line "f" in table 17.2.6. Enter here, the value of cutoff frequency determined by measurement with the voltmeter.
- Measure the voltage  $U_R = U_2$  at the frequencies entered in table 17.2.6, from the oscilloscope screen. Enter the values in the table.

**Note:** At each measurement, check the voltage of the function generator ( $U_1$ ) and correct if necessary (more significant at very low and higher frequencies).

Table 17.2.6: Measured values, RL low-pass filter

f					
$f/f_{cut}$	0,01	0,1	1	10	100
$U_2$ [V <sub>pp</sub> ]					
$U_2/U_1$					

## Practical Experiments

- Complete the line “ $U_2/U_1$ ” in table 17.2.6.
- Draw the curve of the frequency response in the chart (Fig. 17.2.7).


Fig. 17.2.7: Frequency response, RL low-pass

- How can you explain that at  $f_{cut}$ , less than 0,7-times the input voltage is available at the output?

### Exercise 3: Bandstop with LC Series Oscillating Circuit

- Assemble the circuit in Fig. 17.2.8 on the Electronic Circuits Board.
- Set the function generator for  $U_1$  to a sine-wave voltage of  $U_{rms} = 3\text{ V}$ .
- Calculate the resonant frequency  $f_0$  of the circuit from the nominal values. Round-up the result to a whole number.

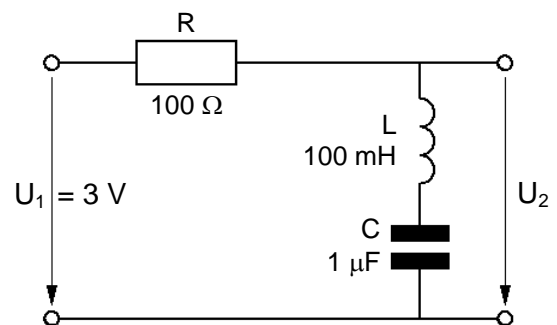


Fig. 17.2.8: Series oscillating circuit as bandstop

- Measure the voltage  $U_2$  at the frequencies given in table 17.2.9. Enter the values in the table.

## Practical Experiments

Table 17.2.9: Measured values, bandstop

f [kHz]	0,1	0,2	0,35	0,45	0,5	0,55	0,65	0,8	1
U <sub>2</sub> [V]									
U <sub>2</sub> /U <sub>1</sub>									

- Complete the line “U<sub>2</sub>/U<sub>1</sub>” in table 17.2.9.
- Draw the curve of the frequency response in the chart (Fig. 17.2.10).

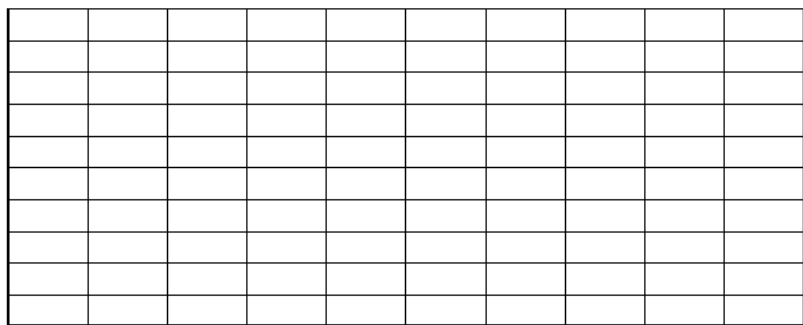


Fig. 17.2.10: Frequency response, bandstop

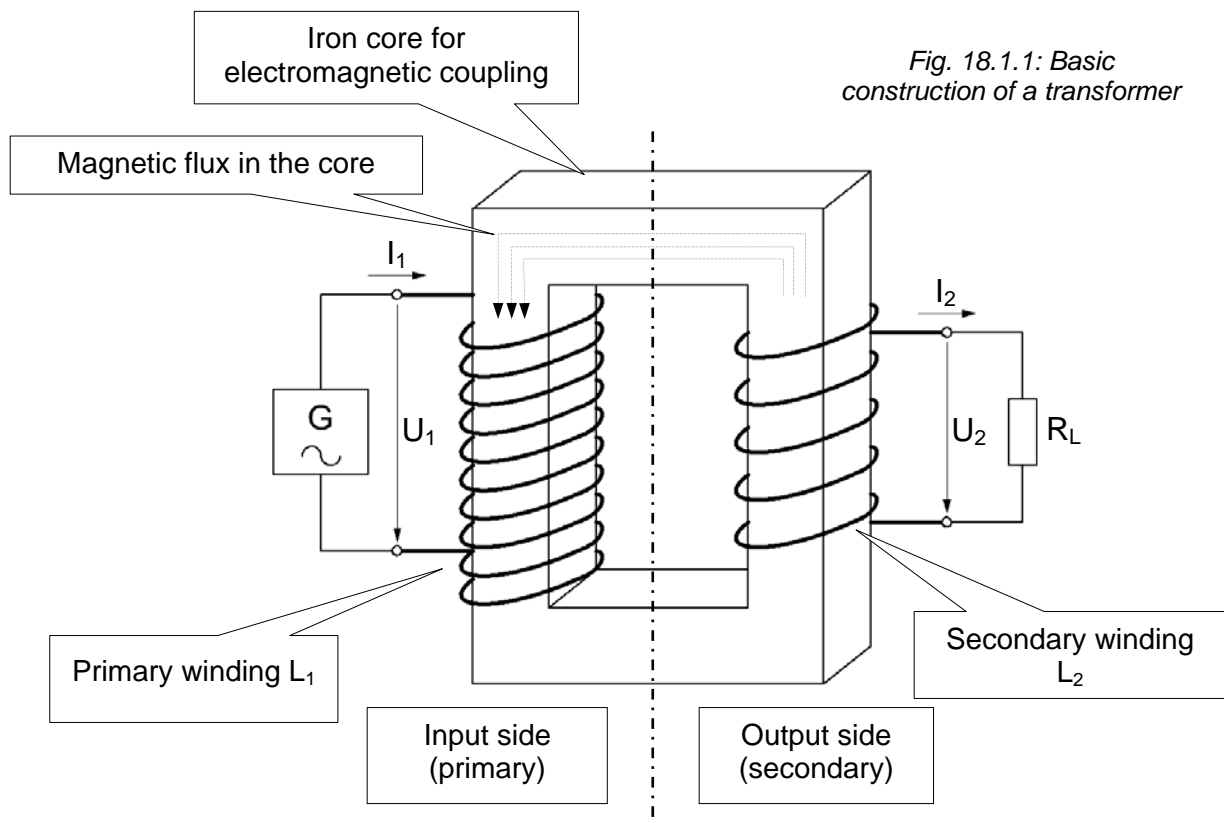
- Measure the upper and lower cutoff frequencies of the bandstop ( $f_{hi}$ ,  $f_{lo}$ ).
- What is the bandwidth  $b$ , of the bandstop filter?
- Mark the bandwidth and cutoff frequencies on the frequency response curve for the bandstop filter drawn in Fig. 17.2.10.

## 18. Transformers

Short form, sometimes used: **Transformer**

### 18.1 Tasks and Function of Transformers

**Transformers** consist of two windings or coils ('**primary**' and '**secondary**' windings), that are magnetically coupled together. The **primary winding** absorbs electrical energy from an AC voltage generator. The energy is converted to a changing magnetic field that cuts the other winding and also produces here, a changing magnetic field. This induces electrical energy in the **secondary winding** and is available at the output of the transformer. The transformation characteristics of a transformer depend mainly on the magnetic coupling between primary and secondary windings. The density of magnetic flux can be considerably increased by 'closing' the magnetic circuit using ferromagnetic material – in Fig. 18.1.1, this is in the form of an iron core.



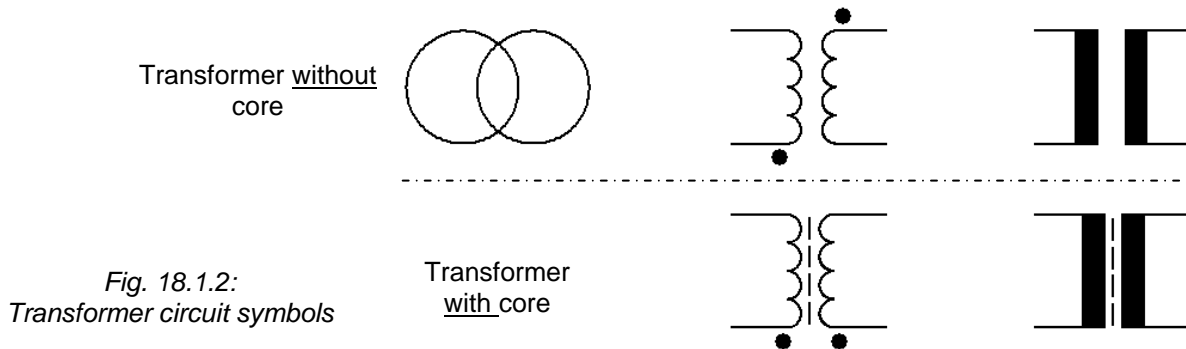
Transformers have the task of matching the electrical properties of an alternating voltage (primary side), to the requirements of a consumer (secondary side). A common example of such a task, is the mains transformer in domestic equipment. Mains outlet sockets, connected to the public mains network, provide a voltage of 220 V. The consumer's equipment however, usually requires a much lower voltage.

Apart from the transformation of energy, transformers can also be used for transforming (matching) currents and resistances (impedances), i.e. matching the output of one circuit to the input of a subsequent circuit. There are many types of matching transformer used in almost all frequency ranges, including high-frequency techniques. In addition to their use for matching electrical properties, transformers are also used for

## Practical Experiments

electrical isolation between circuits where DC voltages must be 'blocked'. This is known as **galvanic isolation**.

There are 3 circuit symbols in common use as shown in Fig. 18.1.2. Dots at the side of the windings, indicate the ends of the winding with the same phase relationship.



### 18.2 Differences between Real and Ideal Transformers

To describe the properties of a transformer, reference is usually made to an ideal transformer:

- In an ideal transformer, there are no losses. Thus, its efficiency is  $\eta = 1$ ; i.e. input and output power are equal.
- When off-load (i.e. no load resistance), an ideal transformer does not consume any active energy.
- All the magnetic flux in the primary coil cuts (or 'threads') the secondary coil; i.e. outside of the core, there is no component present of the magnetic field (no lines of force exist in the free space surrounding the coils); thus, the magnetic coupling between the windings is 100%.
- The waveforms of the input and output alternating voltages are identical; i.e. the signal waveform at the output of the transformer is not distorted.

Its a different picture for real transformers: For example, there are losses of energy that result in an efficiency of  $\eta < 1$ . They are mainly due to resistance losses in the windings and the eddy currents that are produced in the coils. To keep these eddy current losses as small as possible, the cores are constructed from thin laminated strips of soft iron. To reduce distortion of the output signal, the laminations of the core are separated by a very small air gap. However, this leads to a restriction of the magnetic flux that cuts the secondary coil and thus, there is a poorer degree of coupling between primary and secondary sides. The voltage output from the secondary circuit is then less than expected. Power losses or restrictions in the functioning of transformers must be accepted. The formulae described in the following section do not include any considerations of the losses and therefore, apply only to an ideal transformer.



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### 18.3 Voltage, Current and Resistance Transformation (transformation ratio)

The ratio of the number of windings in the primary coil ( $N_1$ ) to the number of windings in the secondary coil ( $N_2$ ), is known as the **turns** or **transformation ratio** and is often indicated by the letter 'T':

$$T = \frac{N_1}{N_2}$$

In an off-load transformer and ignoring losses, this ratio T, also corresponds to the ratio between input and output voltages. To ensure the same power is available in the output circuit as in the primary circuit, the currents are in anti-phase to the voltages:

$$T = \frac{U_1}{U_2} = \frac{I_2}{I_1}$$

The load resistance in the secondary circuit ( $R_L$  or  $R_2$ , Fig. 18.3.1), can be calculated with Ohm's law from the current and voltage. The same applies for  $R_1$ , which is the load of the transformer effective at the AC voltage source:

$$R_2 = R_L = \frac{U_2}{I_2} \quad \text{and} \quad R_1 = \frac{U_1}{I_1}$$

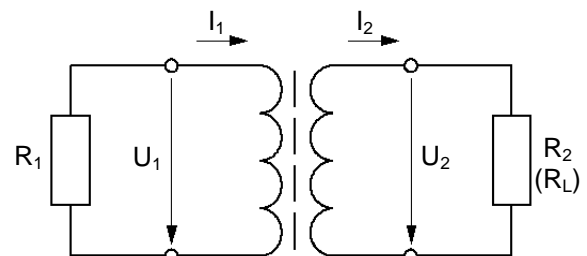


Fig. 18.3.1: Transformer characteristic quantities

When the resistances are formed as a ratio, then :

$$\frac{R_1}{R_2} = \frac{\frac{U_1}{I_1}}{\frac{U_2}{I_2}} = \frac{U_1 \cdot I_2}{U_2 \cdot I_1} = \frac{U_1}{U_2} \cdot \frac{I_2}{I_1} = T \cdot T = T^2 \quad \Rightarrow \quad R_1 = R_2 \cdot T^2 \quad \text{and} \quad T = \sqrt{\frac{R_1}{R_2}}$$

Thus, the load resistance  $R_L$  ( $R_2$ ) is transformed to the primary side as the square of the transformation ratio, T.

## Practical Experiments

### 18.4 Practical Proof of Transformer Effect

The transformation of voltage, current and resistance and their dependence on the transformation ratio,  $T$  as well as the effects of various degrees of coupling, will now be examined with practical exercises.

#### Exercise 1: Various Degrees of Coupling

The dependence of output voltage  $U_2$  and transformation ratio,  $T$  on the magnetic coupling between the windings, will now be examined in 4 different configurations:

- Transformer with core
- Transformer with core and air gap
- Transformer with half-core
- Transformer without core

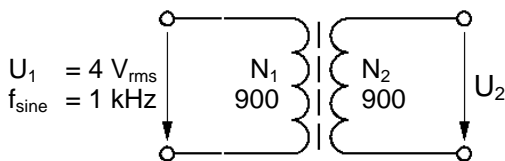
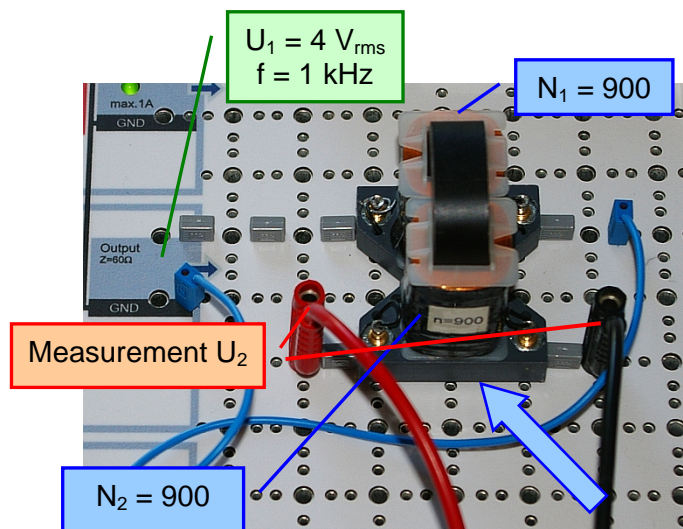


Fig. 18.4.2: Transformer:  $T = 1$

Fig. 18.4.1: Layout, transformer  $N_1=N_2=900$  with core



- Assemble the circuit as shown in Fig. 18.4.2 on the Electronic Circuits Board.

**Note: Ensure that the transformer and coil holders are in contact with the surface of the Board (i.e. not mounted on short circuit plugs, see arrow in Fig. 18.4.1). This will ensure that the core sections are in tight contact with each other.**

- Set the function generator for  $U_1$  to sine-wave voltage  $U_{rms} = 4\text{ V}$ ,  $f = 1\text{ kHz}$ .
- Measure the secondary voltage of the transformer when off-load. Enter the value in table 18.4.3.
- Remove the top half of the core and repeat the measurement (enter the value in the table).

Configuration	$U_2$ [ $V_{rms}$ ]
with core	
with core and air gap	
with $\frac{1}{2}$ core	
without core	

Table 18.4.3: Measured

- To simulate an air gap between the core sections, cut 2 pieces of paper (Fig. 18.4.4 on the next page). Position the paper in the body of the core and replace the upper half of the core.
- Measure  $U_2$  with core and air gap (enter the value in the table).

## Practical Experiments

- Remove the transformer coils, short circuit plugs and connecting leads from the Board. Using 4 mm connecting leads, connect the primary winding to the input voltage  $U_1$ . couple the voltmeter in the same way, to the output of the secondary coil (Fig. 18.4.5).
- Measure the output voltage  $U_2$  without core (enter the value in table 18.4.3). During measurement, make sure that the upper opening of both coil formers align with each other, so that as much of the magnetic lines of force from the primary winding, cut the secondary coil (Fig. 18.4.5).

Fig. 18.4.4:  $U_2$  measurement, core with air gap

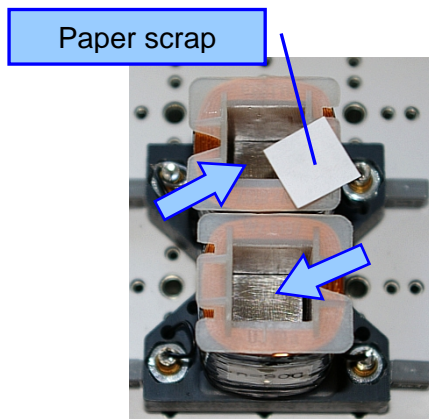
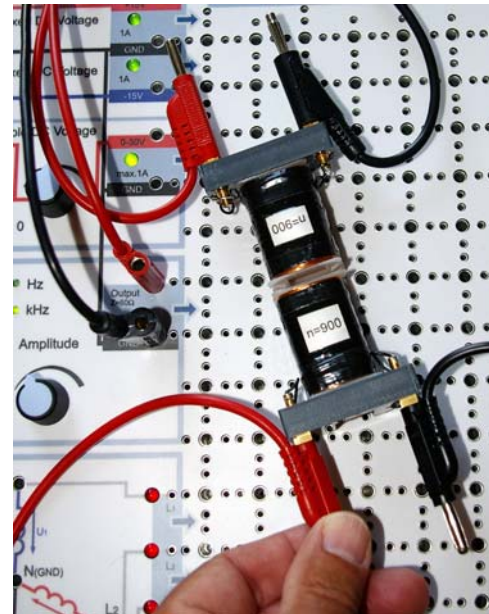


Fig. 18.4.5:  $U_2$  measurement, without core



- Explain the different values measured for the secondary voltage.

- To what extent does the formula for the transformation ratio (or turns ratio)  $T$ , apply the the 4 configurations?

## Practical Experiments

### Exercise 2: Proving the Transformation Ratio (or turns ratio), T

By taking measurements of voltage and current on 2 transformers with a different secondary winding, the relationship between the transformation ratio T and the number of turns in the winding N, will be examined.

- Assemble the circuit as shown in Fig. 18.4.6 on the Electronic Circuits Board. First, use the secondary coil with  $N_2 = 900$  windings.

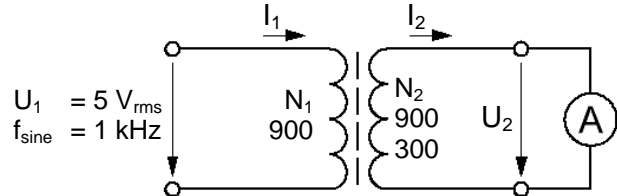


Fig. 18.4.6: Exercise circuit, transformer  $N_2=900$  or 300 with core

- Set the function generator for  $U_1$  to sine-wave voltage  $U_{rms} = 5\text{ V}$ ,  $f = 1\text{ kHz}$ .

- Remove the ammeter, and measure the secondary voltage (with  $N_2 = 900$ ). Replace the secondary coil with the  $N_2 = 300$  windings and repeat the voltage measurement. Enter both values measured in table 18.4.7.

- What is the transformation ratio T, when the number of windings in the coils are taken for the calculation?

With  $N_2 = 900$ :

With  $N_2 = 300$ :

- Calculate the transformation ratio from the measured values of secondary voltage (enter the values in table 18.4.7).

With  $N_2 = 900$ :

With  $N_2 = 300$ :

$N_1$	$N_2$	$U_1$ [V]	$U_2$ [V]	T
900	900	5		
	300			

Table 18.4.7: Voltage measurement

$N_1$	$N_2$	$I_1$ [mA]	$I_2$ [mA]	T
900	900			
	300			

Table 18.4.8: Current measurement

- Now, measure the primary and secondary current for both versions of the transformer. Here, the very low internal resistance of the ammeter present a load to the secondary circuit – as shown in Fig. 18.4.6. Enter the measured values in table 18.4.7.

- Calculate the transformation ratio from the measured values of secondary current (enter the values in table 18.4.8).

With  $N_2 = 900$ :

With  $N_2 = 300$ :

## Practical Experiments

- The coils are now changed over (Fig. 18.4.9). Now, the primary coil has  $N_1 = 300$  windings and the secondary,  $N_2 = 900$  windings. Calculate the value that must be set for the input voltage  $U_1$  to give an off-load voltage at the secondary of the transformer of  $U_2 = 6,5$  V,  $f = 100$  Hz?

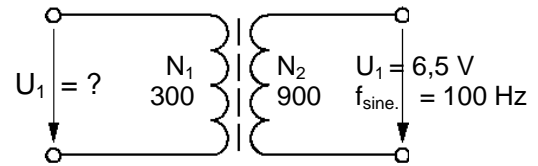


Fig. 18.4.9: Exercise circuit, transformer  $N_1 = 300$ ,  $N_2 = 900$  with core

- Turn the voltage control on the function generators fully counter-clockwise (output voltage = 0 V) and switch off the voltage supply to the Electronic Circuits Board.
- Assemble the transformer on the Electronic Circuits Board as shown in Fig. 18.4.9 and prove your calculations by measurement (Slowly and carefully, increase the voltage at the function generator).

At  $U_2 = 6,5$  V (secondary), measured at the primary side:  $U_1 = \dots\dots\dots$

- During the measurements, sounds can be heard at the transformer, that apparently depend on the frequency of the transformed alternating voltage. At  $f = 1$  kHz this is an unmistakable whistle, then at  $f = 100$  Hz, a humming tone. How are these sounds produced?

### Exercise 3: Resistance (Impedance) Transformation

By voltage and current measurements on a transformer with different transformation ratio's and 2 different load resistors, the relationship between the resistance of primary and secondary circuits will be examined.

- Assemble the circuit shown in Fig. 18.4.10 on the Electronic Circuits Board. First, use the secondary coil with  $N_2 = 900$  windings.

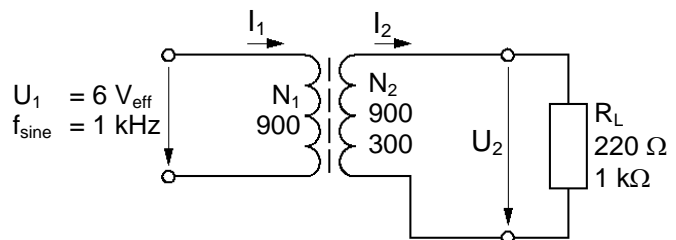


Fig. 18.4.10: Exercise circuit, transformer  $N_2 = 900$  or  $300$  with core

- Set the function generator for  $U_1$  to sine-wave voltage  $U_{rms} = 6$  V,  $f = 1$  kHz.

- Enter the transformation ratio  $T$  for both transformer versions in table 18.4.11.
- Measure the voltage and current for both transformer versions and both load resistors. Enter the values in table 18.4.11.

## Practical Experiments

$N_1$	$N_2$	$T$	$R_L$ [k $\Omega$ ]	$U_1$ [V]	$U_2$ [V]	$I_1$ [mA]	$I_2$ [mA]	$R_1$ [k $\Omega$ ]	$R_2 (R_L)$ [k $\Omega$ ]
900	900		1	6					
	300		0,22						

Table 18.4.11: Measured values, Resistance transformation

- Calculate the transformation ratio  $T$  from the measured values of resistance.

For  $N_2 = 900$  and  $R_L = 1 \text{ k}\Omega$ :

For  $N_2 = 300$  and  $R_L = 220 \text{ }\Omega$ :