

Experiment No : 7	Title: Tuning by Ziegler and Nichols second method
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**Objective:**

To get an automatic tuning for the system  $\frac{1}{(s+1)(s^2+2s+2)}$  since manual tuning is hard to adjust and not available always and the first method condition does not match.

**Theory:**

**The conditions of second method for Ziegler and Nichols theory**

Add gain (Kp) to the system with unity feedback then find the total transfer function and from The characteristic equation apply the Routh–Hurwitz stability criterion if there is appositve value for gain value (Kp) make any value in first coulomb zero then the system make identical oscillation and the Theory is applied and this value of Kp represent Kcr

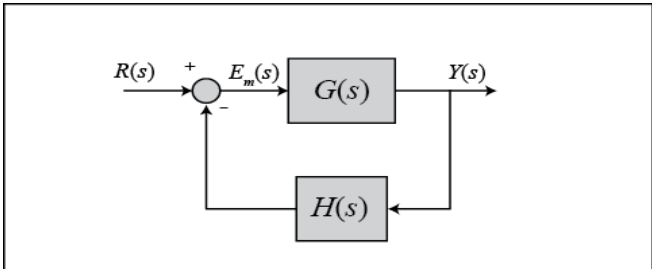
For example  $G(s) = \frac{(s+2)(s+3)}{s(s+1)(s+5)}$

The first method does not applied let check for second method conditions

First add gain to the system with unity feed back

$$T.F = \frac{G(s)}{1+G(s)*H(s)} = \frac{\frac{kp*(s+2)(s+3)}{s(s+1)(s+5)}}{1+\frac{kp*(s+2)(s+3)}{s(s+1)(s+5)}} = \frac{kp(s+2)(s+3)}{s(s+1)(s+5)+kp(s+2)(s+3)}$$

The characteristic equation is  $s(s+1)(s+5)+kp(s+2)(s+3) = s^3+(6+kp)s^2+(5+5kp)s+6kp=0$



The routh array become

$s^3$	1	$5+5kp$
$s^2$	$6+kp$	$6kp$
$s^1$	$\frac{30+35kp+5kp^2}{6+kp}$	
$s^0$	$6kp$	

There is no appositve value of Kp to make any value in first coulomb zero so the theory is not applied

Another example

$$G(s) = \frac{1}{(s+1)(s^2+2s+2)}$$

The first method does not apply let check for second method conditions

First add gain to the system with unity feed back

$$T.F = \frac{G(s)}{1+G(s)*H(s)} = \frac{\frac{kp}{(s+1)(s^2+2s+2)}}{1+\frac{kp}{(s+1)(s^2+2s+2)}} = \frac{kp}{(s+1)(s^2+2s+2)+kp}$$

The characteristic equation is  $(s+1)(s^2+2s+2)+kp = s^3+3s^2+4s+2+kp=0$

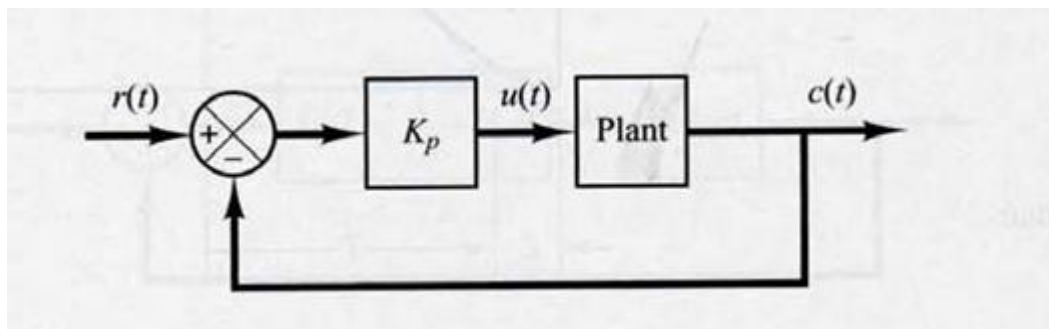
The routh array become

$s^3$	1	4
$s^2$	3	$2+kp$
$s^1$	$\frac{12-2-kp}{3}$	
$s^0$	$2+kp$	

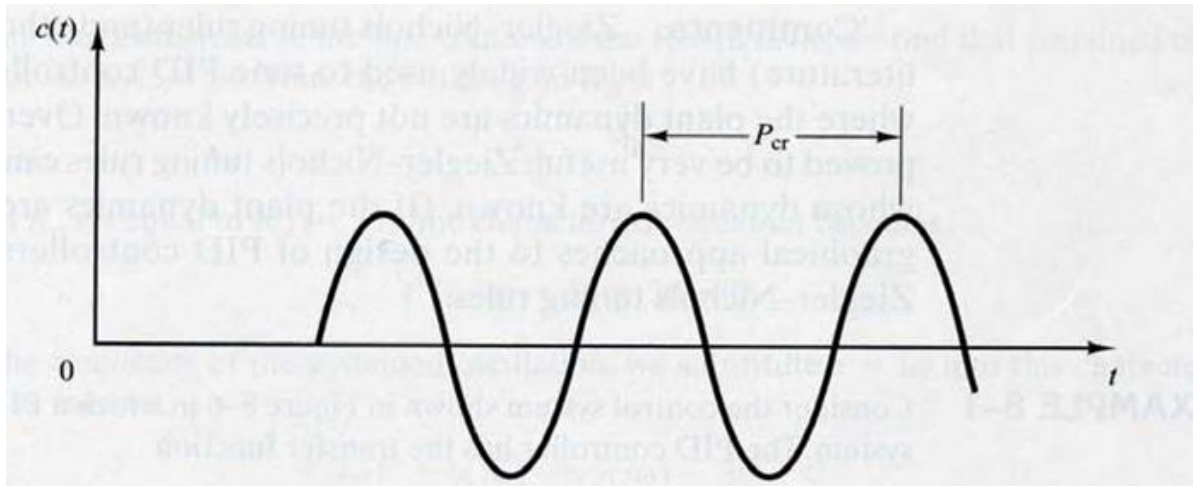
There is appositive value of  $K_p=10$  to make any value in first coulomb zero so the theory is applied for this system

**Second method theory:**

Add again  $kp$  to the system with unity feedback as shown below:



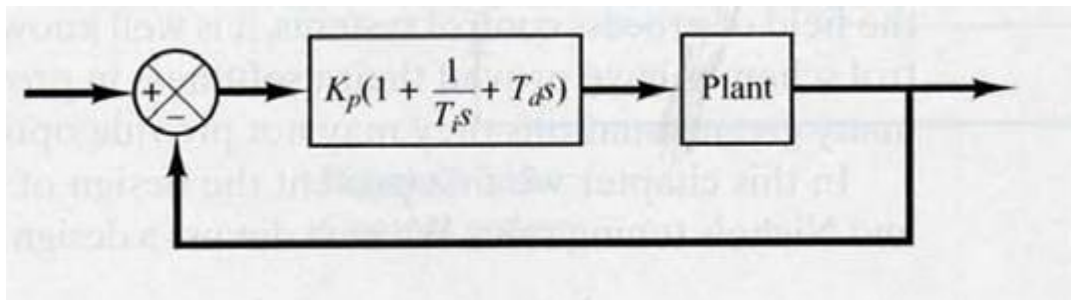
Then increase the value of gain  $K_p$  to get identical oscillation in the output this value of gain that get identical oscillation called  $K_{cr}$  and the distance between any two peak called  $P_{cr}$  as shown below:



Then compensate the values of  $K_{cr}$  and  $P_{cr}$  in the table below:

Type of Controller	$K_p$	$T_i$	$T_d$
P	$0.5K_{cr}$	$\infty$	0
PI	$0.45K_{cr}$	$\frac{1}{1.2}P_{cr}$	0
PID	$0.6K_{cr}$	$0.5P_{cr}$	$0.125P_{cr}$

Then compensate the values of  $K_p$  and  $T_i$  and  $T_d$  in the figure below



The first row represents the response due to P controller

The second row represents the response due to PI controller

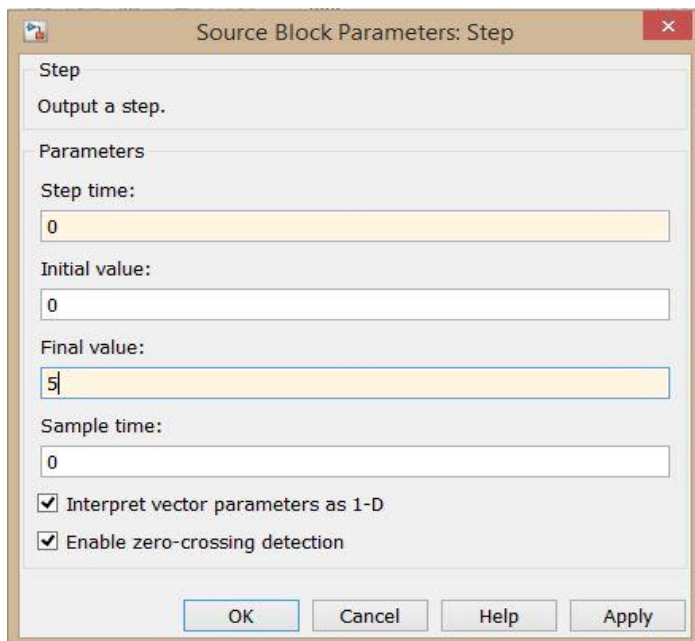
The third row represents the response due to PID controller

## Equipments:

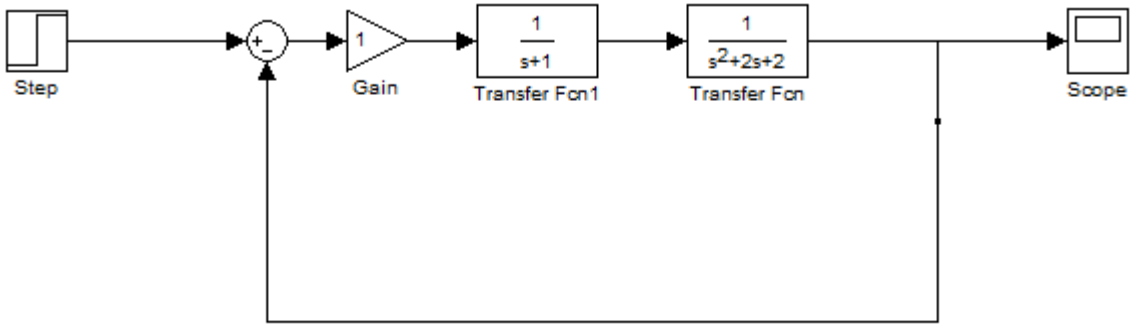
- 1) Step (from 'source')
- 2) Ramp (from 'source')
- 3) Transfer fun. (From 'continuous')
- 4) sum (from 'commonly used block')
- 5) Scope (from 'commonly used block')
- 6) Mux (from 'commonly used block')
- 7) Derivative (From 'continuous')

## Procedure:

1-Double click on the step to change parameter as below:



2- Connect the circuit as below:

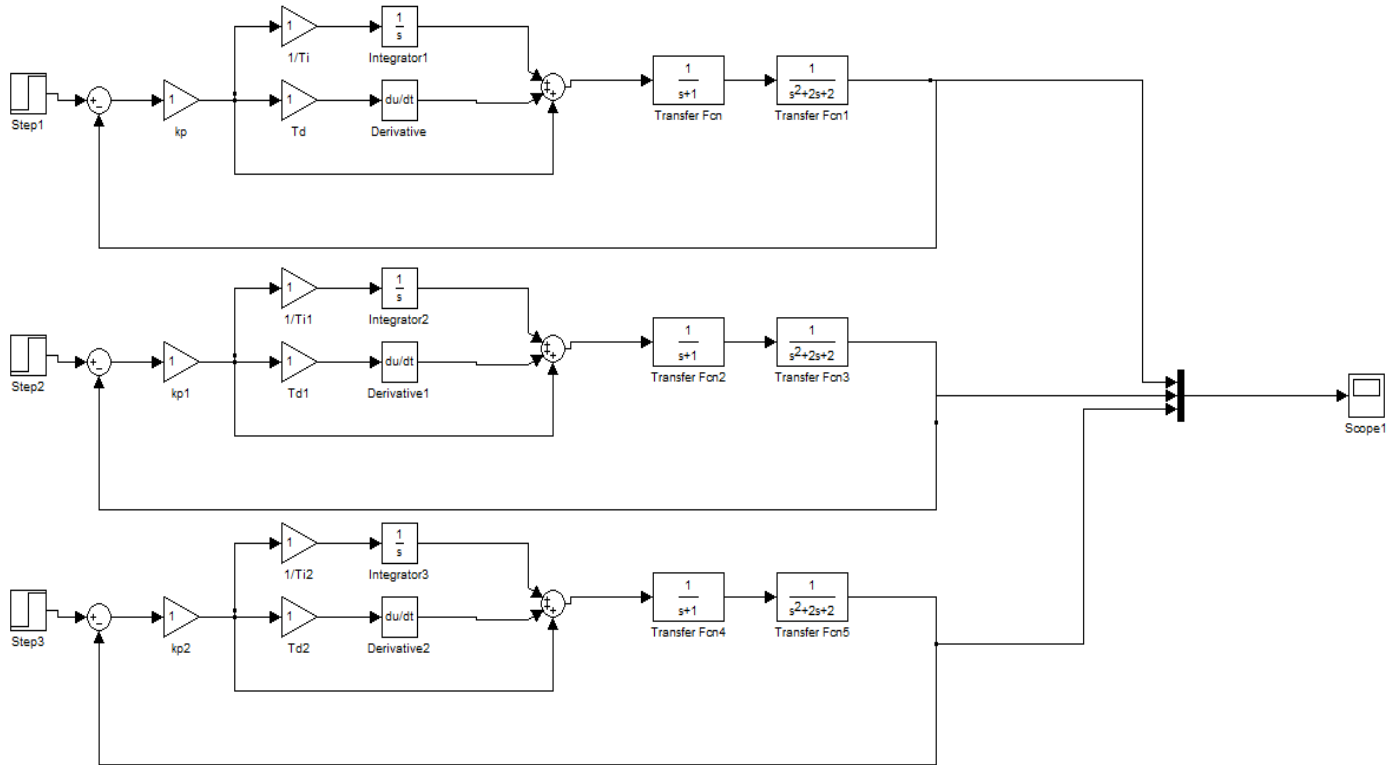


3- Change the value of gain to get identical oscillation in the output this gain called  $K_{cr}$  and distance between any two peaks called  $P_{cr}$

4-Then compensate the values of  $K_{cr}$  and  $P_{cr}$  in the table below:

Type of Controller	$K_p$	$T_i$	$T_d$
P	$0.5K_{cr}$	$\infty$	0
PI	$0.45K_{cr}$	$\frac{1}{1.2}P_{cr}$	0
PID	$0.6K_{cr}$	$0.5P_{cr}$	$0.125P_{cr}$

5-connect the circuit as bellow



Compensate the first row value in above table in first graph

Compensate the second row value in above table in second graph

Compensate the third row value in above table in third graph

And click run

6-Draw the output response

**Question :**

1- What is the effect of P, PI, and PID on the system  $\frac{1}{(s+1)(s^2+3s+3)}$  ?

2- What is the advantage and disadvantage for this theory?

3- Is this tuning method complying with the system needs?

4- Which from P, PI, and PID is the best and why ?

5- What is the output value from PID controller in Laplace if the value of  $k_{cr}=12$  and  $p_{cr}=5$ ?

6- is the theory applied on the system  $\frac{1}{(s+0.5)(s^2+2s+2)}$  check for that if yes what is the value for  $K_{cr}$ ?