

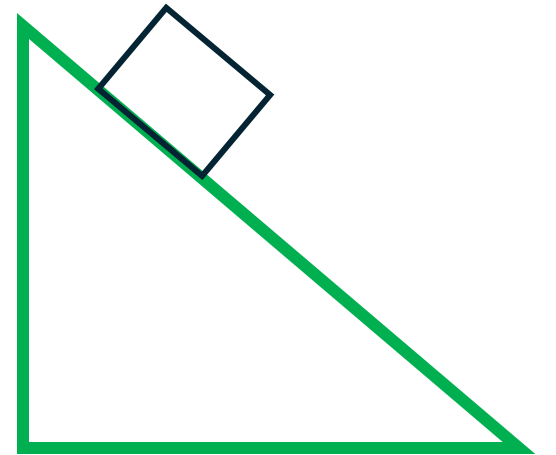
Chapter 5 & 8 problems

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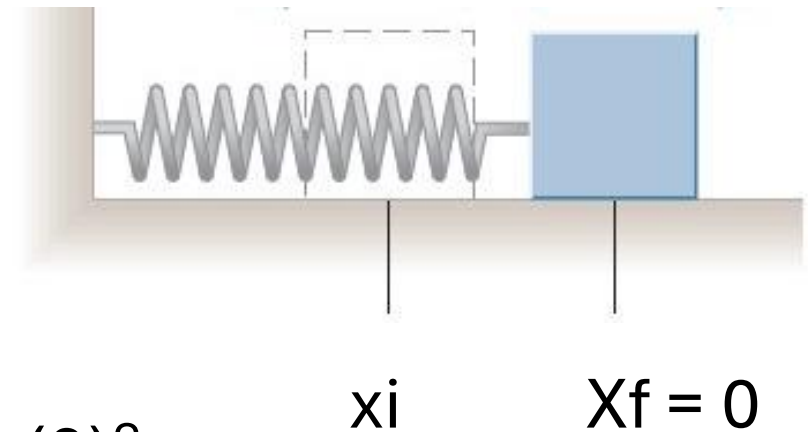
33. A child and sled with a combined mass of 50.0 kg slide down a frictionless hill that is 7.34 m high. If the sled starts from rest, what is its speed at the bottom of the hill?

- $M = 50\text{kg}$, $h = 7.34\text{m}$, $V_i = 0$
- From conservation of energy law:
- $\rightarrow K.E_i + P.E_i = K.E_f + P.E_f$
- $0.5 m V_i^2 + m g h_1 = 0.5 m V_f^2 + m g h_2$
- $0.5 (50) (0)^2 + (50) (10) (7.34) = 0.5 (50) (V_f)^2 + (50) (10) (0)$
- $3670 = 25 V_f^2 \rightarrow V_f^2 = 146.8 \rightarrow V_f = 12.1 \text{ m/s}$



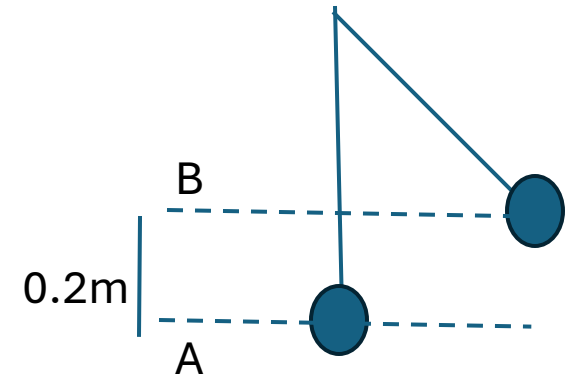
Problem

- An object of mass 2 kg compresses a horizontal spring for 0.1 m on a horizontal track.
- What is the spring constant if the velocity the object moves with at the beginning of the motion is 1 m/s?
- Solution:
- From conservation of energy law:
- ---> $K.E_i + P.E_i = K.E_f + P.E_f$
- ---> $0.5 m v_i^2 + 0.5 k x_i^2 = 0.5 m v_f^2 + 0.5 k x_f^2$.
- ---> $0.5 (2) (0)^2 + 0.5 k (0.1)^2 = 0.5 (2) (1)^2 + 0.5 k (0)^2$.
- $0.005 k = 1$ ---> $k = 1/0.005 = 200 \text{ N/m}$



Problem

- A pendulum swings as shown in the figure. The mass of the ball is 0.1 kg.
- What is the velocity of the object at the bottom of the pendulum if it starts from rest?
- $V_i = 0$,
- Assume point A to be the reference
- $\rightarrow y_A = 0$, $y_B = 0.2\text{m}$
- From conservation of energy law:
- $\rightarrow K.E_i + P.E_i = K.E_f + P.E_f$
- $0.5 m V_i^2 + m g y_A = 0.5 m V_f^2 + m g y_B$
- $\rightarrow 0.5 (0.1) (0)^2 + (0.1) (10) (0.2) = 0.5 (0.1) (V_f)^2 + (0.1) (10) (0)$
- $0 + 0.2 = 0.05 V_f^2 + 0$
- $0.2 = 0.05 V_f^2 \rightarrow V_f^2 = 4 \rightarrow V_f = 2 \text{ m/s}$



20. An engineer weighs a sample of mercury ($\rho = 13.6 \times 10^3 \text{ kg/m}^3$) and finds that the weight of the sample is 4.5 N. What is the sample's volume?

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- $\rho = 13.6 \times 10^3 \text{ kg/m}^3 = 13600 \text{ kg/m}^3$.
- $W = 4.5\text{N}$, $V = ?$
- $W = m g$
- $4.5 = m (10) \rightarrow m = 0.45 \text{ kg}$
- $\rho = m / V \rightarrow V = m / \rho$
- $\rightarrow V = 0.45 / 13600 = 3.3 \times 10^{-5} \text{ m}^3$.

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9. A sample of an unknown material weighs 300.0 N in air and 200.0 N when submerged in an alcohol solution with a density of $0.70 \times 10^3 \text{ kg/m}^3$. What is the density of the material?

- $F_g = W = 300\text{N}$, $F_{\text{net}} = 200\text{N}$, $\rho(\text{liquid}) = 0.7 \times 10^3 \text{ kg/m}^3 = 700 \text{ kg/m}^3$
- $V_o = V(\text{liquid})$
- $F_{\text{net}} = F_B - F_g$
- $\rightarrow -200 = F_B - 300 \rightarrow F_B = 300 - 200 = 100 \text{ N}$
- $F_B = \rho_w \times V_w \times g$, $F_g = \rho_o \times V_o \times g$
- When submerged $\rightarrow F_B / F_g = \rho_w \times V_w \times g / \rho_o \times V_o \times g$
- $\rightarrow \mathbf{F_B / F_g = \rho_w / \rho_o .}$
- $100/300 = 700 / \rho_o \rightarrow 1/3 = 700 / \rho_o \rightarrow 0.333 = 700 / \rho_o$
- $\rightarrow \rho_o = 700/0.333 \rightarrow \rho_o = 2100 \text{ kg/m}^3.$